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Measurement of the branching fraction for the decay $\psi(3686) \rightarrow \phi K_S^0 K_S^0$

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Based on $(448.1 \pm 2.9) \times 10^6$ $\psi(3686)$ events collected with the BESIII detector operating at the BEPCII collider, the decay $\psi(3686) \rightarrow \phi K_S^0 K_S^0$ is observed for the first time. Taking the interference between $\psi(3686)$ decay and continuum production into account, the branching fraction of this decay is measured to be $\mathcal{B}(\psi(3686) \rightarrow \phi K_S^0 K_S^0) = (3.53 \pm 0.20 \pm 0.21) \times 10^{-5}$, where the first uncertainty is statistical and the second is systematic. Combining with the world average value for $\mathcal{B}(J/\psi \rightarrow \phi K_S^0 K_S^0)$, the ratio $\mathcal{B}(\psi(3686) \rightarrow \phi K_S^0 K_S^0)/\mathcal{B}(J/\psi \rightarrow \phi K_S^0 K_S^0)$ is determined to be $(6.0 \pm 1.6)\%$, which is suppressed relative to the 12% rule.

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I. INTRODUCTION

The J/ψ and $\psi(3686)$ are nonrelativistic bound states of a charm and an anticharm quark, called charmonium. Experimental measurements of the decays of charmonium states ψ [which denotes both the J/ψ and $\psi(3686)$] can provide an ideal laboratory to study the dynamics of strong force physics, validate models and test various aspects of quantum chromodynamics (QCD) [1,2]. Since the discovery of the $\psi(3686)$ in 1974 [3], it has been studied for over 40 years. However, there are still problems and puzzles that need to be understood [4].

Perturbative QCD predicts that both the J/ψ and $\psi(3686)$ decay into light-hadron final states with a width proportional to the square of the wave function at the origin [5,6]. This yields the widely known “12% rule”: $Q_h = \mathcal{B}_{\psi(3686) \rightarrow h}/\mathcal{B}_{J/\psi \rightarrow h} \simeq \mathcal{B}_{\psi(3686) \rightarrow e^+e^-}/\mathcal{B}_{J/\psi \rightarrow e^+e^-} \simeq 13.3\%$ [7], where h denotes any exclusive hadronic decay mode. Although this relation is expected to hold to a reasonably good degree for both inclusive and exclusive decays [8], it fails severely in the case of vector-pseudoscalar meson final states, such as $\rho\pi$ [9]. With the recent experimental results on J/ψ and $\psi(3686)$ two-body decays, such as the vector-tensor channel [10], the pseudoscalar-pseudoscalar channel [11], baryon-antibaryon mode [12], and multibody decays such as $\phi\pi^+\pi^-$, $p\bar{p}\pi^0$ [13], etc., extensive tests of the 12% rule have been performed. The ratios Q_h for some decay modes are

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suppressed, some are enhanced, while others obey the 12% rule. More experimental results are still desirable to test the 12% rule and further investigate charmonium decay mechanisms [4].

In this work, we present the first observation and branching fraction (BF) measurement of the decay $\psi(3686) \rightarrow \phi K_S^0 K_S^0$ by analyzing $(448.1 \pm 2.9) \times 10^6$ $\psi(3686)$ events collected with the BESIII detector in 2009 and 2012 [14]. In addition, the 12% rule in the decay $\psi(3686) \rightarrow \phi K_S^0 K_S^0$ are tested.

II. BESIII EXPERIMENT AND MONTE CARLO SIMULATION

The BESIII detector [15] records symmetric e^+e^- collisions provided by the BEPCII [16] storage ring in the c.m. energy range from 2.00 GeV to 4.95 GeV, with a peak luminosity of $1 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$ achieved at $\sqrt{s} = 3.77 \text{ GeV}$.

