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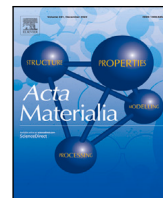
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Full length article



Efficiency, accuracy, and transferability of machine learning potentials: Application to dislocations and cracks in iron

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ABSTRACT

Machine learning interatomic potentials (ML-IAPs) enable quantum-accurate, classical molecular dynamics simulations of large systems, beyond reach of density functional theory (DFT). Yet, their efficiency and ability to predict systems larger than DFT supercells are not fully explored, posing a question regarding transferability to large-scale simulations with defects (e.g. dislocations, cracks). Here, we apply a three-step validation approach to body-centered-cubic iron. First, accuracy and efficiency are assessed by optimizing ML-IAPs based on four state-of-the-art ML packages. The Pareto front of computational speed versus testing root-mean-square-error (RMSE) is computed. Second, benchmark properties relevant to plasticity and fracture are evaluated. Their relative root-mean-square-error (Q) with respect to DFT is found to correlate with RMSE. Third, transferability of ML-IAPs to dislocations and cracks is investigated by using per-atom model uncertainty quantification. The core structures and Peierls barriers of screw, M111 and three edge dislocations are compared with DFT. Traction–separation curve and critical stress intensity factor (K_{Ic}) are also predicted. Cleavage on the pre-existing crack plane is found to be the zero-temperature atomistic fracture mechanism of pure body-centered-cubic iron under mode-I loading, independent of ML package and training database. Quantitative predictions of dislocation glide paths and K_{Ic} can be sensitive to database, ML package, cutoff radius, and are limited by DFT accuracy. Our results highlight the importance of validating ML-IAPs by using indicators beyond RMSE. Moreover, significant computational speed-ups can be achieved by using the most efficient ML-IAP package, yet the assessment of the accuracy and transferability should be performed with care.

1. Introduction

Plastic deformation and fracture in metals are controlled by the motion and interaction of extended defects, such as dislocations, grain boundaries, and cracks. For example, plastic deformation in body-centered cubic (bcc) metals at moderate temperatures is primarily dictated by the mobility of screw dislocations, which is significantly slower than that of edge dislocations as a consequence of the compact core structure [1–4]. Additionally, the competition between crack propagation and dislocation emission from crack-tips controls the intrinsic ductility, which plays a role in determining the fracture toughness [5, 6]. Understanding those mechanisms in pure iron is a fundamental step towards investigating environmental cracking phenomena such as hydrogen embrittlement [7], and liquid metal embrittlement [8]. Therefore, accurate modeling of extended defects at the atomic scale

is a fundamental step to understand and engineer the mechanical properties of metals.

Classical molecular statics/dynamics (MS/MD) simulations are routinely employed to investigate the structure and propagation mechanism of extended defects at the atomic scale. However, in the case of bcc metals like iron, the empirical interatomic potentials (IAPs) struggle to accurately predict the compact screw dislocation core structure and the atomic scale crack propagation mechanism [9–11]. Recent advances in machine learning (ML) techniques have allowed the development of ML-IAPs that are able to predict extended defects with similar accuracy as density-functional theory (DFT) calculations (~ 1 meV/atom), but at a computational speed that is orders of magnitude faster. For instance, ML-IAPs can faithfully replicate the compact core structure of screw dislocations in various bcc transition metals as predicted by DFT [12–15]. More recently, an active learning

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List of abbreviations

ACE	Atomic cluster expansion
BCC	Body-centered cubic
DFT	Density-functional theory
DOFs	Degrees of freedom
GAP	Gaussian approximation potential
LAE	Local atomic environment
MEAM	Modified embedded atom method
ML-IAP	Machine learning interatomic potential
MTP	Moment tensor potential
MS/MD	Molecular statics/dynamics
NEB	Nudged elastic band
NN	Neural network (NN)
PES	Potential energy surface
qSNAP	quadratic spectral neighbor analysis potential
RMSE	Root-mean-square error
SNAP	Spectral neighbor analysis potential
SOAP	Smooth Overlap of Atomic Positions

scheme has been developed within the Gaussian Approximation Potential (GAP) framework, which enables the prediction of fracture mechanisms in bcc iron [16]. These successful applications demonstrate that ML-IAPs are promising tools for simulating mechanisms at the atomic scale. Yet, ML-IAPs suffer from significant computational cost and require extensive validations to test the transferability.

To improve both accuracy and computational efficiency, multiple ML-IAP frameworks have been developed, that differ by the local atomic environment (LAE) expansion approach and the regression method [17–21]. A benchmark study of moment tensor potential (MTP), GAP, spectral neighbor analysis potential (SNAP), and quadratic SNAP (qSNAP) for a wide range of materials (Li, Mo, Cu, Ni, Si, and Ge) was conducted in Ref. [22], showing that root-mean-square error (RMSE) of ~ 1 meV/atom can be achieved for all ML-IAPs at computational speeds spanning two orders of magnitude. The Pareto front of RMSE against computational speed showed that MTP occupies the frontier for all material systems. Following the results in Ref. [22], atomic cluster expansion (ACE) potential has been added and has been shown to occupy the Pareto frontier for copper and silicon, being mildly faster and more accurate than MTP [23]. However, extended defects such as dislocations and cracks have not been investigated in Ref. [22,23]. A recent summary showed that most ML-IAPs consider point defects, stacking faults, and free surfaces as training configurations [24]. For dislocations, grain boundaries and cracks, only a few elements, such as Al, Si, Mo, and W have been explored [14,25–27]. The dislocation core structures in bcc iron have been studied by several ML-IAPs [28–30], yet, the efficiency, accuracy and transferability of ML-IAPs in predicting extended crystal defects, i.e., dislocations and cracks, have not been fully investigated.

Here, we present a systematic training and validation procedure of an array of state-of-the-art ML-IAPs for ferromagnetic bcc iron, which is based on a three-step approach that is summarized in Fig. 1. During ML-IAPs training, several fitting (hyper)parameters are optimized [13,16]. This hyperparameter optimization procedure is an essential step to achieve both accuracy and efficiency, since it affects the convergence behavior of the ML-IAP to the training data as a function of the number of degrees of freedom (DOF). Therefore, the convergence of RMSE (typically below 5 meV/atom) with respect to the DOF constitutes the first criterion to evaluate the accuracy (*criterion I. Converged RMSE* in Fig. 1), and is a standard procedure for verifying the fitting accuracy and avoiding poor/overfitting issues. In general, an increased

number of DOFs may be needed if the ML-IAP fails to pass criterion I. The second checkpoint of an accurate ML-IAP is the relative root-mean-square-error (referred to as quality factor Q) (*criterion II. Quality factor*), which is measured by considering a broad range of benchmark properties that are relevant for plasticity and fracture, such as elasticity, surface/stacking-fault energy *etc.*, and that can be computed with DFT supercells thus enabling direct comparison. Passing *criterion II* ensures the training of a general purpose potential that is capable of replicating DFT predictions for elementary properties. However, its transferability is not guaranteed to the simulation of extended defects encompassing features (e.g. crack-tips, kinks) that were not part of the training database. Therefore, we propose here the assessment of the transferability by computing the per-atom uncertainty as a measure of the degree of extrapolation from the DFT database, for large-scale simulations of extended defects that cannot be computed with direct DFT supercells (*criterion III. Converged per-atom uncertainty*). The model uncertainty has been previously applied to active learning of dislocations [31] and cracks [16]. A converged per-atom model uncertainty below 15 meV/atom (for GAP trained on current database) or below 3 (γ parameter in ACE) indicates that the model is interpolating or extrapolating mildly the DFT data, hence the potential is suitable for simulations involving the tested extended defects. The ML-IAPs are therefore accurate, efficient and transferable if all the three criteria are met. Iterative/active learning can be applied to include more relevant DFT data, if the ML-IAPs fail to pass criteria II and/or III.

In this study, dislocation glide and crack propagation are investigated including model uncertainty quantification. The core structure and Peierls barrier of five dislocations, including $a_0[100](010)$ edge, $a_0[100](011)$ edge, $a_0/2[\bar{1}\bar{1}1](\bar{1}10)$ edge, $a_0/2[111](\bar{1}10)$ 71° mixed (also known as M111), and $a_0/2(111)$ screw, are evaluated by using the Nudged Elastic Band (NEB) approach [32]. Furthermore, we compute the traction-separation (T–S) curves and critical stress intensity factors for {100} and {110} crack planes. In addition, we train an array of GAP models based on an independent, larger iron DFT database to study the influence of the database on the predictions [33]. We demonstrate the consistent accuracy and transferability of GAP ML-IAPs, which can be obtained with the smaller database, as well as the efficiency of ACE ML-IAPs, which can achieve comparable accuracy with up to two orders of magnitude computational speed-up.

The paper is organized as follows. In Section 2, we present the approach used to train and optimize the different ML-IAPs, discussing the main steps of the fitting procedure and the training scripts. This section is intended to guide ML-IAPs users who need to train a new ML-IAP, or extend the database of an existing ML-IAP to enhance the transferability to materials science applications. In Section 3, we predict a variety of properties that are related to plasticity and fracture based on the ML-IAPs from Section 2. In Section 4, we compute the core structures and Peierls barriers for five dislocation characters. In Section 5, we perform fracture simulations for crack systems on {100} and {110} planes at $T = 0$ K and 100 K. We discuss critical issues regarding the validation of ML-IAPs, the choice of the ML framework, the cutoff radius, and the DFT database in Section 6. The main findings are summarized in Section 7.

2. Consistent training of ML-IAPs

To construct a ML-IAP, a set of consistent quantum mechanical data (atomic positions, energy, force and virial stress) needs to be obtained by performing first principle calculations, typically DFT. The atomic coordinates of DFT configurations are represented by descriptors that incorporate permutational, translational and rotational invariance. The machine learning algorithm provides the (unknown) potential energy surface (PES) as a function of the descriptors, by fitting to the DFT data. The training of ML-IAPs involves a range of (hyper)parameters that are crucial for the performance of ML-IAPs, such as the DOFs, the cutoff radius, the weights of energy/force/virial, and the choice of

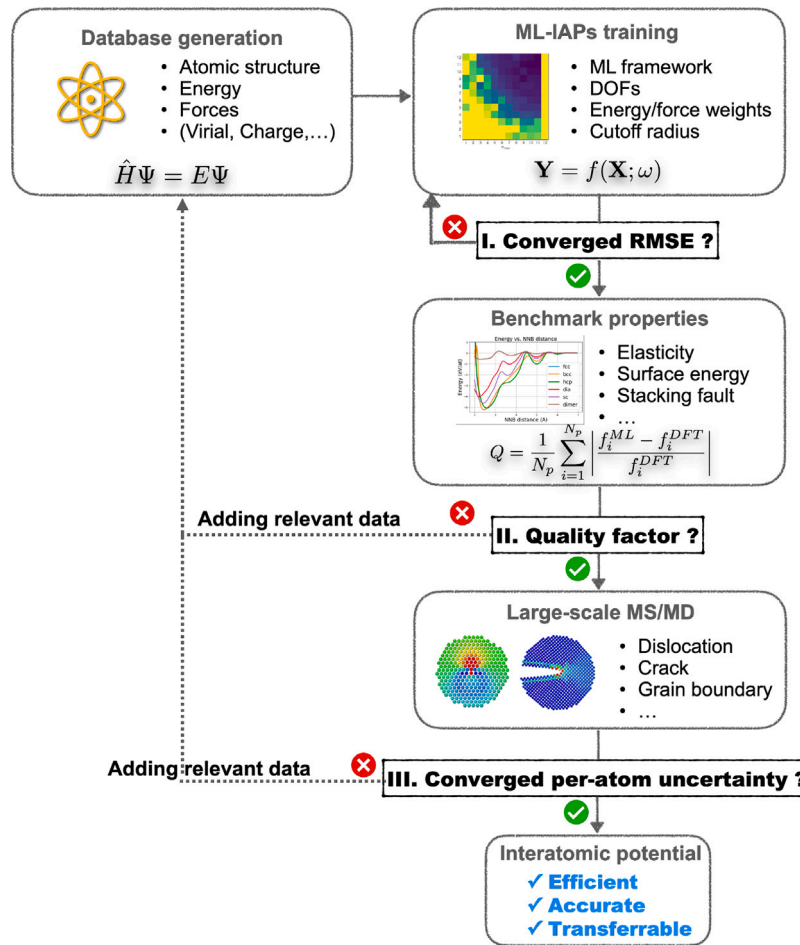


Fig. 1. Flowchart for ML-IAPs training and validation proposed in this work. Three criteria (i.e., I. Converged RMSE, II. Quality factor, III. Converged per-atom model uncertainty) need to be met for an efficient, accurate and transferable ML-IAP.

hyperparameters for the regression task. For MTP and ACE, the DOFs are set by the expansion level of the local atomic environment (LAE), i.e., the descriptor that encodes the local atomic position information. Since the two databases considered in this work are relatively large, a sparse version of the Gaussian process is employed, in which the fitting parameters of GAP are determined by the number of representative sparse points (M). For the neural network (NN) potential, the DOFs depend on the number of layers and nodes of the network architecture. Because the number of potentials to be trained grows exponentially with the number of parameters to vary, we focus on optimizing the DOFs and energy/force/virials weights. In the subsequent subsections, we briefly list the main configurations included in the database and review the key ingredients behind each ML potential that are involved in the optimization of the (hyper)parameters. The training scripts used in this work are available at the url specified in the *Data Availability* Section.

2.1. DFT database

Two iron DFT databases are employed in the current study. The first database, referred to as DB-I, was originally developed for thermomechanics and defects, including dislocations [13,34], and has been extended recently with an active-learned database to predict fracture in single crystal [16]. DB-I has 14,476 configurations and 160,280 LAEs, including the deformed bcc, face-centered cubic (fcc) and hexagonal close-packed (hcp) primitive cells/supercells, point defects, low index surfaces, γ surfaces, surface separation paths and small crack-tips. The

details of the database can be found in Refs. [13,16]. We train five ML-IAPs on DB-I to assess their accuracy and compare their computational efficiency.

Another iron DFT database considered here is extracted from a Fe-H database that was used to train a NN potential, which was developed for modeling hydrogen embrittlement [33]. The pure iron configurations from the Fe-H database are selected, referred to as DB-II. DB-II contains 9,622 configurations (768,986 LAEs) which include deformed supercells, point defects, low index surfaces, γ surfaces, a few symmetric tilt grain boundaries, various dislocation core structures, and inherent structures of the liquid state. More details about DB-II and the DFT calculations can be found in Ref. [33].

