Solubilities of Sub- and Supercritical Carbon Dioxide in Polyester Resins

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In supercritical carbon dioxide (CO₂) assisted polymer processes the solubility of CO₂ in a polymer plays a vital role. The higher the amount of CO₂ dissolved in a polymer the higher is the viscosity reduction of the polymer. Solubilities of CO₂ in polyester resins based on propoxylated bisphenol (PPB) and ethoxylated bisphenol (PEB) have been measured using a magnetic suspension balance at temperatures ranging from 333 to 420 K and pressures up to 30 MPa. An optical cell has been used to independently determine the swelling of the polymers, which has been incorporated in the buoyancy correction. In both polyester resins, the solubility of CO₂ increases with increasing pressure and decreasing temperature as a result of variations in CO₂ density. The experimental solubility has been correlated to the Sanchez–Lacombe equation of state. POLYM. ENG. SCI., 46:643–649, 2006. © 2006 Society of Plastics Engineers

INTRODUCTION

Polyester resins in powder form are frequently used in paint and toner industry. Milling, grinding, and spray drying are the particle formation processes commonly used in the industry. Narrow particle size distribution, solvent recovery, and the prevention of volatile organic components (VOC) emission are the major challenges associated with these processes. Moreover, the classical processes have clear disadvantages in terms of energy requirement due to expensive cryogenic cooling, and problems with product quality due to heat dissipation during milling, which causes agglomeration by molten polymer particles. This has motivated chemical engineers as well as chemists to adopt supercritical technologies in which the problems described above can be eliminated.

Unusual solvent properties above the critical point like gas-like diffusivities and liquid-like densities make supercritical technology attractive. Particles from gas saturated solution (PGSS) is one of the particle production methods using a supercritical fluid [1]. Supercritical carbon dioxide (CO₂) has a high solubility in many polymers. In PGSS, the viscosity of the polymer, particle size, and morphology of the particles are mainly determined by the amount of CO₂ dissolved in the polymer. Therefore, it is important to determine the solubilities of CO₂ in a polymer at different conditions so as to define the processing window.

Various experimental methods exist to determine the solubility of CO₂ in solid and in molten polymers. Phase separation [2], volumetric [3], and gravimetric [4] methods are commonly used. In the first two methods, the amount of polymer required is large compared to gravimetric methods, and hence, the time required to reach equilibrium is substantially longer. Moreover, high accuracy in pressure sensors and volume measurements are required in the first two methods for solubility calculations. These disadvantages are overcome by a gravimetric method that uses a microbalance [4]. The principle behind the gravimetric method is the weight difference between a gas-free and a gas-sorbed polymer sample. With a microbalance of high accuracy, even a small change in the weight of the polymer sample due to dissolved gas can be measured. Recently, a magnetic suspension balance (MSB), developed by Kleinrahm and Wagner [5], has been used to measure the solubility of CO₂ in various polymers [6–8]. A major advantage of using the MSB is that measurements can be carried out at elevated...
temperatures and pressures without having direct contact between a sample and the balance.

The main objective of this work was to determine the solubilities of CO\textsubscript{2} in polyester resins using an MSB. An important parameter in such gravimetric measurements is the swelling of polymer due to dissolved CO\textsubscript{2}. A buoyancy correction due to swelling has to be taken into account while calculating the dissolved quantity of CO\textsubscript{2} in a polymer [6–8]. Therefore, an optical cell has been used in separate experiments to observe the swelling of polymers in the presence of CO\textsubscript{2} at similar conditions. The other objective of the study was to describe the solubility data using a thermodynamic model, the Sanchez–Lacombe equation of state (S-L EOS) [9, 10].

**EXPERIMENTAL PROCEDURES**

**Materials**

Polyester resins based on propoxylated bisphenol (PPB, CAS: 177834–94-5) and ethoxylated bisphenol (PEB, CAS: 170831–75-1) were obtained from Akzo Nobel, The Netherlands. The physical properties of the polymers are provided in Table 1. Both polymers are amorphous, which was confirmed by DSC measurements. The dry grade (> 99.5%) CO\textsubscript{2} was used for the measurements. All chemicals were used as-received without further purification.

**Apparatus and Method**

**Magnetic Suspension Balance.** An MSB (Fig. 1) was used for measuring the solubility of CO\textsubscript{2} in both polymers. The MSB can be used at temperatures up to 473 K and pressures up to 50 MPa. A polymer sample was kept in a basket that was not directly connected to the weighing balance (microbalance), but was kept in place using a so-called suspension magnet. The suspension consists of a measuring load, a sensor core, and a permanent magnet. The measured weight of the basket containing the polymer was transmitted by a magnetic suspension coupling to an external microbalance, and thus, leak-proof measurements can be performed. In the MSB apparatus, the microbalance can be tare and calibrated during measurements. Using the MSB, the amount of CO\textsubscript{2} dissolved in a polymer was determined from the following relationship:

\[
W_{\text{CO}_2} = \Delta W + \rho_{\text{CO}_2}(V_P(P, T, S) + V_b)
\]  