The cylindrical core of the BESIII detector covers 93% of the full solid angle and consists of a helium-based multilayer drift chamber (MDC), a plastic scintillator time-of-flight (TOF) system, and a CsI(Tl) electromagnetic calorimeter (EMC), which are all enclosed in a superconducting solenoidal magnet providing a 1.0 T magnetic field. The solenoid is supported by an octagonal flux-return yoke with resistive plate counter muon identification modules interleaved with steel. The charged-particle momentum resolution at 1 GeV/c is 0.5%, and the dE/dx resolution is 6% for electrons from Bhabha scattering. The EMC measures photon energies with a resolution of 2.5% (5%) at 1 GeV in the barrel (end cap) region. The time resolution in the TOF barrel region is 68 ps, while that in the end cap region is 110 ps.

Simulated data samples produced with a Geant4-based [17] Monte Carlo (MC) package, which includes the geometric description of the BESIII detector [18,19] and the detector response, are used to determine detection efficiencies and to estimate backgrounds. The simulation models the beam energy spread and initial state radiation in the e^+e^- annihilations with the generator KKMC [20].

The inclusive MC sample includes the production of the $\psi(3686)$ resonance, the initial state radiation production of the J/ψ , and the continuum processes incorporated in KKMC [20]. All particle decays are modeled with EvtGen [21,22] using BF's either taken from the Particle Data Group (PDG) [7], when available, or otherwise estimated with LUNDCHARM [23,24]. Final state radiation from charged final state particles is incorporated using the PHOTOS package [25]. To determine the detection efficiency for the signal process, 2×10^5 signal MC samples are generated with a modified data-driven generator BODY3 [21,26], which could simulate contributions from different intermediate states in data for a given three-body final state. Data sets collected at center-of-mass energies ranging from 3.508 GeV to 3.773 GeV are used to estimate the contribution from continuum processes. The $\psi(3686)$ scan data sets ranging from 3.670 GeV to 3.710 GeV are used to estimate the phase angles between continuum processes and the $\psi(3686)$. The total integrated luminosity for all data except 3.773 GeV and psi(3686) scan data is 504.6 pb^{-1} , while the integrated luminosity for 3.773 GeV is 2931.8 pb^{-1} [27] and the average integrated luminosity for $\psi(3686)$ scan data is 92.2 pb^{-1} .

III. EVENT SELECTION AND DATA ANALYSIS

To select candidate events for $\psi(3686) \rightarrow \phi K_S^0 K_S^0$, the ϕ and K_S^0 mesons are reconstructed using their decays to $K^+ K^-$ and $\pi^+ \pi^-$, respectively.

Each candidate signal event is required to have at least six charged tracks. The charged tracks detected in the MDC are required to be within a polar angle (θ) range of $|\cos\theta| < 0.93$, where θ is defined with respect to the z axis, which is the symmetry axis of the MDC. The charged tracks from the $\phi \rightarrow K^+ K^-$ decay are required to have a distance of closest approach to the interaction point (IP) less than 10 cm along the z axis ($|V_z|$) and less than 1 cm in the transverse plane ($|V_{xy}|$). The dE/dx information recorded by the MDC and the time-of-flight information in the TOF are used for particle identification (PID), and the charged tracks are assigned as kaons when the kaon hypothesis has a greater likelihood, *i.e.*, $\mathcal{L}(K) > \mathcal{L}(\pi)$.

The charged pions used for K_S^0 reconstruction are required to have a greater likelihood for the pion hypothesis, *i.e.*, $\mathcal{L}(\pi) > \mathcal{L}(K)$. Both pions must satisfy $|\cos\theta| < 0.93$ and $|V_z| < 20 \text{ cm}$ and their trajectories are constrained to originate from a common vertex by applying a vertex fit [28]. The invariant mass of the $\pi^+ \pi^-$ pair $M_{\pi^+ \pi^-}$ needs to be in the range (0.45, 0.55) GeV/c^2 . Here, $M_{\pi^+ \pi^-}$ is calculated with the pions constrained to originate at the decay vertex. The K_S^0 candidate is then formed and the opposite direction of its momentum is constrained to point to the IP. The decay length of the K_S^0 candidate is required to be greater than twice the vertex resolution.