Comparing the size of the two databases, DB-II encompasses a number of atomic environments that is ~ 5 times larger than DB-I. The difference between DB-I and DB-II in terms of configuration types is that DB-I includes hcp primitive cells, surface separation paths and crack tips, while DB-II has Bain path, diffusion pathways, symmetric tilt grain boundaries, dislocation structures, and inherent structures of the liquid phase. To investigate the influence of the choice of the database on the prediction of dislocation and fracture properties, we train GAP on both DB-I and DB-II, and we refer to the two potentials as GAP-DB-I and GAP-DB-II.

2.2. Training of ML-IAPs

Here, we use DB-I to train ML-IAPs based on four state-of-the-art packages. All the packages have been previously applied to metallic systems, are open-source, well-documented, ready-to-use, and provide

various examples, including basic training and validation, prediction, and active learning if applicable. Furthermore, these codes are interfaced with the Large-scale Atomic/Molecular Massively Parallel Simulator (LAMMPS), which enables the efficient parallelization of large-scale atomistic simulations (e.g., plasticity and fracture). Although the training is not needed once the potential is obtained, the training efficiency should be considered as one of the performance indices of ML-IAPs, especially when active/iterative learning is used, or in the context of applications where extensive training is required. Note that a fair comparison of the training efficiency is not possible among the employed packages and is not conducted in this study. A brief summary of the main features of the packages employed in the current study is provided in *Supplementary Material S1.1*.

The basic assumption of all these ML-IAPs is the localization of the total energy, whereby the total energy of an atomic system can be written as the sum of per-atom contributions

$$E_{\text{tot}} = \sum_i E_i, \quad (1)$$

where i runs over all atoms of the system. A central task of ML-IAPs is to approximate the local energy E_i , the expansion expression of which differs in each ML framework. In the following, we summarize the LAE expansion approach and the regression method of each ML framework. The training and convergence analysis of RMSE is also presented. The database is randomly split into training and testing sets with a 9:1 ratio for all training realizations. The cutoff radius is set to 6.5 Å if not specified otherwise.

2.2.1. GAP

GAP computes the local energy of atom i based on the Smooth Overlap of Atomic Positions (SOAP) descriptor q_i by [18]

$$E_i = \sum_s \alpha_s K(q_s, q_i) \quad (2)$$

where q_s is the descriptor of atom s from the database. The array α of weights α_s is determined via [12]

$$\alpha = (\mathbf{K}_{MM} + \mathbf{K}_{MN} \mathbf{L} \mathbf{A}^{-1} \mathbf{L}^T \mathbf{K}_{NM})_{MM}^{-1} \mathbf{K}_{MN} \mathbf{L} \mathbf{A}^{-1} \mathbf{t}, \quad (3)$$

where $\mathbf{A} = \sigma_v^2 \mathbf{I}$ is a regularization noise and σ_v is the tolerance (expected error) in fitting the DFT data. Here, we set the default expected energy (σ_v^{energy}), force (σ_v^{force}) and virial (σ_v^{virial}) errors to be 5 meV/atom, 0.2 eV/Å, and 0.01 eV/atom. In practice, it is found that the accuracy of the potential can be improved by choosing different values of the expected errors for different types of input data [12,13]. Therefore, we apply different σ_v^{energy} , σ_v^{force} , and σ_v^{virial} to subsets of the DFT data according to their expected accuracy (see GAP training scripts in *Data availability*). \mathbf{t} is the DFT observable, i.e. total energies, forces and virials. \mathbf{L} is a linear operator that converts the DFT total energy, force and virial into the unknown localized atomic energies. Note that this is a sparse version of the Gaussian process (GP) coefficients, where N is the total number of LAE from the database and M is a representative subset of N .¹ At the evaluation step, the computational cost reduces from $\mathcal{O}(N)$ to $\mathcal{O}(M)$, enabling the simulation of large-scale systems based on a large DFT database. The elements of \mathbf{K} (K_{ij}) are the covariances between q_i and q_j , which is also the kernel that measures their similarity. The dot product kernel is applied

$$K_{ij} = |q_i \cdot q_j|^\zeta, \quad (4)$$

where ζ is a parameter that is used to sharpen the sensitivity towards changes of the atomic positions. Here, $\zeta = 4$ is used [12,13].

¹ The M ($M \ll N$) representative data points are selected using a leverage-score CUR algorithm that is implemented in the *QUIP* package [18,35,36]. Thus, the sparse GP filters out part of the redundant data and reduces the computational cost of both the training and the evaluation steps.

We use the open-source package *Quantum mechanics and Interatomic Potentials (QUIP)* to fit GAP [18,35,36]. A distance-based 2-body descriptor and two TurboSOAP descriptors are employed [37,38], i.e., one “inner” TurboSOAP with $r_{\text{cut}} = 3$ Å and another “outer” TurboSOAP with $r_{\text{cut}} = 6.5$ Å. To ensure convergence of the sparse GP, we investigate the influence of M on RMSE by fixing the LAE expansion ($n_{\text{max}} = 8$, $l_{\text{max}} = 8$). As shown in Fig. 2a, the training and testing RMSE on energies converges at increasing M (>3200). Therefore, we fix $M = 4800$ for the rest of the GAP potentials trained on DB-I. Note that the saturated M is database-dependent. Moreover, the accuracy of GAP depends also on the LAE expansion level [39], which is determined by the radial (n_{max}) and angular (l_{max}) expansion degrees. In order to find the optimal combination of n_{max} and l_{max} , we conduct a grid search. Our findings highlight a fundamental difference between TurboSOAP and original SOAP descriptors (see *Supplementary Material S1.2.1*). The optimal combination of hyperparameters that yields the lowest energy and force RMSE are listed in Table S1 of *Supplementary Material S1.2*. In addition, we provide the convergence analysis of GAP trained on DB-II in *Supplementary Material S1.4*.

2.2.2. ACE

In the general ACE formalism, the local energy is expressed as a function of atomic properties [21,40]

$$E_i = \mathcal{F}(\varphi_i^{(1)}, \dots, \varphi_i^{(P)}), \quad (5)$$

where $\varphi_i^{(p)}$ ($p = 1, \dots, P$) can be expanded as

$$\varphi_i^{(p)} = \sum_{v=1}^{v_{\text{max}}} c_v^{(p)} B_{iv}. \quad (6)$$

$c_v^{(p)}$ are the expansion coefficients to be fitted by the regression algorithm. B_{iv} is the basis constructed by the atomic cluster expansion, where the permutation, reflection, and rotation invariants are incorporated [21]. The \mathbf{B} basis is efficiently reconstructed by the multiplication between the generalized Clebsch–Gordan coefficients and the permutation-invariant \mathbf{A} basis functions (see details in Ref. [21,23]). Two functional forms of \mathcal{F} (Eq. (5)) have been applied recently [23,41]. The simplest model expands the local energy as a linear function of the density

$$E_i = \varphi_i^{(1)} \quad (7)$$

while a nonlinear Finnis–Sinclair-type model is formulated as

$$E_i = \varphi_i^{(1)} + \sqrt{\varphi_i^{(2)}}. \quad (8)$$

We use the *PACEMAKER* package [23,41] to train these two versions of ACE, i.e., the linear and Finnis–Sinclair models (referred to as PACE-L and PACE-FS, respectively). We train PACE-L and PACE-FS with correlation orders $N_c = 3-6$ and energy/force weight coefficients ratio $\kappa = 0.08, 0.16, 0.32$ (weights are defined as $1/\kappa - 1$). The results are shown in Fig. 2b. We find that the correlation order and the weight coefficients ratio have no significant influence on RMSE. The training and testing RMSE on energy for both PACE IAPs are saturated with the increased number of basis functions. PACE-FS converges faster than PACE-L with the increasing number of basis functions, and can reach a smaller RMSE when the number of basis functions is large. The optimal combinations of hyperparameters that yield the lowest energy and force RMSE are given in Table S2 of *Supplementary Material S1.2*. The full convergence plots for the PACE potentials are shown in Fig. S2b of the *Supplementary Material S1.3*.

2.2.3. MTP

MTP represents the local energy of atom i as a linear combination of the complete basis functions set B_α , which is constructed from the moment tensor descriptor [19]

$$E_i = \sum_\alpha \zeta_\alpha B_\alpha(\mathbf{r}), \quad (9)$$

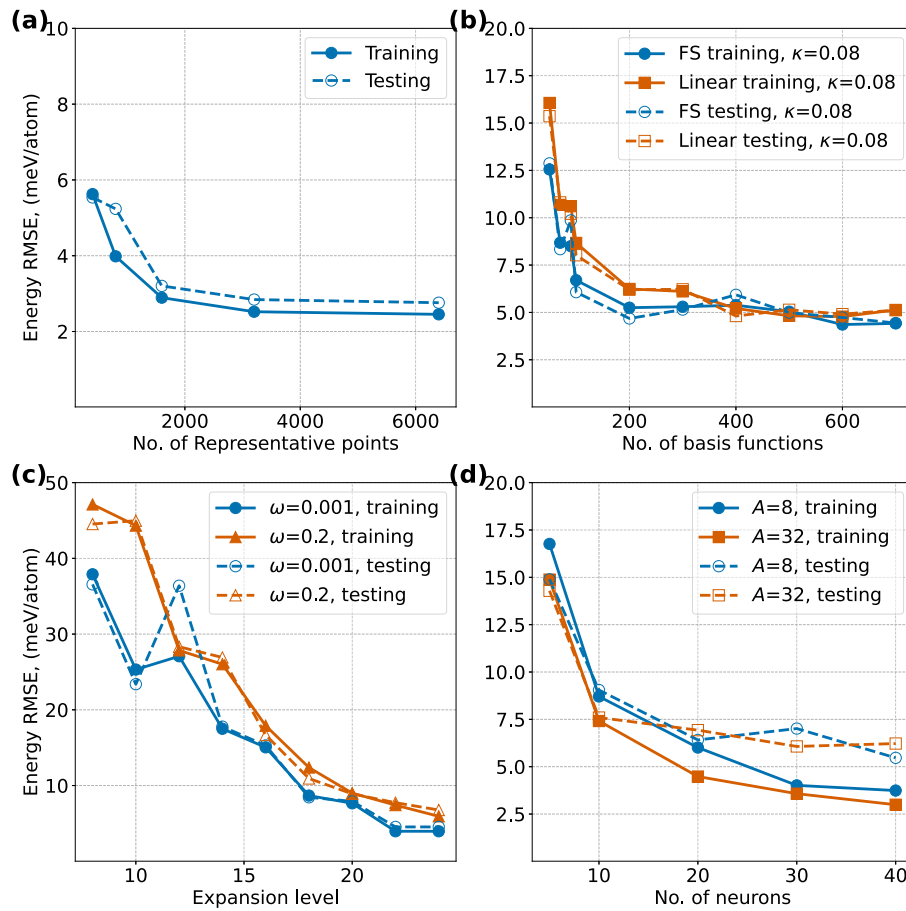


Fig. 2. Training and testing RMSE on energy for (a) GAP, (b) PACE, (c) MTP, and (d) NNP. Solid and dashed lines indicate the training and testing errors, respectively. The number of representative LAE in GAP equals the number of sparse points (M). The energy/force weight ratio is defined as $1/\kappa - 1$ in PACE-FS and PACE-Linear. ω is the energy/force weight ratio of MTP. A is the number of angular basis functions of NNP. For clarity, only representative hyperparameter choices are shown here. The complete hyperparameter optimization is reported in Fig. S2 of the *Supplementary Material S1.3*.

where ζ_α are the coefficients to be fitted. The moment descriptor is designed to be invariant with respect to atomic permutations, rotations, and reflections, and it consists of a radial part and an angular part

$$M_{\mu,\nu}(\mathbf{r}) = \sum_{j \in S_i^{R_c}} \underbrace{f_\mu(|r_{ij}|)}_{\text{radial}} \underbrace{\mathbf{r}_{ij} \otimes \dots \otimes \mathbf{r}_{ij}}_{\substack{\text{angular} \\ \nu \text{ times}}}, \quad (10)$$

where j runs over all atoms inside the cutoff radius R_c , \mathbf{r}_{ij} is the vector of the relative coordinates between atoms i and j , and $|r_{ij}|$ is the distance between atoms i and j . The radial part is expanded inside R_c as

$$f_\mu(|r_{ij}|) = \sum_{\beta=0}^{\beta_{\max}} c_{\mu,\beta} \varphi_\beta(|r_{ij}|) (R_c - |r_{ij}|)^2, \quad (11)$$

where φ_β are Chebyshev polynomials and $c_{\mu,\beta}$ are the radial expansion fitting coefficients. The angular part is defined as ν -times the tensor product of atomic position vectors, encoding the angular information of the atomic environment $S_i \in R_c$. The expansion degree of MTP is determined by μ , ν and β_{\max} . The developers of MTP [42,43] define the *level* of moments as

$$\text{lev}_{M_{\mu,\nu}} = 2 + 4\mu + \nu. \quad (12)$$

This is an optimal relation obtained after a number of tests [42], which is implemented into the *MLIP-2* package [43]. The detailed relation between basis function B_α and expansion level $M_{\mu,\nu}$ is coded into the *MLIP-2* package and can be found in Ref. [42,43]. The number of basis functions is determined by the *level* of moments, which determines

how many times the contractions of the moments are performed. We train MTP with *levels* ranging from 8 to 24. The force weights (ω) are optimized by fixing the energy weights to 1 and virial weights to 0.05, as plotted in Fig. 2c. Both energy and force RMSE are converged with the increased level of expansion, reaching the accuracy limit at $\text{lev} = 22$. $\omega = 0.001$ has lower energy RMSE than $\omega = 0.2$, which is expected because of the reduction of the force weights in the loss function. The optimal combination of hyperparameters that yields the lowest energy and force RMSE are given in Table S3 of *Supplementary Material S1.2*.

2.2.4. NNP

NN potentials were first introduced by Behler and Parrinello to describe the atomistic PES [17]. Here, we apply a 2-layers NN, in which the atomic energy of atom i is expressed as

$$E_i = f_1^{(3)} \left\{ b_1^{(3)} + \sum_{k=1}^{k_{\max}} w_{k1}^{(23)} \cdot f_k^{(2)} \left[b_k^{(2)} + \sum_{j=1}^{j_{\max}} w_{jk}^{(12)} \cdot f_j^{(1)} (b_j^{(1)} + \sum_{i=1}^{\mu} w_{ij}^{(01)} \cdot G_i^\mu) \right] \right\}, \quad (13)$$

where j_{\max} and k_{\max} are the number of nodes in the first and second hidden layer, w and b are the weights and the bias to be fitted, f are the activation functions (which can be different for each node), and G_i^μ is the atomic symmetry function (ASF) that describes the LAE.