(1)

where \(\Delta W\) is the weight difference between a polymer sample in the absence of CO\textsubscript{2} at time \(t = 0\) and the same sample equilibrated with CO\textsubscript{2} at a desired temperature \(T\) and pressure \(P\) until a constant weight is obtained. The second term in Eq. 1 is a buoyancy correction term, which is required as polymers swell considerably in the presence of dissolved CO\textsubscript{2}. \(\rho_{\text{CO}_2}\), \(V_P(P, T, S)\), and \(V_b\) are the density of CO\textsubscript{2}, the volume of the swollen polymer after contacting CO\textsubscript{2} with a solubility \(S\), and the volume of the basket, respectively. As it was not possible to observe the polymer swelling simultaneously during the solubility measurements, an optical cell was used separately for the swelling measurements.

CO\textsubscript{2} solubility measurements were carried out above the glass-transition temperature \((T_g)\) of both polyesters. Temperature and pressure were varied from 333 to 420 K and 5–30 MPa, respectively. A polymer sample was first exposed to a vacuum for a few hours at the measurement temperature and an initial reading was recorded. This was followed by addition of CO\textsubscript{2} in the chamber until the desired pressure was attained. The sample was allowed to attain sorption equilibrium (in terms of the weight differ-
ence) before the final reading was recorded. Subsequently, more CO₂ was introduced to attain a higher pressure and the new reading was recorded after equilibrium. Thus, solubility isotherms (without swelling correction) as a function of pressure were obtained.

Optical Cell. A high-pressure optical cell used for swelling measurements is shown in Fig. 2. The cell can be used at temperatures up to 473 K and pressures up to 35 MPa. The inner volume of the cell was 20 ml. The temperature of the cell was controlled within 0.1 K using an oil bath. CO₂ was pumped to the cell at elevated pressures using an HPLC pump. A small glass cuvette having a square cross section was used for holding a polymer sample. In the cuvette, the swelling of the polymer occurred only in one direction as the other directions were confined by the walls of the cuvette as shown in Fig. 2. The swelling of the polymer was viewed through a quartz window of the optical cell. A cathetometer having a precision of 0.01 mm was used to measure the difference in the height of the sample from which a fractional change in the volume of the polymer was calculated.

Here, the change in the volume of the polymer sample is termed as fractional swelling, \( \Delta V/V_0 \). \( \Delta V \) and \( V_0 \) are the increment in the volume of the polymer sample due to swelling and the volume of the polymer sample in the absence of dissolved CO₂, respectively.

It can be seen from Eq. 1 that the data obtained using an MSB are not sufficient to calculate the solubility. Therefore, swelling measurements were carried out separately. For these measurements, a sample was prepared by pouring a molten polymer into a mould having a shape similar to the cuvette. After weighing the molded sample, it was fitted into the cuvette. The sample was again heated slightly above its \( T_g \) and pressed against the cuvette walls by a metal rod. The cylinder was then kept inside the cell and was heated to the desired temperature for about 3 h. Subsequently, the polymer surface was marked with a cathetometer followed by the addition of CO₂ to the desired pressure. Due to a rapid initial swelling, it was difficult to mark the surface immediately after the addition of CO₂ with the cathetometer. Pressure–volume–temperature (PVT) data of the polymer (i.e., specific volume of the polymer) were used to correct the initial cathetometer reading. The sample was then allowed to attain equilibrium. As the sorption equilibrium was reached, no further swelling of the polymer occurred. Then, the new surface was marked with the cathetometer. The difference in the sample volume was used to calculate the swelling of the polymer. For subsequent measurements at higher pressures, an additional amount of CO₂ was introduced stepwise and a similar procedure was adopted.

The PVT data of the polymers were obtained using a high-pressure GNOMIX PVT apparatus (DatapointLabs, USA) for a temperature range from 317 to 473 K and pressures up to 40 MPa. The PVT data of CO₂ were obtained from the Span and Wagner EOS [11].

Sanchez–Lacombe Equation of State. To predict the solubility of CO₂ at equilibrium conditions, the S-L EOS was used. Measured solubilities of sub- and supercritical CO₂ in various polymers have successfully been correlated to the S-L EOS [6–8]. According to this theory, the polymer molecules are ordered according to a lattice structure. The theory accounts for the change in volume due to the presence of “holes” in the lattice, and hence, it does not require separate parameters to account for the flexibility of the molecule. The S-L EOS is given by:

\[
\rho^2 + P + T \left[ \ln(1 - \rho) + (1 - 1/r)\rho \right] = 0 \tag{2}
\]

\[
\dot{\nu} = 1/\rho \tag{3}
\]

where \( \rho, \dot{\nu}, P, T \) and \( r \) are the reduced density, specific volume, pressure, temperature, and the number of the lattice sites occupied by a molecule, respectively. An assumption used in the S-L EOS is that the polymer is monodisperse. The reduced parameters are defined as
\[ \hat{\rho} = \rho / \rho^* \]

\[ \hat{v} = v / v^* \]

\[ \bar{P} = P / P^* \]

\[ \bar{T} = T / T^* \]

\[ r = M^* / R T^* \rho^* \]

where \( \rho^* \) (the corresponding mass density in the close-packed state at 0 K), \( v^* \) (the corresponding specific volume in the close-packed state), \( P^* \) (the hypothetical cohesive energy density in the close-packed state), and \( T^* \) (related to the depth of the potential energy well) are the characteristic parameters of components. These parameters are obtained by fitting PVT data of pure components using Eqs. 2–4 [12].