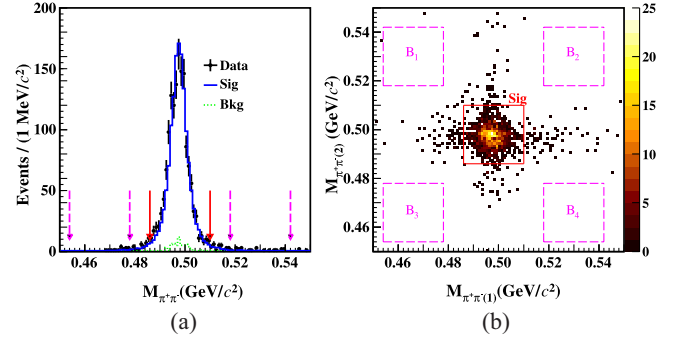


FIG. 1. (a) The distribution of $M_{\pi^+ \pi^-}$, where the signal region is defined as $M_{\pi^+ \pi^-} \in (0.486, 0.510) \text{ GeV}/c^2$ and the sideband regions are defined as $M_{\pi^+ \pi^-} \in (0.454, 0.478)$ or $(0.518, 0.542) \text{ GeV}/c^2$, respectively. The black points with error bars are data. The blue solid curve is the signal MC. The green dashed curve is the inclusive MC. The pair of red arrows shows the signal region, and the two pairs of pink dashed arrows show the sideband region. (b) The 2D distribution of $M_{\pi^+ \pi^{(2)}}$ vs. $M_{\pi^+ \pi^{(1)}}$ (the subscripts 1 and 2 indicate the two $\pi^+ \pi^-$ combinations, respectively) in the signal and sideband regions. The red solid rectangle shows the 2D signal region where both K_S^0 candidates are required to be in the range (0.486, 0.510) GeV/c^2 , and the pink dashed rectangles show the 2D sideband regions where both K_S^0 candidates are required to be in the range of (0.454, 0.478) or (0.518, 0.542) GeV/c^2 .

A four-constraint (4C) kinematic fit imposing energy and momentum conservation is performed. The helix parameters of the charged tracks in the MC events are corrected to improve the consistency with data. The correction factors for K^\pm are cited from Ref. [29], while the correction factors for π^\pm are determined by studying the $\psi(3686) \rightarrow \pi^+ \pi^- K_S^0 K_S^0$, $K_S^0 \rightarrow \pi^+ \pi^-$ process. The events satisfying $\chi_{4C}^2 < 50$ are kept for further analysis. If there are multiple candidates in an event, the one with the smallest χ_{4C}^2 is kept for further analysis.

Analysis of the $\psi(3686)$ inclusive MC sample with an event type examination tool, TopoAna [30], indicates that the main background events come from $\psi(3686) \rightarrow \pi^+ \pi^- J/\psi$ with $J/\psi \rightarrow \phi \pi^+ \pi^-$, $\phi \rightarrow K^+ K^-$. The background events, however, do not contain a $K_S^0 K_S^0$ pair and can thus be described by $K_S^0 K_S^0$ sideband events. The one-dimensional distribution of $M_{\pi^+ \pi^-}$ for the K_S^0 candidates in the signal and sideband regions is shown in Fig. 1(a). The two-dimensional (2D) $M_{\pi^+ \pi^-}$ distribution for the two K_S^0 candidates is shown in Fig. 1(b), where the signal region in the red solid rectangle indicates that both K_S^0 candidates are required to satisfy $M_{\pi^+ \pi^-} \in (0.486, 0.510) \text{ GeV}/c^2$ (marked as Sig). The size of the signal region corresponds to three times the resolution around the known K_S^0 mass [7]. The 2D sideband region is defined as $M_{\pi^+ \pi^-} \in (0.454, 0.478) \text{ GeV}/c^2$ or $(0.518, 0.542) \text{ GeV}/c^2$ (marked as B_i with $i = 1, 2, 3, 4$), where both K_S^0 candidates lie in the sideband region.