We use the *n2p2* package to train NNPs [17,44,45]. *n2p2* implements multiple atomic symmetry functions, activation functions, and cutoff functions. The radial and angular symmetry functions are chosen

to be

$$G_i^2 = \sum_{j \neq i} e^{-\eta(r_{ij}-r_s)^2} f_c(r_{ij}) \quad (14)$$

and

$$G_i^9 = 2^{1-\zeta} \sum_{\substack{j,k \neq i \\ j < k}} (1 + \lambda \cos \theta_{ijk})^\zeta e^{-\eta((r_{ij}-r_s)^2 + (r_{ik}-r_s)^2)} f_c(r_{ij}) f_c(r_{ik}), \quad (15)$$

respectively [17,46], where r_{ij} is the distance between atoms i and j , θ_{ijk} is the angle formed by atom triplets centered on atom i , r_s and η are Gaussian center and width parameters, $\zeta \in \{1, 6\}$ and $\lambda \in \{-1, 1\}$ are two hyperparameters. A logistic activation function $f_a(x) = 1/(1 + e^{-x})$ is applied for two hidden layers and the identity function $f_a(x) = x$ is used for the output layer. The cutoff function is set to $f_c(x) = ((15 - 6x)x - 10)x^3 + 1$.

The influence of the angular expansion level and the number of neurons is explored by fixing the radial expansion to 10 and the force weight ratio (relative to energy) to 0.1. Fig. 2d plots the energy RMSE as a function of neuron numbers for different numbers of angular basis functions. The test RMSE is saturated with 20 neurons. The increase of A does not reduce the RMSE significantly, which indicates that $A = 8$ is enough to encode the 3-body interactions. The optimal combinations of hyperparameters that yield the lowest energy and force RMSE are given in Table S4 of *Supplementary Material S1.2*.

2.3. Model uncertainty quantification

In this work, model uncertainty quantification is proposed as the final step of the ML-IAP validation procedure (Fig. 1). In Section 4, we make extensive use of the per-atom uncertainty of GAP and PACE in order to assess the degree of extrapolation of the LAE from the configurations that are present in the training database. This approach can be applied within the context of benchmark simulations of extended defects, and it enables to verify the transferability of the ML-IAPs to large scale simulations involving these defects. The per-atom uncertainty of GAP, which is the square root of the Gaussian process variance and has units of energy, has been widely used in iterative/active learning [16,47,48]. We use QUIP package to evaluate the GAP variance. PACEMAKER package implements the per-atom uncertainty based on the extrapolation degree γ of the local atomic environment. This extrapolation degree reflects a geometric distance between the predicted atomic environment and the atomic configurations in the database, and is computed based on D-optimality [49]. The evaluation of γ can be directly invoked via LAMMPS commands.

2.4. ML-IAP performance and cost assessment

Fig. 3a shows the testing energy RMSE of the optimized ML-IAPs as a function of the number of DOFs (see Fig. S4 of the *Supplementary Material S1.3* for the force RMSE counterpart). The error bars indicate the standard deviation, which is computed based on five independent trainings. All ML-IAPs are able to reach a testing RMSE lower than 5 meV/atom, indicating that a good fitting accuracy can be achieved by increasing the number of DOFs. NNP shows the largest error bar compared with the other ML-IAPs, reflecting the stochastic nature of neural networks. In particular, GAP shows the minimum test RMSE (~ 2 meV/atom) and MTP can reach 5 meV/atom accuracy with the minimum number of DOFs, compared with the other ML-IAPs. Since all ML-IAPs can reach comparable testing RMSE, albeit at different DOFs and hence model complexity, efficiency is expected to be an important benchmark property. We calculate the computing cost of all ML-IAPs by performing MD in the NVE ensemble for 16,000 atoms using 32 cores. The performance of parallelization is involved in this benchmark study, since our interest is in large-scale MD simulations where parallelization is unavoidable. The test energy RMSE against computational cost is plotted in Fig. 3b. The force RMSE versus computational cost

is reported in Fig. S4b of the *Supplementary Material S1.3* and shows a similar trend. For each ML-IAP, energy and force RMSEs decrease with the increase of the computational time. The energy RMSE of ~ 5 meV/atom can be achieved for all ML-IAPs. In particular, GAP is able to reach an accuracy of ~ 2 meV/atom. All force RMSEs converge to ~ 0.04 eV/Å except for NNP (~ 0.06 eV/Å). PACE-L and PACE-FS are close to each other, occupying the Pareto frontier of the energy and force RMSE. GAP is also on the Pareto front of the energy RMSE, yet at much longer computational timescales. The speed of MTP ranges from being the fastest to being one order of magnitude slower, indicating the rapid growth of the computational cost upon increasing the expansion level. GAP has the lowest energy RMSE but is up to two orders of magnitude slower than PACE-FS. It is worth noting that TurboSOAP descriptor is applied in this study, which is already two orders of magnitude faster than the ordinary SOAP [38].

We have optimized an array of ML-IAPs, that achieve close-to-DFT accuracy (measured in terms of test RMSE) at different degrees of computational efficiency. In the following, we investigate the ability of these ML-IAPs to predict benchmark properties that are relevant to applications, i.e. dislocations and cracks.

3. Accuracy of the prediction of benchmark properties

The purpose of ML-IAPs is to predict physical/chemical properties/processes in extended systems (that include defects such as dislocations, cracks, grain boundaries) with quantum accuracy. The atomistic structure and the mobility of these extended defects depend on a number of elementary properties, which should be predicted with sufficient accuracy by ML-IAPs. Here, we predict the lattice parameter (a_0), the vacancy formation energy (E_v), the elastic constants (C_{ij}), the surface energies of low-index planes (γ_s) and the unstable stacking fault energies associated with active slip planes in bcc crystals (γ_{us}). These physical properties are related to either dislocation (see Hirth and Lothe [50]) or fracture properties (see Griffith [51] and Rice [52] theories).

To allow for a quick comparison of the quality of these ML-IAPs, we introduce the quality factor Q

$$Q = \sqrt{\frac{1}{N_p} \sum_{i=1}^{N_p} \left(\frac{f_i^{ML} - f_i^{DFT}}{f_i^{DFT}} \right)^2}, \quad (16)$$

where f_i is the value of the property (a_0 , C_{ij} , E_v , γ_s , and γ_{us}) computed with either the ML-IAP or DFT (see Fig. S6 of the *Supplementary Material S2.1* for generalized stacking fault energy profile). N_p is the total number of properties. All the ML-IAP calculations are performed in LAMMPS [53] using the workflow made publicly available at the url provided in the *Data Availability* section. The benchmark properties predicted by DFT are listed in Ref. [13], and are consistent with the database that has been used for the training of the five ML-IAPs (DB-I). Fig. 4a shows the benchmark properties predicted by the ML-IAPs with the smallest Q . With only a few exceptions, all ML-IAPs are capable of reproducing the benchmark properties with a relative error equal or smaller than 5%, highlighting the accuracy of the ML-IAPs. PACE-L underestimates C_{11} by 13% and NNP overestimates γ_{us} ($\{110\}$ plane) by 9.8%. The PACE-L and NNP performance can be improved by increasing the training weights, in the loss function, of the elastically-deformed and γ surface structures, respectively. The results however suggest that a converged RMSE does not indicate the ability to predict all the desired physical properties at high accuracy.

Fig. 4b shows the correlation between the test energy RMSE and Q (see Fig. S7 of the *Supplementary Material S2.2* for the force RMSE counterpart). The overall trend is that a smaller RMSE correlates to lower Q , especially for MTP, GAP, and PACE-L. Q is not significantly improved with a further reduction of the energy RMSE, therefore confirming the observation that low RMSE alone cannot be used as an indicator for highly accurate physical property predictions. For

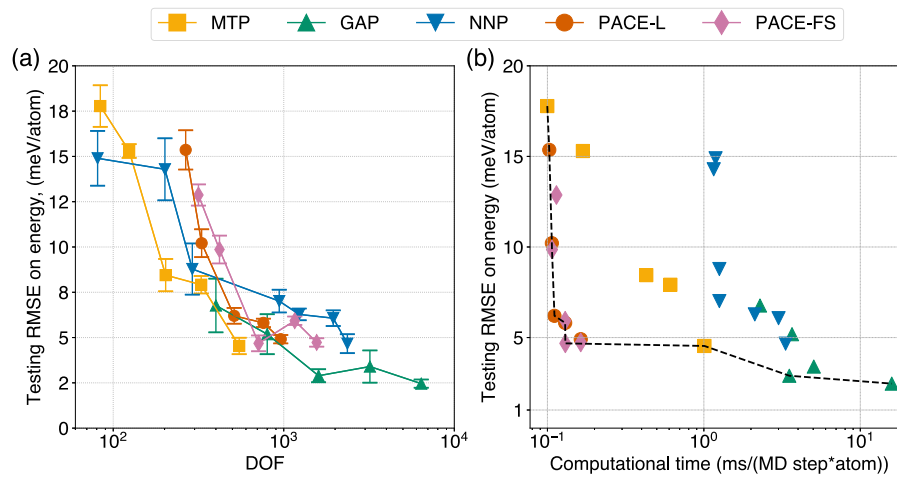


Fig. 3. (a) Testing energy RMSE as a function of the number of DOFs for the five ML-IAPs considered in the current study. (b) Testing energy RMSE versus computational cost for the different ML-IAPs. The black dashed line indicates an approximate Pareto frontier formed by the convex hull of points lying on the bottom left of the chart, which approximates an optimal trade-off between accuracy and computational cost. The computational cost is assessed via LAMMPS calculations of parallelized simulations using 32 cores on a AMD Rome CPU, 7H12 (2x), 64 Cores/Socket, 2.6 GHz, 280 W.

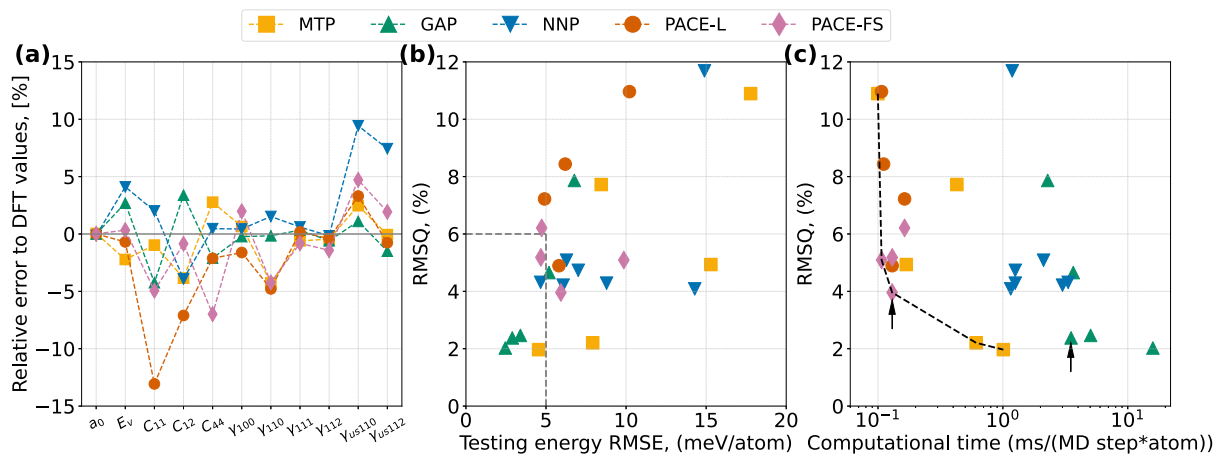


Fig. 4. (a) Relative errors with respect to DFT for various material properties predicted by five ML-IAPs with the lowest Q . In particular, lattice parameter (a_0), vacancy formation energy (E_v), elastic constants (C_{11}, C_{12}, C_{14}), surface energies ($\gamma_{100}, \gamma_{110}, \gamma_{111}, \gamma_{112}$) and maximum (unstable) stacking fault energies on $\{110\}$ and $\{112\}$ planes are considered. (b) Error index Q as a function of the test energy RMSE. (c) Error index Q as a function of the computational speed. The measurement of the computational speed is detailed in Fig. 3 and related main text. The potentials highlighted by the arrows are used for further validation in the following sections.

example, there is no apparent relationship between Q and RMSE in the case of PACE-FS. Non-linear models, such as NNP and PACE-FS, predict $Q < 6\%$ for RMSE 5–10 meV/atom, indicating that non-linear models with significant RMSE can still predict physical properties accurately.

Moreover, Q is plotted as a function of the computational speed, as shown in Fig. 4c. The Pareto front is occupied by PACE-L, PACE-FS and MTP, and is slightly different from the Pareto front based on RMSE in Fig. 3b. This result further indicates the limitation of using RMSE as the only measure of the ML-IAP quality. All potentials can reach an average error Q lower than 3%, and the smallest Q , which is predicted by GAP and MTP, is less than 1.5%. Since PACE-FS and GAP occupy the Pareto front (Figs. 3b and 4c) as the most efficient and accurate ML-IAPs respectively, they are selected to perform further validation based on benchmark MD simulations of dislocations and cracks. Additionally, since the per-atom model uncertainty quantification is implemented in both GAP and PACE frameworks, this will be used in order to benchmark the ML-IAP performance for the prediction of extended defects. As highlighted by the arrows in Fig. 3c, GAP ($l_{\max} = 8$, $n_{\max} = 8$) and PACE-FS ($B = 400$, $\kappa = 0.08$) with the lowest Q are selected for further testing. GAP is trained on two databases (DB-I and DB-II) in

order to assess the impact of the database selection on the prediction of dislocation properties and fracture mechanism.

4. Dislocation core structures and Peierls barriers

In this section, we focus on the prediction of dislocation properties and fracture mechanisms using three potentials, i.e., GAP-DB-I, GAP-DB-II ($l_{\max} = 8$, $n_{\max} = 8$) and PACE-FS (trained on DB-I). Screw, edge and mixed dislocation characters are investigated. The screw dislocation is known to control the low-temperature plasticity in bcc iron [1,4]. $a_0/2[111](1\bar{1}0)$ 70.5° mixed dislocation (referred to as M111 dislocation) has been shown to be an important character during dislocation loop expansion in bcc Ta at low temperature [54], yet the importance for bcc iron remains to be established. Since edge dislocations in bcc iron are known to be extremely mobile, they are of less interest than screw characters. However, edge dislocations can also be formed via dislocation interactions, which may control the intersection node mobility that plays an important role in dislocation network evolution [55]. Therefore, the core structures and Peierls barriers of screw, $a_0[100](010)$ edge, $a_0[100](011)$ edge, $a_0/2[\bar{1}\bar{1}1](1\bar{1}0)$ edge,

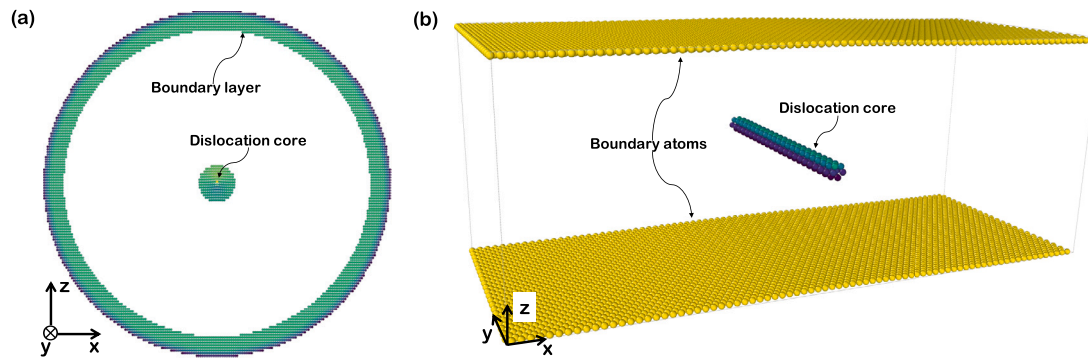


Fig. 5. (a) Rigid boundary (RB) configuration and (b) Periodic array of dislocation (PAD) configuration. Both configurations are used to find the equilibrium structure of the dislocation. PAD configuration is further used for the NEB calculations.

