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## Practice-inspired contributions to inventory theory

Prak, Derk Rutger Jordi

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# **Practice-inspired contributions to inventory theory**

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university of  
 groningen

# Practice-inspired contributions to inventory theory

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to obtain the degree of PhD at the  
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 and in accordance with  
 the decision by the College of Deans.

This thesis will be defended in public on

Thursday 23 May 2019 at 16.15 hours

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# Contents

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<b>1</b>	<b>Introduction</b>	<b>1</b>
1.1	Demand parameter uncertainty . . . . .	4
1.2	Demand parameter estimation from periodic data . . . . .	7
1.3	Decoupling stock reviews and order moments . . . . .	8
1.4	Lead times and order costs in repair services . . . . .	9
1.5	Academic articles . . . . .	11
<b>2</b>	<b>On the calculation of safety stocks when demand is forecasted</b>	<b>13</b>
2.1	Introduction . . . . .	14
2.2	Related literature . . . . .	16
2.3	Corrected variance of the lead time demand when $\mu$ is unknown . . . . .	18
2.4	Correction factors for safety stocks . . . . .	21
2.5	Corrected demand distribution when both $\mu$ and $\sigma^2$ are unknown . . . . .	25
2.6	Applications to inventory systems . . . . .	27
2.7	Numerical results . . . . .	28
2.8	Conclusion . . . . .	32
<b>3</b>	<b>A general method to address forecasting uncertainty in inventory models</b>	<b>35</b>
3.1	Introduction . . . . .	36
3.2	Related literature . . . . .	38
3.3	Model . . . . .	41
3.3.1	General framework . . . . .	42
3.3.2	Inventory model . . . . .	42
3.3.3	Demand models and derivation of the predictive lead time demand distribution . . . . .	46
3.4	Numerical study . . . . .	54
3.4.1	Mean-stationary, normally distributed demand . . . . .	54

3.4.2	Single exponential smoothing for mean-stationary, normally distributed demand . . . . .	58
3.4.3	Normally distributed, trended demand . . . . .	59
3.4.4	Demand is a normal random walk . . . . .	61
3.5	Demand misspecification . . . . .	62
3.6	Conclusion . . . . .	64
<b>4</b>	<b>Compound Poisson parameter estimation for inventory control</b>	<b>67</b>
4.1	Introduction . . . . .	68
4.2	Related literature . . . . .	72
4.3	Demand model, inventory model, and Size-Interval methods . . . . .	75
4.3.1	Demand model . . . . .	75
4.3.2	Inventory model . . . . .	76
4.3.3	Mis-application of period Size-Interval methods . . . . .	77
4.4	Consistent estimators . . . . .	81
4.4.1	The standard method-of-moments estimator . . . . .	82
4.4.2	The maximum likelihood estimator . . . . .	82
4.4.3	The proposed method . . . . .	83
4.5	Numerical study: comparing consistent estimators . . . . .	86
4.5.1	Estimation accuracy . . . . .	86
4.5.2	Inventory control . . . . .	91
4.6	Conclusion . . . . .	94
<b>5</b>	<b>Periodic review and continuous ordering</b>	<b>97</b>
5.1	Introduction . . . . .	98
5.2	The one-period problem: base-line model . . . . .	100
5.3	The multi-period problem: general optimal policy . . . . .	104
5.4	Sensitivity analysis and comparison with pure periodic review . . . . .	108
5.4.1	Numerical examples and sensitivity analysis . . . . .	108
5.4.2	Cost savings of continuous over periodic ordering . . . . .	111
5.4.3	Applications with Gamma distributed demand . . . . .	112
5.5	Conclusion . . . . .	114
<b>6</b>	<b>The Repair Kit Problem with positive lead times and fixed ordering costs</b>	<b>117</b>
6.1	Introduction . . . . .	118

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6.2	Related literature . . . . .	120
6.3	Model and analysis . . . . .	123
6.3.1	Model description . . . . .	123
6.3.2	Heuristic solution procedure . . . . .	128
6.4	Case study description . . . . .	129
6.5	Results . . . . .	131
6.5.1	Performance of the proposed solution procedure . . . . .	132
6.5.2	Case study results . . . . .	133
6.6	Conclusion . . . . .	138
<b>7</b>	<b>Conclusion &amp; discussion</b>	<b>141</b>
	<b>Bibliography</b>	<b>147</b>
	<b>Summary</b>	<b>161</b>
	<b>Samenvatting</b>	<b>165</b>
	<b>Acknowledgments</b>	<b>169</b>
	<b>Curriculum Vitæ</b>	<b>171</b>