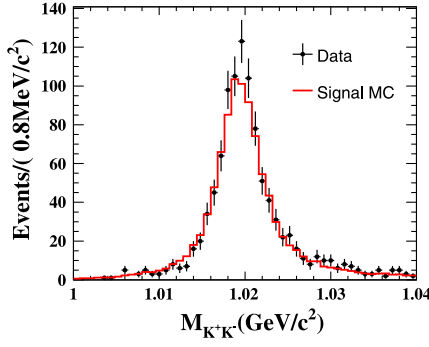


FIG. 2. The $M_{K^+K^-}$ distribution for the accepted candidates in the 2D K_S^0 signal region for the $\psi(3686)$ data. The black points with error bars are data. The red solid curve is the signal MC.

Figure 2 shows the distributions of $M_{K^+K^-}$ in the 2D K_S^0 signal region. The background rate determined by fitting to the $M_{K^+K^-}$ distributions was found to be extremely low, reaching a value of 10^{-6} . In the fit, the ϕ signal shape was described with the MC signal shape convolved with a parameter-floating Gaussian function, and the background was described with a first-order polynomial function. This low background level allows us to directly count the number of signal events in the 2D K_S^0 signal region without considering any significant background contributions. The number of net $\psi(3686) \rightarrow \phi K_S^0 K_S^0$ candidate events is given by $N_{\text{net}}^{\psi(3686)} = N_{\text{sig}}^{\psi(3686)} - N_{\text{bkg}}^{\psi(3686)}$, where $N_{\text{sig}}^{\psi(3686)}$ is determined by counting the events left in the 2D K_S^0 signal region and $N_{\text{bkg}}^{\psi(3686)}$ is estimated with the mean value of the background events in the sideband regions defined in Fig. 1(b), *i.e.*, $N_{\text{bkg}}^{\psi(3686)} = \sum B_i/4$ (with $i = 1, 2, 3, 4$). For $N_{\text{sig}}^{\psi(3686)}$ and $N_{\text{bkg}}^{\psi(3686)}$, the values are 1023 ± 32 and 0, respectively.

To investigate the background from the continuum processes [14] $e^+e^- \rightarrow \phi K_S^0 K_S^0$, the same selection criteria

TABLE I. The continuum background estimation for each data set, where E_{CM} is the center-of-mass energy; $\mathcal{L}_{\text{cont}}$ is the integrated luminosity, N_{net} is the number of signal events in the 2D K_S^0 signal region after subtracting the backgrounds estimated with the sideband method, f_c is the scale factor for each energy point, and N_{cont} is the continuum contribution calculated with $N_{\text{net}} \times f_c$.

E_{CM} (GeV)	$\mathcal{L}_{\text{cont}}$ (pb $^{-1}$)	N_{net}	f_c	N_{cont}
3.508	183.64	32 ± 6	3.30	106 ± 20
3.510	181.79	28 ± 7	3.34	94 ± 23
3.539	25.50	7 ± 3	24.17	169 ± 72
3.553	42.56	10 ± 3	14.59	146 ± 44
3.554	27.24	1 ± 1	22.81	23 ± 23
3.650	43.88	14 ± 4	14.94	209 ± 60
3.773	2931.80	465 ± 22	0.24	112 ± 5

and sideband definition are applied on the off-resonance data samples. The obtained values of signal yields N_{net} from the continuum data samples are listed in Table I. A scale factor f_c is considered to account for the energy dependence of the cross section.