Table 1
Crystallographic orientations of the dislocation configurations.

Dislocation	Character	x	y	z
$a_0/2[111]$	screw	$[\bar{1}21]$	$[111]$	$[\bar{1}01]$
$a_0[100](010)$	edge	$[100]$	$[010]$	$[001]$
$a_0[100](011)$	edge	$[100]$	$[011]$	$[011]$
$a_0/2[\bar{1}\bar{1}1](1\bar{1}0)$	edge	$[11\bar{1}]$	$[\bar{1}21]$	$[101]$
$a_0/2[111](1\bar{1}0)$	70.5° mixed	$[12\bar{1}]$	$[\bar{1}\bar{1}1]$	$[101]$

and M111 dislocations are computed at $T = 0$ K under zero applied stress.

The rigid body (RB) configuration is employed to find the equilibrium core structure of the dislocation (Fig. 5a). In the RB configuration, a single dislocation is put at the center of a cylinder ($r \approx 160$ Å) by applying the anisotropic linear elastic displacement field to all atoms [56]. The open source software *Atomsk* is used to generate the initial configurations with the linear elastic displacement field [57]. The atoms in the inner cylinder ($r \approx 140$ Å) are allowed to relax while the atoms in the outer rim of the cylinder are kept fixed [58]. Periodic boundary conditions (PBC) are applied along the dislocation line direction (y). A convergence test is conducted to ensure that the predicted dislocation core structure is converged with respect to the configuration radius. In order to compare with the DFT predictions [58], we apply the RB configuration and relax the dislocation structures using a combination of conjugate gradient (CG) and FIRE algorithm with a force tolerance of 10^{-12} eV/Å and 10^{-3} eV/Å, respectively.

Next, periodic array of dislocations (PAD) configuration is used to compute the Peierls barrier [56] (Fig. 5b). The sample orientations used for modeling different dislocation characters are listed in Table 1. PBCs are applied along the dislocation line (y) and the slip (x) directions. We apply the climbing-image nudged elastic band (CI-NEB) method to calculate the Peierls barrier for all dislocation characters [32]. CI-NEB requires the initial and final configurations of the dislocation glide process. The initial and final PAD configurations are constructed by following the procedure described in section 2.3 of Ref. [56]. All models are generated in LAMMPS and the corresponding scripts are provided at the url reported in the *Data Availability* section. At the start of the NEB calculations, replicas are created by linear interpolation of the atomic positions between the initial and final states. We use 64 replicas and the FIRE algorithm with a force tolerance of 10^{-3} eV/Å [59]. The predicted atomic positions around the dislocation cores are compared quantitatively with published DFT calculations [58].

4.1. Screw dislocation

Fig. 6a shows the Peierls barrier, that is the energy barrier (per unit dislocation length in terms of the Burgers vector magnitude b) for a short screw dislocation (here, $2b$ along y) to glide from the

easy core position to an adjacent easy core position. The reference DFT data is taken from Ref. [13] and is consistent with the DB-I database. The energy of the end replica is ~ 10 meV/ b larger than the initial replica because the small DFT quadrupole cell geometry is not optimized with respect to the tilt components along the Burgers vector [4,60]. This induces elastic interactions between dislocations in the quadrupole configuration as one of the dislocations moves along the Peierls path [4,34]. Therefore, the actual DFT predicted Peierls barrier [13] lies in between 48 and 58 meV/ b . The GAP-DB-I and PACE-FS predicted Peierls barriers are within this range and hence consistent with. The prediction from GAP-DB-II (53.6 meV/ b) also falls into this range. The differential displacement map of the screw dislocation is calculated, showing a compact dislocation core structure (see Fig. S8 of the *Supplementary Material S3.1*).

We further compute the dislocation trajectory along the migration path using GAP-DB-I, as shown in the inset of Fig. 6a. The dislocation core position along the migration path is determined by computing the displacement differences among the three innermost $\langle 111 \rangle$ columns of atoms (see Ref. [28]). The trajectory shows that the screw dislocation glides along an almost flat path, crossing in between the hard core and the split core configurations, which is in good agreement with other ML-IAPs [28] and DFT calculations [4,61]. This means that the Peierls barrier configuration lies at the saddle point that is located between the higher energy hard and split core configurations [3]. In order to verify this, we calculate the energy profile between the hard and split core positions. The path is obtained by interpolating linearly the in-plane displacements of the three innermost $\langle 111 \rangle$ atomic columns between the hard core and the split core configurations. The energy profile is evaluated by keeping the in-plane displacements of these three atomic columns fixed while relaxing the rest of the atoms (see *Supplementary Material S3.2* for details). As shown in Fig. 6b, all the tested ML-IAPs (GAP-DB-I, GAP-DB-II and PACE-FS) are able to predict a local minimum along the hard-to-split transition path. Moreover, both GAP-DB-I and GAP-DB-II predict that the hard core is lower energy than the split core, consistent with previous DFT calculations [3,4]. The computed model uncertainty for GAP-DB-I is less than 10 meV/atom (see insets of Fig. 6b). Therefore, GAP-DB-I is improved with respect to the previous GAP18 [28], since GAP-DB-I has been trained on a database that has been extended to enable fracture predictions [16], and hence it contains a larger amount of distorted DFT supercells compared with the original GAP18 database. Instead, PACE-FS cannot capture the correct energetic hierarchy (hard core lower energy than split core). However, we have verified that by fitting PACE-FS to DB-II the correct energy hierarchy is predicted. This is consistent with the fact that DB-II includes DFT supercells with various screw dislocation structures. In *Supplementary Material S3.3*, the ability of GAP and PACE-FS to reproduce the DFT energies of the dislocation configurations from DB-II is shown. It is also shown that GAP converges to the DB-II hard-to-split path data as the number of DOFs is increased, while PACE-FS

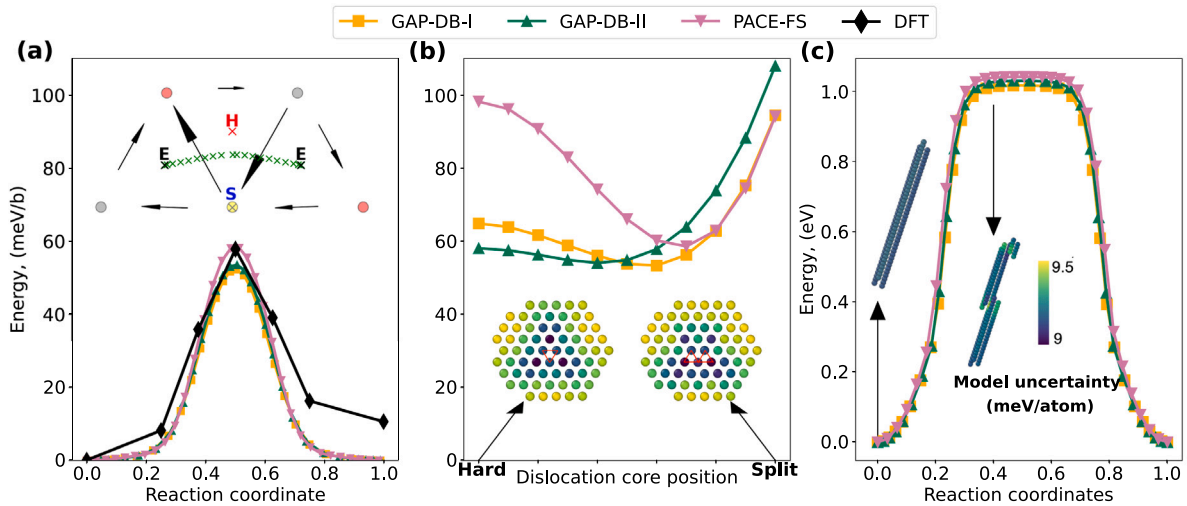


Fig. 6. (a) Peierls potential computed with the PAD configuration at $T = 0$ K and zero applied stress. The DFT results are taken from Ref. [13], which uses a quadrupolar cell without elastic corrections. The inset shows the Peierls path, and the differential displacement (DD) map for the configuration at the Peierls barrier, predicted by GAP-DB-I. Atoms are colored according to the three possible positions along the dislocation line direction in the pristine bcc crystal, for one periodic unit cell (length b). E, H, and S indicate the easy, hard and split core positions, respectively. The dislocation trajectory, indicated by the green symbols “x” is calculated according to Ref. [3,28]. (b) Energy profile between the hard and the split core positions. The insets are the hard and the split dislocation core structures, colored according to the GAP model uncertainty. The red circles indicate the centers of the dislocation cores in the two configurations (two circles in the split configuration indicate the center of the split core partials). (c) The energy barrier for the kink-pair nucleation process. The insets show the atoms close to the dislocation core at the initial configuration and in the middle of the transition path. Atoms are colored according to the GAP model uncertainty.

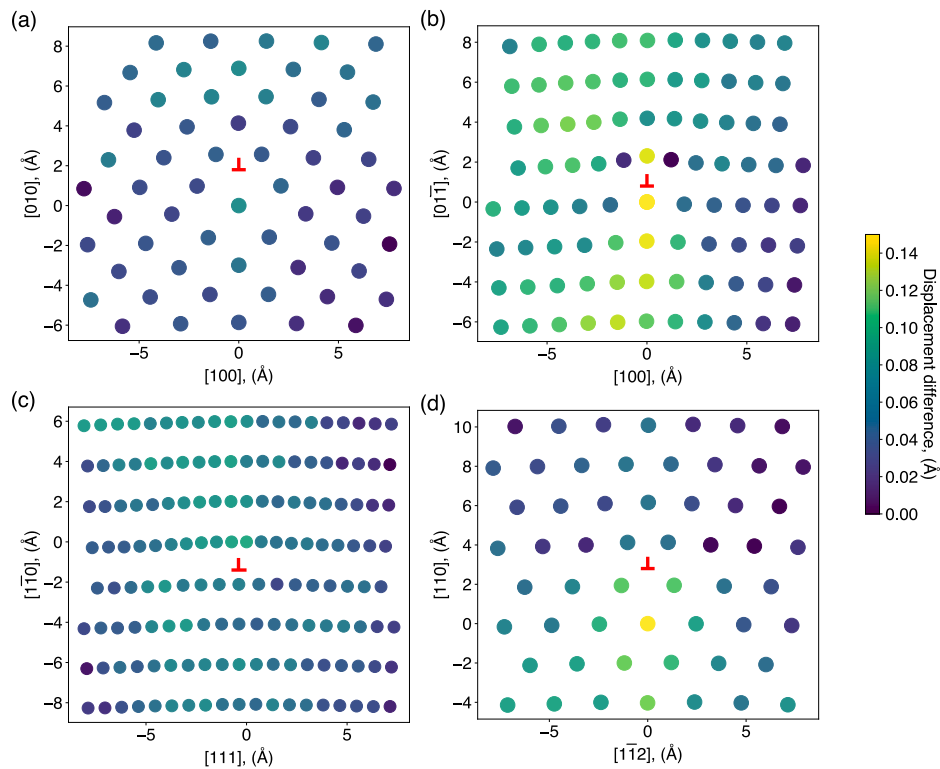


Fig. 7. Core structures predicted by GAP-DB-I: (a) $a_0[100](010)$ edge, (b) $a_0[100](011)$ edge, (c) $a_0/2[\bar{1}\bar{1}1](1\bar{1}0)$ edge, and (d) $a_0/2[111](1\bar{1}0)$ M111 dislocations. Atoms are colored by the displacement difference relative to DFT predictions [58]. The dislocation center is indicated by the red symbol. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

predictions do not converge as closely as GAP to the DFT predictions by increasing the number of basis functions.

The energy to move a dislocation grows proportionally to the length of the dislocation line, which leads to a large barrier to move a long screw dislocation (~ 1 eV for $20b$). Long-standing theory envisions that the actual glide mechanism of screw dislocations occurs via kink-pair

nucleation and migration, which is a thermally activated process [1, 62]. Here, we compute the kink-formation energy by using CI-NEB method with a long screw dislocation geometry ($40b$ along y), which allows the kink-pair formation and propagation process instead of straight gliding. The energy barrier associated with kink-pair nucleation is indicated by the plateau of the energy profile in Fig. 6c (~ 1 eV),

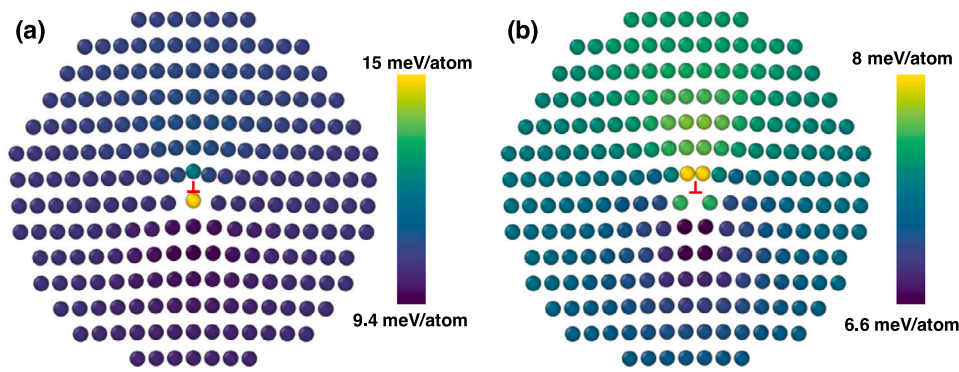


Fig. 8. Core structure of $a_0[100](011)$ edge dislocation predicted by GAP-DB-I: (a) $R_{\text{cut}} = 6.5 \text{ \AA}$, and (b) $R_{\text{cut}} = 5 \text{ \AA}$. The two core structures are referred to as atom-centered (AC) and bond-centered (BC) structures, respectively. The dislocation center is indicated by the red symbol “ \perp ”. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

which is in line with Ref. [34]. The kink can easily propagate once it is formed, since the Peierls barrier for $\{110\}(111)$ edge dislocation glide is tiny (Fig. 9c). The core structures in Fig. 6b are colored according to the GAP-DB-I model uncertainty, evidencing that the model uncertainty is converged to less than 10 meV/atom during the kink-formation process.

