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Model reduction for controller design for infinite-dimensional systems

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**Model reduction for controller design
for infinite-dimensional systems**

Mark R. Opmeer

Rijksuniversiteit Groningen

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