$$f_c = \frac{\mathcal{L}_{\psi(3686)}}{\mathcal{L}_{\text{cont}}} \times \frac{s_{\text{cont}}^n}{s_{\psi(3686)}^n}, \quad (1)$$

where $\mathcal{L}_{\psi(3686)}$ [14] and $\mathcal{L}_{\text{cont}}$ are the integrated luminosities for the $\psi(3686)$ and continuum data samples, and $s_{\psi(3686)}$ and s_{cont} are the squares of the corresponding c.m. energies. We use $n = 1$ in the nominal result, which corresponds to a $1/s$ dependence for the continuum cross section. The impact of this assumption for n will be considered as a source of systematic uncertainty. The calculated results for N_{cont} estimated from different data sets are listed in the last column of Table I. To combine these different N_{cont} into an average combined result \bar{N}_{cont} , we use a weighted average method where the weights for each N_{cont} are proportional to the inverse square of the corresponding uncertainties. The \bar{N}_{cont} is determined to be 108 ± 5 .

Figure 3 shows the Dalitz plots for the accepted candidates in data and BODY3 signal MC samples. The one-dimensional projections of the Dalitz plots are shown in Fig. 4. The detection efficiency for $\psi(3686) \rightarrow \phi K_S^0 K_S^0$ is determined to be $(18.50 \pm 0.09)\%$, where the uncertainty comes from the MC statistics.

The interference between the $\psi(3686)$ decay and the continuum production $e^+e^- \rightarrow \phi K_S^0 K_S^0$ is considered by fitting to the cross sections in the vicinity of the $\psi(3686)$, followed the method in Ref [31]. The fit yields two solutions for the phase angle between the $\psi(3686)$ and continuum processes, corresponding to a constructive interference of $(83 \pm 11)^\circ$ and a destructive interference of $-(85 \pm 9)^\circ$ (with more details in Appendix). The former is determined to be the physical one by the isospin symmetry with the decay of $\psi(3686) \rightarrow \phi K^+ K^-$ [7]. The interference contribution is estimated by scaling the continuum contribution with the ratio of the cross sections between the interference term and the continuum process. It is determined to be $N_{\text{inter}} = 228 \pm 24$.

The BF of $\psi(3686) \rightarrow \phi K_S^0 K_S^0$ is determined by

$$\mathcal{B}_{\psi(3686) \rightarrow \phi K_S^0 K_S^0} = \frac{N_{\text{net}}^{\psi(3686)} - \bar{N}_{\text{cont}} - N_{\text{inter}}}{N_{\psi(3686)} \cdot \epsilon \cdot \mathcal{B}_{\phi \rightarrow K^+ K^-} \cdot \mathcal{B}_{K_S^0 \rightarrow \pi^+ \pi^-}^2}, \quad (2)$$

where $N_{\text{net}}^{\psi(3686)} - \bar{N}_{\text{cont}} - N_{\text{inter}} = 687 \pm 40$ is the net number of $\psi(3686) \rightarrow \phi K_S^0 K_S^0$, $N_{\psi(3686)} = (448.1 \pm 2.9) \times 10^6$ is the total number of $\psi(3686)$ events [14],

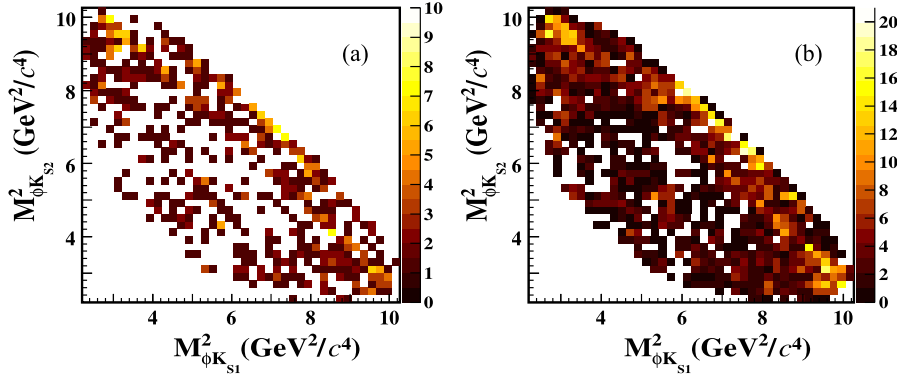


FIG. 3. Dalitz plots of $M^2_{\phi K_{S1}^0}$ vs. $M^2_{\phi K_{S2}^0}$ for the accepted candidates in (a) data and (b) BODY3 signal MC events.