Overall, the analysis shows that the GAP and PACE-FS potentials agree with published DFT and predict glide with limited uncertainty. PACE-FS needs training on more dislocation path-specific data in order to capture the precise hierarchy of dislocation core structures, especially the hard-to-split transition path.

4.2. Core structures and energy barriers of edge and M111 dislocations

Fig. 7 shows the core structures of three edge dislocations and the M111 dislocation, predicted by GAP-DB-I using the RB configuration (see *Supplementary Material S4.1.1* for the predictions of GAP-DB-II and PACE-FS). The atoms are colored according to the difference between the ML-IAP and the DFT atomic positions, using DFT data from [58] as a reference, and indicate quantitative agreement with DFT. All ML-IAPs are able to predict the DFT core structures except for PACE-FS, which predicts another structure for the $a_0[100](011)$ edge dislocation core [58] (Fig. S17b). $a_0[100](010)$, $a_0/2[\bar{1}\bar{1}1](1\bar{1}0)$ and M111 show errors that are lower than 0.1 \AA (Figs. 7a and 7c). The error associated with $a_0[100](011)$ edge is as high as 0.15 \AA for the central atoms. Nevertheless, the predicted core structure is qualitatively the same as DFT predictions.

To explore other possible core structures, we further relax the dislocation core by breaking the symmetry of the initial geometry, i.e., by starting from a slightly asymmetric dislocation core configuration. We find that different core structures are predicted for M111 dislocation by using GAP-DB-I and for $a_0[100](011)$ edge dislocation by using GAP-DB-II (see *Supplementary Material S4.1.2*). The discrepancies between the core structures emerging from symmetric and asymmetric initial geometries indicate that multiple local minima core structures exist for these dislocations in GAP-DB-I and GAP-DB-II. Moreover, GAP-DB-I and GAP-DB-II with $R_{\text{cut}} = 5 \text{ \AA}$ are found to yield a bond-centered (BC) rather than an atom-centered (AC) structure for $a_0[100](011)$ edge dislocation, as shown in Fig. 8b. Note that the $R_{\text{cut}} = 6.5 \text{ \AA}$ has a larger baseline uncertainty because the local atomic environment is more complex compared to $R_{\text{cut}} = 5 \text{ \AA}$ due to the large cutoff radius. Atoms with the largest uncertainty tend to be located at the center of the dislocation, which is expected since the bonds around the central atom are highly distorted. The results suggest that $R_{\text{cut}} = 5 \text{ \AA}$ may not be sufficient to describe the complex energy landscape, and to distinguish between AC and BC core structures.

The PAD configuration is employed to compute the Peierls barrier, which involves a different process to create the initial dislocation configuration, as described in Ref. [56]. The PAD configuration predicts the same equilibrium dislocation core structures as the RB configuration starting from asymmetric initial geometries (see *Supplementary Material S4.1.2*). Fig. 9 shows the Peierls potential of the four dislocations, predicted by GAP-DB-I, GAP-DB-II, and PACE-FS. Peierls barrier of $a_0[100](010)$ edge dislocation ranges from 276 to 516 meV/b predicted by three ML-IAPs, indicating that dislocation is immobile. For $a_0[100](011)$ edge dislocation, two stable core structures, AC and BC, are predicted by the different ML-IAPs. GAP-DB-I predicts the transition pathway AC-BC-AC while PACE-FS predicts BC-AC-BC. The per-atom uncertainty of PACE-FS shows a signal peak along the dislocation glide path for $a_0[100](011)$ edge dislocation, suggesting that PACE-FS is extrapolating (see *Supplementary Material S4.2*). GAP-DB-II predicts a small barrier (1 meV/b) with an irregularly shaped Peierls potential, which is detected by the GAP model uncertainty (Fig. S23). This is because the relevant dislocation configuration is not present in the DFT database. The Peierls barrier of $a_0/2[\bar{1}\bar{1}1](1\bar{1}0)$ edge dislocations is negligibly small (0.055 meV/b) according to PACE-FS. NEB performed with two GAPs fail to converge because of even smaller energy barriers, as verified by Peierls stress calculations. Thus, our findings suggest that the Peierls barrier is insignificant ($<0.1 \text{ meV/b}$). Finally, the Peierls potentials of M111 dislocation exhibit low barriers (2–5 meV/b) compared with screw and $a_0[100](011)$ edge dislocations. GAP-DB-I predicts AC core as the stable structure while the other two potentials show that BC is more stable. The discrepancies among the different ML-IAPs regarding the prediction of the equilibrium core structures suggest the existence of a multi convex hull PES with similar energy minima that ML-IAPs may not be capable of discriminating.

In particular, both the RB and PAD configurations are employed to find the equilibrium dislocation core structures. The RB configuration is found to yield different core structures upon relaxing the symmetric and slightly asymmetric initial dislocation geometry. GAP-DB-I and GAP-DB-II ($R_{\text{cut}} = 6.5 \text{ \AA}$) with the RB configuration and symmetric initial geometry predict core structures consistent with DFT [58]. However, the core structures predicted by RB configurations with asymmetric initial geometry and PAD configuration are inconsistent with DFT results for $a_0[100](011)$ edge and M111 dislocations, indicating the existence of multiple local minima. The results suggest that, if the dislocation has multiple metastable core structures with similar energies, the predicted dislocation core structures can be extremely sensitive to the initial geometry and boundary conditions. Therefore, care should be taken when identifying the equilibrium dislocation core structures. Breaking the symmetry such as starting from slightly distorted geometry may help to escape from local minima.

In summary, the predictions of the edge and M111 core structures are consistent across the ML-IAPs considered here, and the per-atom

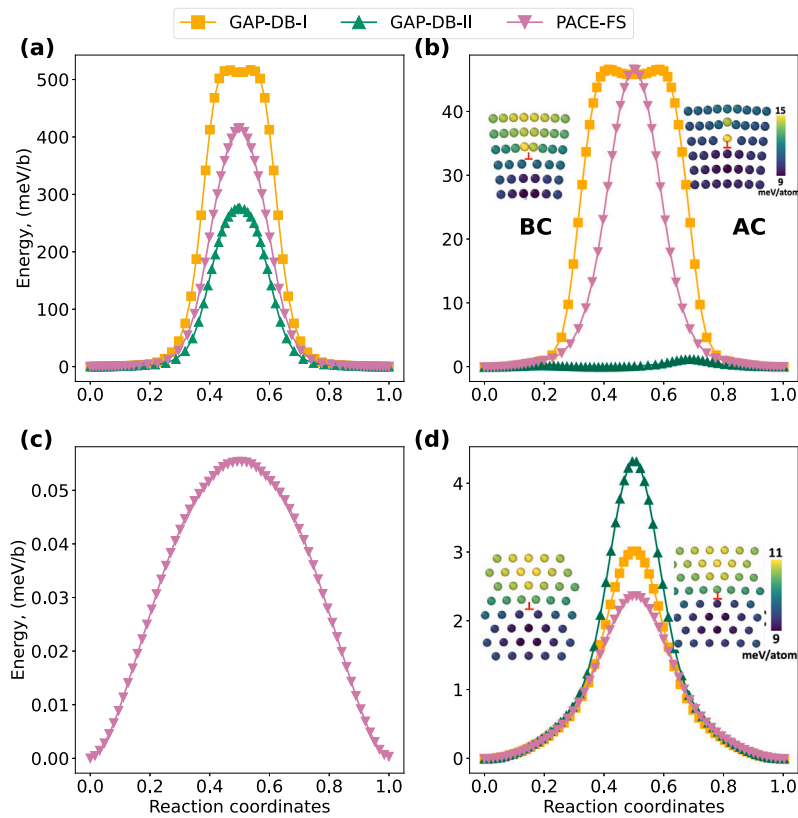


Fig. 9. Peierls potential of (a) $a_0[100](010)$, (b) $a_0[100](011)$, (c) $a_0/2[\bar{1}\bar{1}1](1\bar{1}0)$ edge dislocations, and (d) M111 dislocation. The Peierls barrier is computed using PAD configuration at $T = 0$ K under zero applied stress. The insets are colored according to the GAP model uncertainty predicted by GAP-DB-I, indicating where the largest extrapolation is located (see *Supplementary Material S4.2* for more details). The dislocation center is indicated by the red symbol. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

model uncertainty with respect to DFT is sufficiently low with only few exceptions. Where multiple core structures can occur that have small energy differences, close to DFT accuracy (~ 1 meV/atom), then the predicted minimum energy core is sensitive to the specific ML-IAP and boundary conditions. Rather than being a ML-IAP limitation, this outcome shows that ML-IAP predictions are limited by the choice of configurations that are included in the database and, possibly, by DFT accuracy itself when energy differences approach ~ 1 meV/atom.

5. Atomistic fracture

5.1. Traction–separation process

The traction–separation (T–S) curve is often used to quantify brittle fracture, since it encodes the surface energy, the cohesive strength and the rigid surface separation process. We compute the T–S curve based on the ML-IAPs trained in Section 2. The traction–separation profiles are calculated by taking the derivative of the energy–separation curve, which is obtained by rigidly separating a perfect crystal. During the calculation, a bcc iron single crystal is separated along $\{100\}$ and $\{110\}$ planes using an incremental step of 0.05 \AA .

Fig. 10 shows the T–S curves predicted by ML-IAPs with $R_{\text{cut}} = 6.5 \text{ \AA}$. DFT predicts a smooth curve with a single maximum traction (the so-called cohesive strength). All ML-IAPs (including MTP, NNP and PACE-L, see *Supplementary Materials S5.1.1*) are able to predict a distinct maximum normal stress, yet, all T–S curves show multiple artificial local minima after reaching the cohesive strength, especially at the end of the separation process. Among all potentials, GAP-DB-I and PACE-FS yield the closest predictions compared to DFT. The GAP-DB-I predicted T–S curve is smoother than GAP-DB-II since DB-I includes the surface separation process (the solid circle DFT data in

Fig. 10). In all cases, the area under the curve is calculated and is equal to twice the surface energy, as expected (see *Supplementary Materials S5.1.2*).

Since ML potentials are constructed based on the energy localization assumption, the choice of the maximum interaction range (R_{cut}) might have consequences on the T–S curve. Therefore, we train two sets of PACE-FS potentials (see *Supplementary Material S5.1.3 and S5.1.4*). The first set is trained with cutoff ranges from 5 to 7 \AA to investigate the influence of R_{cut} . The results show that $R_{\text{cut}} = 6.5 \text{ \AA}$ has the minimal “tail” non-smoothness effects while capturing the cohesive strength among all R_{cut} (Fig. S28). Yet, the potentials are able to capture the essential behavior (single-peak, skewed shape) of the T–S curve with the proper choice of R_{cut} . Note that all ML-IAPs are only trained with limited surface separation data (solid circles in **Figs. 10a** and **10b**). Therefore, the second set is trained by adding four times more separation configurations to the training database (see the computed T–S curves in Fig. S29). The results show that the end of the separation is still not smooth, indicating that the oscillation is not primarily caused by the lack of training data. The many-body interactions nature of ML-IAPs introduces a complex energy landscape, which might induce multiple artificial local minima. Such oscillations posit an open question regarding their origin, which might be associated to a poor regularization of the ML-IAPs. Attention is thus required when analyzing the T–S curves with ML-IAPs. Nonetheless, the T–S curve is obtained from rigid separation while the surface is under relaxation during fracture simulation. Especially after the cohesive strength, the crystal separates physically with a displacement jump. Therefore, the end of the T–S is not physically relevant to the fracture behavior. We conclude that the oscillations at the tail of the T–S curves have a minor influence on the fracture prediction, as discussed in the next Section.

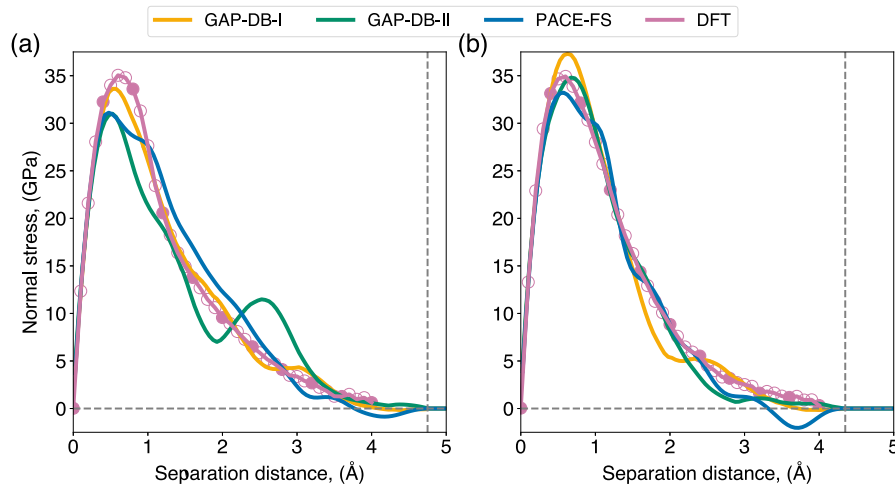


Fig. 10. Traction–separation curves predicted by ML-IAPs and DFT in bcc iron for (a) {100} and (b) {110} plane. The solid circles indicate the DFT data used in the training database (DB-I). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

5.2. Atomistic fracture mechanism

Based on the ML-IAPs trained in Section 2, MS and MD simulations are performed to study the atomistic fracture mechanism and to predict the critical stress intensity factor (K_{Ic}) of single crystal bcc iron. A cylinder-shaped near-crack-tip geometry is used in combination with the K -test framework, as illustrated in Fig. 11a [6]. The crack is aligned with a Cartesian coordinate system, where x , y and z are the crack-propagation direction, the crack-front and the crack-plane normal, respectively. The radius of the cylinder is set to 150 Å, which enables converged predictions [16]. A displacement controlled loading procedure is implemented, whereby the boundary atoms are displaced according to the anisotropic linear elastic solution of an infinite crack subject to a remote K_I . The crack is initially loaded to K_{init} , at which the crack tip is maintained at its original position. Next, K_I is increased with a step of $\Delta K = 0.01 \text{ MPa}\sqrt{m}$ until a critical event occurs at the crack tip, i.e., either crack propagation, dislocation emission, phase transition, or the combination of multiple mechanisms. In the MS simulations, the atoms at the mobile region of the cell ($r < 140$ Å) are relaxed using a combination of CG and FIRE minimizers [59] with a force tolerance of 10^{-9} eV/Å and 10^{-3} eV/Å, respectively, while the rest of the atoms are fixed at each incremental step. For finite temperature MD simulations, the mobile region is equilibrated for 10 ps at each incremental step with the Nosé–Hoover thermostat. More details of the K -test loading procedure can be found in [16,63].

We perform K -test simulations for four crack systems at $T = 0$ K to investigate the atomistic fracture mechanism, including (100)[010], (100)[011], (110)[001], and (110)[1 $\bar{1}$ 0] (crack plane normal/crack front). Since the cutoff radius significantly influences the behavior of the traction–separation curve, all ML-IAPs are trained with two cutoff radii ($R_{cut} = 5$ Å and 6.5 Å) to study the effect of the cutoff radius. Here, we show the results of $R_{cut} = 6.5$ Å, while $R_{cut} = 5$ Å results are reported in *Supplementary Material S5.3*. The ML-IAPs trained on DB-I predict cleavage fracture on the pre-cracked plane for all crack systems, for both $R_{cut} = 5$ Å and 6.5 Å. The only exception is that GAP-DB-II with $R_{cut} = 5$ Å predicts crack deviation to the (100) plane for the (110)[001] crack system. The fundamental atomistic fracture mechanism (cleavage) remains unchanged, yet, the predicted K_{Ic} varies with the potential, as shown in Fig. 11b. Some fluctuations in the predicted K_{Ic} 's are expected because of the different ML-IAP schemes. For crack system (110)[001], we concluded in our previous study [16] that the large K_{Ic} at $T = 0$ K compared to K_G is due to the existence of a small lattice trapping barrier, which is introduced by the rough PES. Therefore, we perform MD simulations for (110)[001] at $T = 100$ K,

which allows the system to overcome the small activation energy barrier and reduce the predicted K_{Ic} . As indicated by the open triangles in Fig. 11b, K_{Ic} 's for (110)[001] drop significantly at $T = 100$ K, which is consistent with the existence of a small lattice trapping barrier. The predicted K_{Ic} 's for crack system (110)[1 $\bar{1}$ 0] are nearly the same for all potentials. All ML-IAPs with $R_{cut} = 6.5$ Å predict cleavage on the pre-cracked plane for all crack systems, confirming that the atomistic fracture mechanism is cleavage. Moreover, the per-atom model uncertainty predicted by the GAP variance and the extrapolation grade γ are consistent with each other. No large extrapolation ($\gamma > 3$, see [64]) is detected during the fracture process (see *Supplementary Material S5.2*). Fig. 11c reveals the relation between MS predicted K_{Ic} 's and the Griffith prediction [51]

$$K_G = \sqrt{\frac{2\gamma_s}{B}}, \quad (17)$$

where γ_s is the surface energy. B is a constant that is expressed as

$$B = \sqrt{\frac{b_{11}b_{22}}{2} \left(\frac{2b_{12} + b_{66}}{2b_{11}} + \sqrt{\frac{b_{22}}{b_{11}}} \right)}, \quad (18)$$

where b_{ij} are determined by the elastic constants. Since K_G only depends on surface energy and elastic constants, all ML-IAPs predict similar results, ranging from 1.025–1.15 $\text{MPa}\sqrt{m}$. K_{Ic} is always larger than K_G , indicating that all ML-IAPs predict lattice trapping effects. For {100} crack plane, (110)[1 $\bar{1}$ 0] system at $T = 0$ K and (110)[001] at $T = 100$ K, K_{Ic} and K_G show a quasi-linear correlation. This result reveals that the critical K_I is correlated with the surface energy in the presence of lattice trapping effects. Crack system (110)[001] at $T = 0$ K exhibits an artificial trapping barrier for part of the ML-IAPs, leading to the scattered distribution.

Our analysis shows that the trained ML-IAP potentials are transferable to crack propagation simulations, and predictions are qualitatively consistent. Limited quantitative differences in the predictions (K_{Ic} , lattice trapping) can be encountered based on the choice of the cutoff radius (which has been optimized here) and the ML-IAP package.

6. Discussion

6.1. Complementing accuracy analysis with transferability assessment via model uncertainty quantification

We have proposed a three-step procedure to achieve DFT accuracy, optimize the efficiency, and verify the transferability of ML-IAPs. This procedure includes extensive use of training/testing RMSE, quality

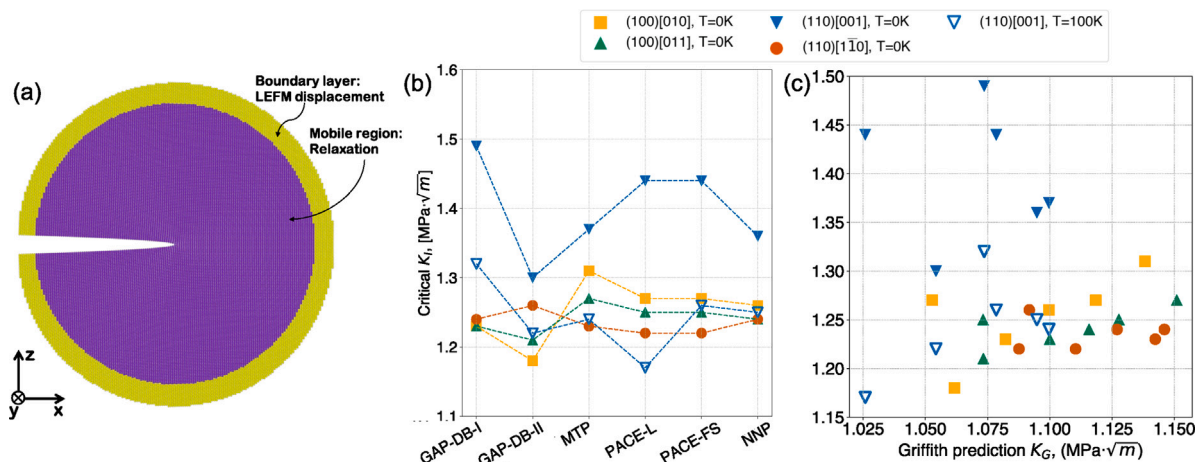


Fig. 11. (a) Schematic plot of K -test fracture simulation setup. x , y and z are aligned with the crack propagation direction, crack plane normal and crack front, respectively. (b) Critical K_{Ic} predicted by different ML-IAPs at $T = 0\text{K}$ for four crack systems and $T = 100\text{K}$ for (110)[010] crack system. Crack systems are indicated by crack plane/crack front. (c) Critical K_{Ic} predicted by ML-IAPs versus Griffith criterion K_G .

factor evaluation, and model uncertainty quantification. As a matter of fact, the RMSE and quality factor are commonly used during the validation of ML-IAPs [22,28,33]. However, instead of using an average quality factor/score, the existing literature compares the individual properties directly to DFT, e.g. by looking at the equation of state, the elastic constants, the surface energies, the vacancy formation and migration energies, and the GSFE curves [22,23]. Here, we use an aggregate index Q that is defined in Eq. (16) as the relative root-mean-square-error of the predicted physical properties. The relation between RMSE and Q reveals the existence of an RMSE limit ($\sim 6\text{ meV/atom}$) under which lower RMSE does not correspond to smaller Q (Fig. 4), which underlines the limitation of using RMSE as the only accuracy measure. Therefore, an optimum between accuracy and efficiency can be found by selecting potentials with RMSE around 6 meV/atom , and we propose to use model uncertainty quantification in the context of benchmark simulations of extended defects to further assess the ML-IAP transferability.

In this work, we have calculated and demonstrated the usage of two different model uncertainty quantification measures to validate the transferability of the ML-IAPs to dislocation and cracks. These two measures are correlated to each other, in the sense that they identify consistently the highest uncertainty in the same atomistic regions (see *Supplementary Material S4.2.2 and S5.2*). The properties of screw dislocations in bcc metals, i.e., compact core structure, Peierls barrier, and kink-pair nucleation/migration, are considered to be essential aspects that ML-IAPs should be able to capture [12–15,24,28,30], and they cannot be computed directly with DFT supercells. Here, we have shown that the GAP variance and extrapolation grade γ from PACE-FS indicate interpolation for screw dislocation glide, including Peierls barrier and kink pair nucleation. Furthermore, K -tests have been performed to investigate the atomistic fracture mechanisms of single crystal bcc iron, whereby the model uncertainty is converged within the threshold. We highlight that, when applying the ML-IAP for large-scale MD simulations, the extrapolation degree (i.e., predicted variance for GAP and extrapolation grade γ for ACE) should be monitored to further verify the transferability of the potential and the reliability of the simulations.

6.2. The choice of the DFT database

Generating a database is the most time-consuming part of training ML-IAPs, since quantum mechanical calculations (typically DFT) are computationally expensive. The conventional way is to create a general database that contains equilibrium and perturbed configurations of possible phases and various defects (surface, point defects, lattice

expansion/compression, isolated clusters, grain boundaries *etc.*) [13,65,66]. The perturbed configurations can be generated either by random rattling of atomic displacements or by finite-temperature MD using some preliminary version of the potential. For specific applications, user experience is still needed to design the database that consists of relevant configurations. However, any hand-built database is user-biased and sometimes redundant. To reduce both human intervention and usage of computational resources, (hyper)active learning (combined with model uncertainty quantification) is being developed and applied to different ML frameworks, which enables fast creation of the database [41,43,67,68].

As detailed in Section 2.1, DB-I was initially constructed in a conventional manner and subsequently extended with an active-learned fracture-relevant database, where small crack-tip configurations were added based on GAP variance predictions [13,16]. DB-II has been designed with an attempt to cover *a priori* all possible defects, leading to a 5 times larger number of LAEs compared with DB-I. DB-I contains no dislocation structures while DB-II includes $a_0/2(111)$ screw dislocation and edge dislocations. Yet, GAPS trained on either DBs can predict DFT-accurate Peierls barrier and kink pair nucleation barrier of screw dislocations, as well as core structures of edge and M111 dislocations. This finding is consistent with previous work, where an ANN potential was shown to accurately predict the dislocation core structure and Peierls barrier, despite being trained on a DFT database without any dislocation structures [28]. This suggests that the γ -surface is enough for the prediction of the compact core structure and single hump Peierls barrier for screw dislocation [33,34], a result that is consistent with earlier analysis by Duesbery and Vitek [69], where authors show that correct reproduction of the γ -surface gives correct core structure. It has been shown in Ref. [12,24] that direct inclusion of dislocation core configurations in the database can lead to a better accuracy in predicting the core structure. A detailed study, i.e., training and testing ML-IAPs with different sub-databases, would be required to quantitatively examine the influence of directly including the relevant configurations.

GAP-DB-II predicts cleavage on the pre-cracked plane to be the atomistic fracture mechanism on {100} and {110} planes, which is consistent with the prediction of GAP-DB-I. However, DB-I encompasses several crack-tip configurations that are obtained through active learning while DB-II does not include any crack-tip configurations [16]. This result suggests that an extensive but also less redundant DFT database can be obtained via specific design and active learning, which is a key implication for researchers interested in developing, using and/or adapting ML potentials. The comparison of two databases suggests that

Table 2
Peierls barrier and double kink-pair formation energy predicted by DFT, line tension (LT) model, and different ML-IAPs.

Potential	Peierls barrier (meV/b)	Kink-pair formation (eV)
DFT [4,13,60,71]	35–58	–
line-tension (LT) models [2,3]	–	0.73–0.91
ANN (<i>aenet</i>) [28]	35.3	0.94
NNP (<i>n2p2</i>) [33]	38.2	0.70
MTP [29]	30.5	–
LML [30]	41.9	0.77
QNML [30]	38.2	0.84
GAP-DB-I	52.3	1.02
GAP-DB-II	53.6	1.03
PACE-FS	58.5	1.04

inherent liquid state structures or grain boundaries included in DB-II may play an important role when predicting fracture. A separate study would be needed to identify the extra data that enables the fracture prediction without direct inclusion of the crack tips, which is beyond the scope of the present work.

6.3. Variability in the predictions of dislocation core structures and Peierls barriers

Thermally activated $a_0/2\langle 111 \rangle$ screw dislocation controls the low-temperature plasticity (brittle–ductile transition) of bcc metals. Most of the classical potentials fail to predict a compact core structure and a single hump Peierls potential [70]. Therefore, the core structure and Peierls barrier of screw dislocations are first benchmarked for bcc ML-IAPs [12,13,15,30]. In this work, we have shown that all ML-IAPs are able to predict a compact screw dislocation core structure for bcc iron. Peierls barrier calculated via NEB approach shows a single hump, ranging from 48 to 58 meV/b. DFT calculations which are consistent with DB-I predict a Peierls barrier between 48 and 58 meV/b [13]. Based on the same DFT database, original NNP (DB-II) predicts a smaller Peierls barrier than GAP-DB-II. Moreover, the NNP trained on DB-I predicts Peierls barrier of 41.99 meV/b, which is smaller than both GAP-DB-I and PACE-FS (see Fig. S15 of the Supplementary Material S3.4). This suggests that NNP tends to underestimate the DFT data of screw dislocation glide, as further discussed in Fig. S13 of the Supplementary Material S3.3. We showed that GAP-DB-II predicts a Peierls barrier in this same range, and it converges to DFT data of DB-II which include configurations that are relevant to the Peierls path. Using the same geometry, other independent DFT calculations predict a Peierls energy barrier of 40 ± 5 meV/b based on a plane wave approach [4]. Such discrepancies are introduced by the model geometry and DFT calculation details, e.g., code, convergence setup, exchange–correlation function, and pseudopotential. Therefore, the Peierls barrier of screw dislocation ranges from 35 to 58 meV/b according to different DFT calculations [4,13,60]. Table 2 lists the Peierls barrier and double kink formation energy predicted by DFT and ML-IAPs, including two NNPs [28,33], an MTP [29], a LML model, and a QNML Potential [30]. From Table 2, all available ML-IAPs are able to quantitatively predict the Peierls barrier and kink-pair mechanism irrespective of the ML approach and DFT database, which makes ML-IAPs suitable candidates for studying screw dislocation behavior. Furthermore, the energy profiles along the cross section of hard to split core path predicted by GAP-DB-I and GAP-DB-II show the correct energy hierarchy, i.e., the energy of split core is larger than hard core, while PACE-FS can be improved to predict the correct energy hierarchy by training on DB-II.