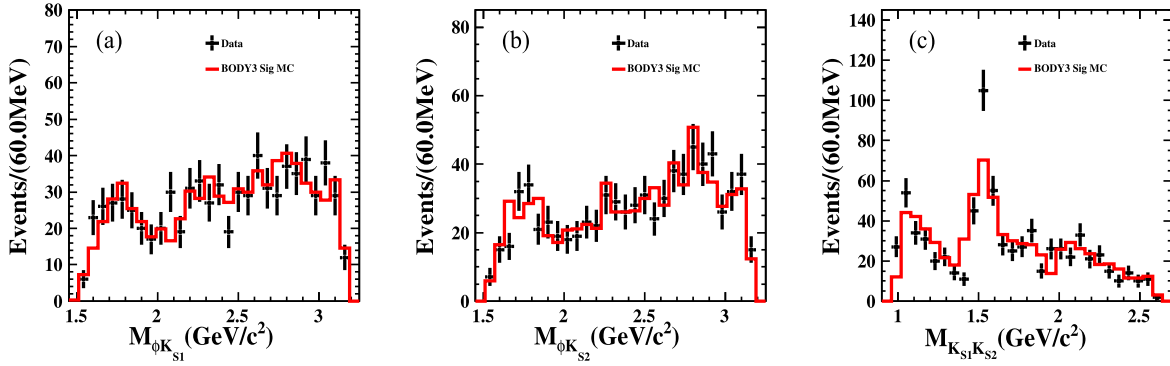


FIG. 4. Invariant mass distributions for (a) $M(\phi K_{S1}^0)$ (b) $M(\phi K_{S2}^0)$ (c) $M(K_S^0 K_S^0)$. The points with error bars are data, the red histograms are the BODY3 signal MC.

$\mathcal{B}_{\phi \rightarrow K^+ K^-}$, and $\mathcal{B}_{K_S^0 \rightarrow \pi^+ \pi^-}$ are the BFs of $\phi \rightarrow K^+ K^-$ and $K_S^0 \rightarrow \pi^+ \pi^-$ quoted from the PDG [7], and $\varepsilon = (18.50 \pm 0.5)$ is the detection efficiency for $\psi(3686) \rightarrow \phi K_S^0 K_S^0$. Based on these numbers, we can obtain $\mathcal{B}_{\psi(3686) \rightarrow \phi K_S^0 K_S^0} = (3.53 \pm 0.20) \times 10^{-5}$.

IV. SYSTEMATIC UNCERTAINTY

The systematic uncertainties are evaluated from a variety of sources, as summarized in Table II.

The MDC tracking and PID efficiencies for kaons are studied using a control sample of $J/\psi \rightarrow K_S^0 K^\pm \pi^\mp$, $K_S^0 \rightarrow \pi^+ \pi^-$. The difference in the tracking or PID efficiencies between data and MC simulation is assigned as individual systematic uncertainties, which is 1.0% for both tracking and PID per kaon. The PID efficiency for pions is determined based on studies of a control sample of $J/\psi \rightarrow \pi^+ \pi^- \pi^0$. The difference in the PID efficiencies between the data and MC simulation, 1.4%, is assigned as the corresponding systematic uncertainty for the four pions.

The efficiency of K_S^0 reconstruction is estimated using a control sample of $J/\psi \rightarrow K^*(892)^\mp K^\pm$, $K^*(892)^\mp \rightarrow K_S^0 \pi^\mp$ [32]. The uncertainty includes the tracking efficiency for $\pi^+ \pi^-$, the requirement of $M_{\pi^+ \pi^-}$ and the requirement on

TABLE II. Relative systematic uncertainties in the BF measurement.