The core structure of edge ($a_0[100](010)$, $a_0[100](011)$, and $a_0/2[\bar{1}\bar{1}1](1\bar{1}0)$) and M111 dislocations have also been used to benchmark the predictability of the ML-IAPs [28,29,58]. For example, it is shown that NNP and an MTP are capable of reproducing these dislocation core structures with DFT accuracy [28,29]. In the current study, both RB and PAD configurations have been employed to reveal

the dislocation core structures and Peierls barriers. We have shown that GAP-DB-I and GAP-DB-II along with the RB configuration are able to reproduce DFT-predicted core structures for all dislocations. Discrepancies are found between different initial geometries, which is the results of multiple metastable core structures with similar energies. Indeed, DFT calculations with flexible boundary conditions predict BC core for M111 [58]. However, a different DFT calculation [72] with a rectangular arrangement of cells shows that the energy difference between AC and BC core is essentially zero, indicating that M111 dislocation in bcc iron has no clear core preference. Since the energy difference between AC and BC core structures is so small that it cannot be captured reliably by small-cell DFT calculations, it is not surprising that ML-IAPs yield different results.

As for edge dislocations, our NEB results show that the Peierls barrier of $a_0[100](010)$ is larger than 260 meV/b, for all ML-IAPs, which is consistent with earlier findings in tungsten [73]. For the $a_0[100](011)$ dislocation, PACE-FS shows an inverted migration path compared with GAP, which may be caused by incorrect extrapolations as suggested by the uncertainty index γ . The Peierls barriers of $a_0/2[\bar{1}\bar{1}1](1\bar{1}0)$ shows a negligible activation barrier that can be easily overcome by mild thermal fluctuations, consistent with the notion that edge dislocations in bcc iron move without thermal activation. Previous calculations of $a_0/2[\bar{1}\bar{1}1](1\bar{1}0)$ edge dislocation based on three EAM potentials also predict Peierls barrier of 0.1–2 meV/b [74]. However, in the same study, another EAM potential (Chiesa09 [75]) predicts a Peierls barrier of 9 meV/b, which is expected to be an artifact of the potential [74]. Such inconsistent outcomes of EAM potentials again highlight the need of accurate IAPs that are capable of providing consistent predictions.

It has been shown that M111 dislocations can play a role in dislocation mobility at low temperature for bcc Ta [54]. Here, our NEB calculations predict a negligible Peierls barrier (2–5 meV/b) under zero applied stress at $T = 0$ K, which is consistent with recent DFT calculations [72]. The DFT calculations show that M111 dislocation in bcc iron has a negligible energy difference between AC and BC core structures [72]. Therefore, M111 dislocation in bcc iron is expected to move without thermal activation/kink-pair nucleation and propagation, which indicates that its contribution to low-temperature plasticity is negligible.

6.4. Challenges associated with the prediction of the traction–separation law

We have shown that the influence of R_{cut} on the traction–separation profile is significant, i.e., the inappropriate R_{cut} introduces multiple peak stress and fluctuations at the end of the separation process. Ideally, a larger cutoff radius is able to contain more information about the LAE, which in principle yields more accurate predictions, at increased computational cost. In practice, the cutoff radius should be chosen to reproduce the elementary properties shown in Section 3 while keeping R_{cut} as small as possible. As also pointed out in Ref. [76], unrealistic stresses are predicted at the end of the separation process based on MEAM potential, which can be addressed by increasing the R_{cut} . Hiremath et al. also fitted MEAM to predict a smooth T–S curve by optimizing the cutoff and smoothing ranges [77]. Another study on bcc vanadium shows that an extended MEAM potential is able to predict a smooth T–S curve without small fluctuations [15]. On the contrary, predictions of GAP exhibit an artificial peak stress at the end of decohesion, which is not observed here. In the same study, a deep NN potential is also employed, which predicts the T–S curve with fluctuations [15]. It is argued here that the T–S curve cannot be entirely captured by ML-IAPs because of the complex energy landscape introduced by many-body interactions and the regularization of the potential, which underlines an open challenge for ML-framework developers. We emphasize that ML-IAPs demonstrate advantages in general-purpose applications; however, these advantages are constrained by the quality of the database and the effectiveness of the ML algorithms.

7. Conclusions

In this study, we have trained and benchmarked several ML-IAPs based on two independent large DFT databases. High accuracy with respect to the training database has been achieved by extensive hyperparameter optimization. The computational cost has been assessed and the optimal potentials in terms of computational speed (PACE-FS) and accuracy (GAP) have been identified. These potentials have been successfully tested on a broad number of benchmark simulations including screw, mixed M111 and several edge dislocations; as well as the challenging crack propagation. By making extensive use of model uncertainty quantification and direct comparison with consistent DFT calculations, we have shown that the optimized ML-IAPs are capable of reproducing a broad range of properties with DFT accuracy, including the structure and Peierls barriers of five dislocation characters, the traction–separation law and crack propagation behavior of bcc iron. The following salient conclusions can be drawn:

1. The three-step validation procedure adopted in this work enables the assessment of the accuracy and transferability of several state-of-the-art ML IAPs to model dislocations and cracks. The procedure has been applied to the case of bcc iron. By optimizing the model parameters and considering different ML packages, the ML-IAPs efficiency can be increased by two orders of magnitude in terms of computational time. We find that GAP occupies the Pareto front in terms of accuracy, while PACE-FS is the most efficient ML-IAP.
2. Depending on the specific application, MS/MD simulations beyond DFT supercell size need to be employed to validate the transferability of ML-IAPs (e.g., dislocations and cracks). This assessment has been performed by using model uncertainty quantification, which is implemented in the state-of-the-art ML-IAP packages and requires limited computing time.
3. Both GAP and PACE-FS are capable of reproducing the key features of screw dislocations in bcc iron (Peierls barrier and kink-pair nucleation), which is a necessary condition for large-scale plasticity simulations of bcc crystals. With both databases, GAP can reproduce the details of the screw dislocation migration path including the correct energetic hierarchy of the dislocation cores (easy, hard and split). The PACE-FS ML-IAP optimized in this manuscript can also reproduce this hierarchy, if DFT data relevant to the hard-to-split migration path are included in the training database.
4. M111 dislocation cores show multiple structures that have a similar energy, which is further verified by NEB calculations. The predicted minimum energy structures can differ depending on the ML-IAP (GAP or PACE-FS) and the training database. This finding shows that, when the energy difference of two core configurations is close to DFT accuracy, ML-IAPs cannot discriminate between the two configurations. We also find that M111 dislocation, which is shown to be the second immobile dislocation character at low temperature in bcc Ta, has negligible Peierls barrier in bcc iron.
5. All the ML-IAPs trained in this work and two independent databases confirm that the atomistic fracture mechanisms in bcc iron at $T=0$ K under mode-I loading is cleavage on the pre-cracked plane, irrespective of the crack front.
6. GAP-DB-I predicts screw dislocation and fracture properties that are in good agreement with GAP-DB-II yet using only 1/5 of the data, showing that the same accuracy and transferability can be achieved by training the ML-IAP to a much smaller database. This finding is important since the DFT database construction involves the most part of the ML-IAP training time. Thus, DFT computational resources can be reduced significantly by careful design of the training database and by using active learning techniques.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

The training scripts and potentials are available on the Github page https://github.com/leiapple/ML-IAPs_iron. The physical properties benchmarking workflow and the LAMMPS script for dislocations are available at https://github.com/leiapple/Potential_benchmark_iron.

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Appendix A. Supplementary data

Supplementary material related to this article can be found online at <https://doi.org/10.1016/j.actamat.2024.119788>.

References

- [1] J.E. Dorn, S. Rajnak, Nucleation of kink pairs and the peierls' mechanism of plastic deformation, *Trans. Metall. Soc. AIME* 230 (1963) 1052–1064.
- [2] L. Proville, L. Ventelon, D. Rodney, Prediction of the kink-pair formation enthalpy on screw dislocations in α -iron by a line tension model parametrized on empirical potentials and first-principles calculations, *Phys. Rev. B* 87 (14) (2013) 144106, <http://dx.doi.org/10.1103/PhysRevB.87.144106>.
- [3] M. Itakura, H. Kaburaki, M. Yamaguchi, First-principles study on the mobility of screw dislocations in BCC iron, *Acta Mater.* 60 (9) (2012) 3698–3710, <http://dx.doi.org/10.1016/j.actamat.2012.03.033>.
- [4] L. Ventelon, F. Willaime, E. Clouet, D. Rodney, Ab initio investigation of the peierls potential of screw dislocations in BCC Fe and W, *Acta Mater.* 61 (11) (2013) 3973–3985, <http://dx.doi.org/10.1016/j.actamat.2013.03.012>.
- [5] E. Mak, B. Yin, W. Curtin, A ductility criterion for BCC high entropy alloys, *J. Mech. Phys. Solids* 152 (2021) 104389, <http://dx.doi.org/10.1016/j.jmps.2021.104389>.
- [6] P. Andric, W. Curtin, New theory for Mode I crack-tip dislocation emission, *J. Mech. Phys. Solids* 106 (2017) 315–337, <http://dx.doi.org/10.1016/j.jmps.2017.06.006>.
- [7] J. Song, W. Curtin, Atomic mechanism and prediction of hydrogen embrittlement in iron, *Nature Mater.* 12 (2) (2013) 145–151, <http://dx.doi.org/10.1038/nmat3479>.
- [8] D. Scheiber, K. Prabit, L. Romaner, W. Ecker, The influence of alloying on Zn liquid metal embrittlement in steels, *Acta Mater.* 195 (2020) 750–760, <http://dx.doi.org/10.1016/j.actamat.2020.06.001>.
- [9] M. Mendeleev, S. Han, D. Srolovitz, G. Ackland, D. Sun, M. Asta, Development of new interatomic potentials appropriate for crystalline and liquid iron, *Phil. Mag.* 83 (35) (2003) 3977–3994, <http://dx.doi.org/10.1080/14786430310001613264>.
- [10] P. Gordon, T. Neeraj, M. Mendeleev, Screw dislocation mobility in BCC metals: a refined potential description for α -Fe, *Phil. Mag.* 91 (30) (2011) 3931–3945, <http://dx.doi.org/10.1080/14786435.2011.597947>.
- [11] J.J. Möller, E. Bitzek, On the influence of crack front curvature on the fracture behavior of nanoscale cracks, *Eng. Fract. Mech.* 150 (2015) 197–208, <http://dx.doi.org/10.1016/j.engfracmech.2015.03.028>.
- [12] W.J. Szlachta, A.P. Bartók, G. Csányi, Accuracy and transferability of Gaussian approximation potential models for tungsten, *Phys. Rev. B* 90 (10) (2014) 104108, <http://dx.doi.org/10.1103/PhysRevB.90.104108>.
- [13] D. Dragoni, T.D. Daff, G. Csányi, N. Marzari, Achieving DFT accuracy with a machine-learning interatomic potential: Thermomechanics and defects in BCC ferromagnetic iron, *Phys. Rev. Mater.* 2 (2018) 013808, <http://dx.doi.org/10.1103/PhysRevMaterials.2.013808>.
- [14] M. Alam, L. Lymparakis, Artificial neural network interatomic potential for dislocation and fracture properties of molybdenum, 2021, [arXiv:2112.04636](https://arxiv.org/abs/2112.04636).

- [15] R. Wang, X. Ma, L. Zhang, H. Wang, D.J. Srolovitz, T. Wen, Z. Wu, Classical and machine learning interatomic potentials for BCC vanadium, *Phys. Rev. Mater.* 6 (11) (2022) 113603, <http://dx.doi.org/10.1103/PhysRevMaterials.6.113603>.
- [16] L. Zhang, G. Csányi, E. Van Der Giessen, F. Maresca, Atomistic fracture in BCC iron revealed by active learning of gaussian approximation potential, *npj Comp. Mater.* 9 (1) (2023) 217, <http://dx.doi.org/10.1038/s41524-023-01174-6>.
- [17] J. Behler, M. Parrinello, Generalized neural-network representation of high-dimensional potential-energy surfaces, *Phys. Rev. Lett.* 98 (14) (2007) 146401, <http://dx.doi.org/10.1103/PhysRevLett.98.146401>.
- [18] A.P. Bartók, M.C. Payne, R. Kondor, G. Csányi, Gaussian approximation potentials: the accuracy of quantum mechanics, without the electrons, *Phys. Rev. Lett.* 104 (13) (2010) 136403, <http://dx.doi.org/10.1103/PhysRevLett.104.136403>.
- [19] A.V. Shapeev, Moment tensor potentials: a class of systematically improvable interatomic potentials, *Multi. Model. Simul.* 14 (3) (2016) 1153–1173, <http://dx.doi.org/10.1137/15M1054183>.
- [20] N. Artrith, A. Urban, An implementation of artificial neural-network potentials for atomistic materials simulations: Performance for TiO₂, *Comput. Mater. Sci.* 114 (2016) 135–150, <http://dx.doi.org/10.1016/j.commatsci.2015.11.047>.
- [21] R. Drautz, Atomic cluster expansion for accurate and transferable interatomic potentials, *Phys. Rev. B* 99 (1) (2019) 014104, <http://dx.doi.org/10.1103/PhysRevB.99.014104>.
- [22] Y. Zuo, C. Chen, X. Li, Z. Deng, Y. Chen, J. Behler, G. Csányi, A.V. Shapeev, A.P. Thompson, M.A. Wood, et al., Performance and cost assessment of machine learning interatomic potentials, *J. Phys. Chem. A* 124 (4) (2020) 731–745, <http://dx.doi.org/10.1021/acs.jpca.9b08723>.
- [23] Y. Lyosogorskiy, C.v.d. Oord, A. Bochkarev, S. Menon, M. Rinaldi, T. Hammer-schmidt, M. Mrovec, A. Thompson, G. Csányi, C. Ortner, et al., Performant implementation of the atomic cluster expansion (PACE) and application to copper and silicon, *npj Comp. Mater.* 7 (1) (2021) 1–12, <http://dx.doi.org/10.1038/s41524-021-00559-9>.
- [24] R. Freitas, Y. Cao, Machine-learning potentials for crystal defects, *MRS Commun.* (2022) 1–11, <http://dx.doi.org/10.1557/s43579-022-00221-5>.
- [25] Y.-S. Lin, G.P.P. Pun, Y. Mishin, Development of a physically-informed neural network interatomic potential for tantalum, *Comput. Mater. Sci.* 205 (2022) 111180, <http://dx.doi.org/10.1016/j.commatsci.2021.111180>.
- [26] A.P. Bartók, J. Kermode, N. Bernstein, G. Csányi, Machine learning a general-purpose interatomic potential for silicon, *Phys. Rev. X* 8 (4) (2018) 041048, <http://dx.doi.org/10.1103/PhysRevX.8.041048>.
- [27] T. Nishiyama, A. Seko, I. Tanaka, Application of machine learning potentials to predict grain boundary properties in fcc elemental metals, *Phys. Rev. Mater.* 4 (12) (2020) 123607, <http://dx.doi.org/10.1103/PhysRevMaterials.4.123607>.
- [28] H. Mori, T. Ozaki, Neural network atomic potential to investigate the dislocation dynamics in BCC iron, *Phys. Rev. Mater.* 4 (4) (2020) 040601, <http://dx.doi.org/10.1103/PhysRevMaterials.4.040601>.
- [29] Y. Wang, J. Liu, J. Li, J. Mei, Z. Li, W. Lai, F. Xue, Machine-learning interatomic potential for radiation damage effects in BCC-iron, *Comput. Mater. Sci.* 202 (2022) 110960, <http://dx.doi.org/10.1016/j.commatsci.2021.110960>.
- [30] A.M. Goryaeva, J. Dérès, C. Lapointe, P. Grigorev, T.D. Swinburne, J.R. Kermode, L. Ventelon, J. Baima, M.-C. Marinica, Efficient and transferable machine learning potentials for the simulation of crystal defects in BCC Fe and W, *Phys. Rev. Mater.* 5 (10) (2021) 103803, <http://dx.doi.org/10.1103/PhysRevMaterials.5.103803>.
- [31] M. Hodapp, A. Shapeev, In operando active learning of interatomic interaction during large-scale simulations, *Mach. Learn. Sci. Technol.* 1 (4) (2020) 045005, <http://dx.doi.org/10.1088/2632-2153/aba373>.
- [32] G. Henkelman, B.P. Uberuaga, H. Jónsson, A climbing image nudged elastic band method for finding saddle points and minimum energy paths, *J. Chem. Phys.* 113 (22) (2000) 9901–9904, <http://dx.doi.org/10.1063/1.1329672>.
- [33] F.-S. Meng, J.-P. Du, S. Shinzato, H. Mori, P. Yu, K. Matsubara, N. Ishikawa, S. Ogata, General-purpose neural network interatomic potential for the α -iron and hydrogen binary system: Toward atomic-scale understanding of hydrogen embrittlement, *Phys. Rev. Mater.* 5 (11) (2021) 113606, <http://dx.doi.org/10.1103/PhysRevMaterials.5.113606>.
- [34] F. Maresca, D. Dragoni, G. Csányi, N. Marzari, W.A. Curtin, Screw dislocation structure and mobility in body centered cubic Fe predicted by a Gaussian Approximation Potential, *npj Comp. Mater.* 4 (1) (2018) 1–7, <http://dx.doi.org/10.1038/s41524-018-0125-4>.
- [35] G. Csányi, S. Winfield, J.R. Kermode, A. De Vita, A. Comisso, N. Bernstein, M.C. Payne, Expressive programming for computational physics in fortran 95+, *IoP Comput. Phys. Newsl.* (2007) Spring 2007.
- [36] J.R. Kermode, f90wrap : an automated tool for constructing deep Python interfaces to modern fortran codes, *J. Condens. Matter Phys.* (2020) <http://dx.doi.org/10.1088/1361-648X/ab82d2>.
- [37] A.P. Bartók, R. Kondor, G. Csányi, On representing chemical environments, *Phys. Rev. B* 87 (18) (2013) 184115, <http://dx.doi.org/10.1103/PhysRevB.87.184115>.
- [38] M.A. Caro, Optimizing many-body atomic descriptors for enhanced computational performance of machine learning based interatomic potentials, *Phys. Rev. B* 100 (2019) 024112, <http://dx.doi.org/10.1103/PhysRevB.100.024112>.
- [39] P. Rowe, V.L. Deringer, P. Gasparotto, G. Csányi, A. Michaelides, An accurate and transferable machine learning potential for carbon, *J. Chem. Phys.* 153 (3) (2020) 034702, <http://dx.doi.org/10.1063/5.0005084>.
- [40] R. Drautz, Atomic cluster expansion of scalar, vectorial, and tensorial properties including magnetism and charge transfer, *Phys. Rev. B* 102 (2) (2020) 024104, <http://dx.doi.org/10.1103/PhysRevB.102.024104>.
- [41] A. Bochkarev, Y. Lyosogorskiy, S. Menon, M. Qamar, M. Mrovec, R. Drautz, Efficient parametrization of the atomic cluster expansion, *Phys. Rev. Mater.* 6 (1) (2022) 013804, <http://dx.doi.org/10.1103/PhysRevMaterials.6.013804>.
- [42] K. Gubaev, E.V. Podryabinkin, G.L. Hart, A.V. Shapeev, Accelerating high-throughput searches for new alloys with active learning of interatomic potentials, *Comput. Mater. Sci.* 156 (2019) 148–156, <http://dx.doi.org/10.1016/j.commatsci.2018.09.031>.
- [43] I.S. Novikov, K. Gubaev, E.V. Podryabinkin, A.V. Shapeev, The MLIP package: moment tensor potentials with MPI and active learning, *Mach. Learn. Sci. Technol.* 2 (2) (2020) 025002, <http://dx.doi.org/10.1088/2632-2153/abc9fe>.
- [44] T. Morawietz, A. Singraber, C. Dellago, J. Behler, How van der Waals interactions determine the unique properties of water, *Proc. Natl. Acad. Sci.* 113 (30) (2016) 8368–8373, <http://dx.doi.org/10.1073/pnas.1602375111>.
- [45] A. Singraber, T. Morawietz, J. Behler, C. Dellago, Parallel multistream training of high-dimensional neural network potentials, *J. Chem. Theory Comput.* 15 (5) (2019) 3075–3092, <http://dx.doi.org/10.1021/acs.jctc.8b01092>.
- [46] J. Behler, Atom-centered symmetry functions for constructing high-dimensional neural network potentials, *J. Chem. Phys.* 134 (7) (2011) 074106, <http://dx.doi.org/10.1063/1.3553717>.
- [47] R. Jinnouchi, J. Lahnsteiner, F. Karsai, G. Kresse, M. Bokdam, Phase transitions of hybrid perovskites simulated by machine-learning force fields trained on the fly with Bayesian inference, *Phys. Rev. Lett.* 122 (2019) 225701, <http://dx.doi.org/10.1103/PhysRevLett.122.225701>.
- [48] R. Jinnouchi, K. Miwa, F. Karsai, G. Kresse, R. Asahi, On-the-fly active learning of interatomic potentials for large-scale atomistic simulations, *J. Phys. Chem. C Lett.* 11 (17) (2020) 6946–6955, <http://dx.doi.org/10.1021/acs.jpclett.0c01061>.
- [49] Y. Lyosogorskiy, A. Bochkarev, M. Mrovec, R. Drautz, Active learning strategies for atomic cluster expansion models, *Phys. Rev. Mater.* 7 (4) (2023) 043801, <http://dx.doi.org/10.1103/PhysRevMaterials.7.043801>.
- [50] J.P. Hirth, J. Lothe, T. Mura, Theory of dislocations, *J. Appl. Mech.* 50 (2) (1983) 476–477, <http://dx.doi.org/10.1115/1.3167075>.
- [51] A.A. Griffith, The phenomena of rupture and flow in solids, *Philos. Trans. Royal Soc. A* 221 (1921) 163–198, <http://dx.doi.org/10.1098/rsta.1921.0006>.
- [52] J.R. Rice, Dislocation nucleation from a crack tip: An analysis based on the peierls concept, *J. Mech. Phys. Solids* 40 (2) (1992) 239–271, [http://dx.doi.org/10.1016/S0022-5096\(05\)80012-2](http://dx.doi.org/10.1016/S0022-5096(05)80012-2).
- [53] S. Plimpton, Fast parallel algorithms for short-range molecular dynamics, *J. Comput. Phys.* 117 (1) (1995) 1–19, <http://dx.doi.org/10.1006/jcph.1995.1039>.
- [54] K. Kang, V.V. Bulatov, W. Cai, Singular orientations and faceted motion of dislocations in body-centered cubic crystals, *Proc. Natl. Acad. Sci.* 109 (38) (2012) 15174–15178, <http://dx.doi.org/10.1073/pnas.1206079109>.
- [55] N. Bertin, W. Cai, S. Aubry, A. Arsenlis, V.V. Bulatov, Enhanced mobility of dislocation network nodes and its effect on dislocation multiplication and strain hardening, 2022, [arXiv:2210.14343](https://arxiv.org/abs/2210.14343).
- [56] D. Bacon, Y. Osetsky, D. Rodney, Dislocation-obstacle interactions at the atomic level, in: J. Hirth, L. Kubin (Eds.), in: *Dislocations in Solids*, vol. 15, Elsevier, 2009, pp. 1–90, [http://dx.doi.org/10.1016/S1572-4859\(09\)01501-0](http://dx.doi.org/10.1016/S1572-4859(09)01501-0).
- [57] P. Hirel, AtomsK: A tool for manipulating and converting atomic data files, *Comput. Phys. Comm.* 197 (2015) 212–219, <http://dx.doi.org/10.1016/j.cpc.2015.07.012>.
- [58] M.R. Fellingner, A.M.Z. Tan, L.G. Hector Jr., D.R. Trinkle, Geometries of edge and mixed dislocations in BCC Fe from first-principles calculations, *Phys. Rev. Mater.* 2 (11) (2018) 113605, <http://dx.doi.org/10.1103/PhysRevMaterials.2.113605>.
- [59] E. Bitzek, P. Koskinen, F. Gähler, M. Moseler, P. Gumbsch, Structural relaxation made simple, *Phys. Rev. Lett.* 97 (17) (2006) 170201, <http://dx.doi.org/10.1103/PhysRevLett.97.170201>.
- [60] L. Ventelon, F. Willaime, Core structure and peierls potential of screw dislocations in α -Fe from first principles: cluster versus dipole approaches, *J. Comput. Aided Mol. Des.* 14 (Suppl 1) (2007) 85–94, <http://dx.doi.org/10.1007/s10820-007-9064-y>.
- [61] L. Dezerald, D. Rodney, E. Clouet, L. Ventelon, F. Willaime, Plastic anisotropy and dislocation trajectory in bcc metals, *Nat. Commun.* 7 (1) (2016) 11695, <http://dx.doi.org/10.1038/ncomms11695>.
- [62] A. Seeger, On the theory of the low-temperature internal friction peak observed in metals, *Phil. Mag.* 1 (7) (1956) 651–662, <http://dx.doi.org/10.1080/14786435608244000>.
- [63] P. Andric, W. Curtin, Atomistic modeling of fracture, *Modelling Simul. Mater. Sci. Eng.* 27 (1) (2018) 013001, <http://dx.doi.org/10.1088/1361-651X/aae40c>.
- [64] E. Podryabinkin, K. Garifullin, A. Shapeev, I. Novikov, MLIP-3: Active learning on atomic environments with moment tensor potentials, 2023, [arXiv:2304.13144](https://arxiv.org/abs/2304.13144).
- [65] V. Botu, R. Batra, J. Chapman, R. Ramprasad, Machine learning force fields: construction, validation, and outlook, *J. Phys. Chem. C* 121 (1) (2017) 511–522, <http://dx.doi.org/10.1021/acs.jpcc.6b10908>.
- [66] V.L. Deringer, M.A. Caro, G. Csányi, Machine learning interatomic potentials as emerging tools for materials science, *Adv. Mater.* 31 (46) (2019) 1902765, <http://dx.doi.org/10.1002/adma.201902765>.

- [67] C. van der Oord, M. Sachs, D.P. Kovács, C. Ortner, G. Csányi, Hyperactive learning for data-driven interatomic potentials, *npj Comp. Mater.* 9 (1) (2023) 168, <http://dx.doi.org/10.1038/s41524-023-01104-6>.
- [68] L. Zhang, D.Y. Lin, H. Wang, R. Car, E. Weinan, Active learning of uniformly accurate interatomic potentials for materials simulation, *Phys. Rev. Mater.* 3 (2) (2019) 023804, <http://dx.doi.org/10.1103/PhysRevMaterials.3.023804>.
- [69] M. Duesbery, V. Vitek, Plastic anisotropy in bcc transition metals, *Acta Mater.* 46 (5) (1998) 1481–1492, [http://dx.doi.org/10.1016/S1359-6454\(97\)00367-4](http://dx.doi.org/10.1016/S1359-6454(97)00367-4).
- [70] L. Proville, D. Rodney, M.-C. Marinica, Quantum effect on thermally activated glide of dislocations, *Nature Mater.* 11 (10) (2012) 845–849, <http://dx.doi.org/10.1038/nmat3401>.
- [71] L. Dezerald, L. Ventelon, E. Clouet, C. Denoual, D. Rodney, F. Willaime, Ab initio modeling of the two-dimensional energy landscape of screw dislocations in BCC transition metals, *Phys. Rev. B* 89 (2) (2014) 024104, <http://dx.doi.org/10.1103/PhysRevB.89.024104>.
- [72] L. Romaner, T. Pradhan, A. Kholobina, R. Drautz, M. Mrovec, Theoretical investigation of the 70.5° mixed dislocations in body-centered cubic transition metals, *Acta Mater.* 217 (2021) 117154, <http://dx.doi.org/10.1016/j.actamat.2021.117154>.
- [73] P. Grigorev, A.M. Goryaeva, M.-C. Marinica, J.R. Kermode, T.D. Swinburne, Calculation of dislocation binding to helium-vacancy defects in tungsten using hybrid ab initio-machine learning methods, *Acta Mater.* 247 (2023) 118734, <http://dx.doi.org/10.1016/j.actamat.2023.118734>.
- [74] S.H. Haghighat, J. von Pezold, C. Race, F. Körmann, M. Friák, J. Neugebauer, D. Raabe, Influence of the dislocation core on the glide of the 1/2{111}{110} edge dislocation in BCC-iron: An embedded atom method study, *Comput. Mater. Sci.* 87 (2014) 274–282, <http://dx.doi.org/10.1016/j.commatsci.2014.02.031>.
- [75] S. Chiesa, P. Derlet, S. Dudarev, Free energy of a {110} dumbbell interstitial defect in BCC Fe: Harmonic and anharmonic contributions, *Phys. Rev. B* 79 (21) (2009) 214109, <http://dx.doi.org/10.1103/PhysRevB.79.214109>.
- [76] W.-S. Ko, B.-J. Lee, Origin of unrealistic blunting during atomistic fracture simulations based on MEAM potentials, *Phil. Mag.* 94 (16) (2014) 1745–1753, <http://dx.doi.org/10.1080/14786435.2014.895441>.
- [77] P. Hiremath, S. Melin, E. Bitzek, P.A. Olsson, Effects of interatomic potential on fracture behaviour in single-and bicrystalline tungsten, *Comput. Mater. Sci.* 207 (2022) 111283, <http://dx.doi.org/10.1016/j.commatsci.2022.111283>.