Source	Uncertainty (%)
K^\pm tracking	2.0
K^\pm PID	2.0
π^\pm PID	1.4
K_S^0 reconstruction	2.3
$N_{\psi(3686)}$	0.7
BODY3 generator	3.6
4C kinematic fit	1.3
f_c factor	0.4
MC statistics	0.5
$\mathcal{B}^{\text{PDG}}(K_S^0 \rightarrow \pi^+ \pi^-)$	0.2
$\mathcal{B}^{\text{PDG}}(\phi \rightarrow K^+ K^-)$	1.0
Interference	2.1
Total	6.0

the K_S^0 decay length. The difference in the K_S^0 reconstruction efficiencies between the data and MC simulation, 1.2% per K_S^0 , is taken as the systematic uncertainty, which is assigned to be 2.3%.

The number of $\psi(3686)$ events is determined from an analysis of inclusive hadronic $\psi(3686)$ decays. The uncertainty of the number of $\psi(3686)$ events, 0.7% [14], is taken as the systematic uncertainty. The systematic uncertainty of the BODY3 MC model comes from the range and the bin divisions of the input Dalitz plot. The uncertainty is estimated by changing the bin size by 20% and taking alternative ranges at the same time. The maximum change of efficiency is taken as the uncertainty, which is 3.6%.

The systematic uncertainty of the 4C kinematic fit is determined by varying the helix parameters by ± 1 standard deviation. The maximum change of signal efficiency, 1.3%, is taken as the corresponding systematic uncertainty. The systematic uncertainties due to the scale factor f_c for the continuum background originate from the uncertainty of luminosity and the uncertainty of energy dependence for the continuum cross section. The systematic uncertainty originating from the luminosity is estimated by recalculating the BF after changing the luminosity obtained by different processes. The maximum difference of the BF, 0.1%, is taken as the uncertainty. The systematic uncertainty due to the energy dependence relationship is estimated by comparing the difference between $1/s$ and $1/s^3$ [33] assumptions. The change of the remeasured BF, 0.4%, is assigned as the corresponding systematic uncertainty.

The uncertainty due to the limited MC statistics is considered as one source of systematic uncertainty. It is evaluated to be 0.5%. The uncertainties of the quoted BFs of $\mathcal{B}(K_S^0 \rightarrow \pi^+\pi^-)$ and $\mathcal{B}(\phi \rightarrow K^+K^-)$ are assigned to be 0.2% and 1.0%, respectively.

The uncertainty from the interference between $\psi(3686)$ decay and continuum production is determined by varying the measured phase angle φ by ± 1 standard deviation. The maximum change of the BF, 2.1% is taken as the corresponding systematic uncertainty.

Assuming that all sources are independent, the total systematic uncertainty is determined to be 6.0% as listed in Table II.

V. SUMMARY

Using $(448.1 \pm 2.9) \times 10^6$ $\psi(3686)$ events accumulated by the BESIII detector, the decay $\psi(3686) \rightarrow \phi K_S^0 K_S^0$ is observed for the first time. Taking the interference between $\psi(3686)$ decay and continuum production into account,

its BF is measured to be $(3.53 \pm 0.20 \pm 0.21) \times 10^{-5}$, where the first uncertainty is statistical, the second one is systematic. Using the world average of $\mathcal{B}(J/\psi \rightarrow \phi K_S^0 K_S^0) = (5.9 \pm 1.5) \times 10^{-4}$ [7], the ratio between the two BFs is determined to be $\mathcal{Q}_{\phi K_S^0 K_S^0} = (6.0 \pm 1.6)\%$, which is suppressed relative to the 12% rule.

The 2.7×10^9 $\psi(3686)$ events recently collected by BESIII [8] offer an opportunity to improve the precision of \mathcal{Q}_h and will lead to a better understanding of the phenomenon.

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APPENDIX: FIT TO THE CROSS SECTIONS FOR $e^+e^- \rightarrow \phi K_S^0 K_S^0$ IN THE VICINITY OF $\psi(3686)$

In this appendix we describe some of the details of our fits to the cross sections for $e^+e^- \rightarrow \phi K_S^0 K_S^0$ in the vicinity of the $\psi(3686)$.

The dressed cross sections of $e^+e^- \rightarrow \phi K_S^0 K_S^0$ in the vicinity of the $\psi(3686)$ are shown in Fig. 5. A least- χ^2 fit is performed to the dressed cross section $\sigma^{\text{dressed}}(s)$ using the following formula [31,34]:

$$\sigma^{\text{dressed}}(s) = |A_{\text{cont}}(s) + A_{\text{res}}(s) \times e^{i\varphi}|^2, \quad (\text{A1})$$

where \sqrt{s} is the c.m. energy, $A_{\text{cont}}(s)$ and $A_{\text{res}}(s)$ represent the amplitudes of the continuum process and $\psi(3686)$, respectively, while φ denotes the relative phase between the two amplitudes. $A_{\text{cont}}(s)$ is defined as \sqrt{C}/\sqrt{s}^n , and the values for C and n can be determined by fitting to the $\psi(3686)$ -scan data. These values of C and n will remain fixed in the fits to σ^{dressed} . $A_{\text{res}}(s)$ is parametrized by the single Breit-Wigner amplitude form [35].

The fitting results are shown in Fig. 5. The fit yields two solutions, corresponding to a constructive interference of $(83 \pm 11)^\circ$ and a destructive interference of $-(85 \pm 9)^\circ$. The destructive solution is excluded from the analysis due to its significant violation of isospin symmetry with the $\psi(3686) \rightarrow \phi K^+ K^-$ [7] decay.

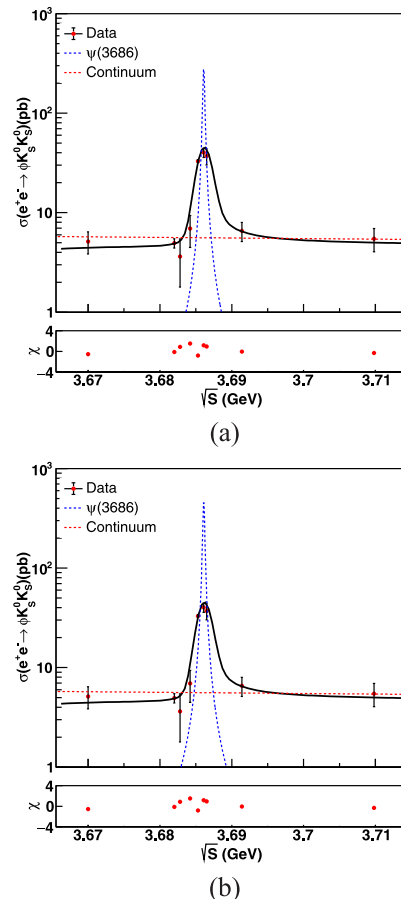


FIG. 5. The dressed cross sections of $e^+e^- \rightarrow \phi K_S^0 K_S^0$ as a function of c.m. energy for (a) constructive solution with $\phi = (83 \pm 11)^\circ$ and (b) destructive solution with $\phi = -(85 \pm 9)^\circ$. The two fits have the same goodness of $\chi^2/\text{ndf} = 9.88/6$. The points with error bars are data, and the red and blue dashed curves represent the continuum contribution (with $C = (4.03 \pm 0.76) \times 10^3 \text{ GeV}^n \cdot \text{pb}$, $n = 5.01 \pm 0.10$) and $\psi(3686)$ contribution, respectively. The χ distributions of the two fits are shown in the bottom panel.

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