The EOS used for a mixture is similar to Eq. 2. The characteristic parameters used in the EOS for a mixture are obtained using the following mixing rules.

\[ P^* = \sum_i \sum_j \phi_i \phi_j P_{ij}^* \]

\[ P_{ij}^* = (1 - k_{ij})(P_i^* P_j^*)^{0.5} \]

\[ T^* = P^* \sum_i (\phi_i T_i^*) / P_i^* \]

\[ r_i^0 v_i^* = r_i v_i^* \]

\[ v^* = \sum_i \phi_i v_i^* \]

\[ 1 / r = \sum_i \phi_i / r_i \]

\[ \phi_i = (\phi_i P_i^* T_i^*) / \sum_j (\phi_j P_j^* T_j^*) \]

\[ \phi_i = (w / \rho_i) / \sum_j (w / \rho_j) \]

where \( \phi \) and \( w \) represent the volume and weight fraction of components in two phases, respectively. Superscript “0” denotes the pure state of a component. Along with Eqs. 1–12, the chemical potential (\( \mu \)) of a component in the available phases is used to predict the solubility of \( \text{CO}_2 \) in a polymer. At equilibrium,

\[ \mu_{i \text{gas}} = \mu_i^{\text{polymer}}. \]

Here, \( \text{CO}_2 \) is termed as component “1” while a polymer as component “2.” The chemical potential of 1 in the polymer phase is given by

\[ \mu_i^{\text{polymer}} = RT [\ln \phi_i + (1 - r_i / r) \phi_2 + \rho_i \hat{\rho}_2 \phi_2 (P_i^* + P_2^* - 2 P_{ij}^*) (P_i^* T_i^*)] + \hat{\rho}_i \hat{\rho}_1 \phi_1 T_i^* + \hat{\rho}_1 \phi_1 \hat{\rho}_1 \phi_2 T_1^* + \hat{\rho}_i \hat{\rho}_2 \phi_1 T_1^* \]

Equation 14 is also used to calculate \( \mu_{i \text{gas}} \) by considering only the gas phase. For polymers of high molecular weight, it is safe to assume that no polymer is present in the gas phase. Thus, the experimental solubility data are regressed with an adjustable interaction parameter, \( k_{ij} \), which measures the deviation of \( \mu_{i \text{gas}} \) from the geometric mean of \( P_i \) and \( P_j \) using Eqs. 2–14.

**RESULTS AND DISCUSSION**

The PVT data of the polymers and \( \text{CO}_2 \) are essential for the interpretation of the swelling measurements and in the S-L EOS as discussed above. Therefore, the PVT and swelling studies are described before the solubility results. The PVT data have been successfully modelled using the S-L EOS for a wide range of temperatures, pressures, and densities. The results for \( \text{CO}_2 \), PPB, and PEB are shown in Figs.
3, 4, and 5, respectively. The characteristic parameters of the pure components, obtained using the S-L EOS are given in Table 2. These parameters have been used to calculate the solubility.

When CO2 is dissolved into a polymer, the mobility of the polymer chains is increased due to disentanglement of the polymeric chains. As a result, the free volume inside the polymer is increased and swelling of the polymer takes place. Experimentally obtained swelling isotherms of PPB and PEB in the presence of CO2 using the optical cell apparatus are shown in Figs. 6 and 7, respectively. It can be seen from these figures that the fractional swelling is increased with increasing pressure for both PPB and PEB. In general, the higher the dissolved amount of CO2 in a polymer the larger is the swelling of the polymer. This effect is the result of increasing CO2 density upon an increase in pressure. Since the CO2 density decreases with temperature, a reduction in the swelling is expected at higher temperatures in both polymers. However, this is observed only for PPB. The swelling of PEB increases with increasing temperature. This inverse swelling behavior has also been reported for poly (dimethyl siloxane) (PDMS), poly (ethylene-terephthalate) (PET), and bisphenol-A polycarbonate (PC) [13, 14].

CO2 solubilities in both polymers have been measured and have correlated with the S-L EOS. The results are shown in Figs. 8 and 9. The experimental data from the MSB are corrected for buoyancy effects using the results of the swelling measurements. The CO2 solubility is represented in terms of the weight fraction of CO2 dissolved in the polymer. The solubilities of CO2 have been corrected with the experimental swelling data. For both polymers, it is found that the solubility increases with increasing pressure, whereas it decreases with increasing temperature. This relates to high CO2 densities at high pressures and low temperatures, and vice versa. At a low temperature, around 333 K, the solubility behavior is not linear above 15 MPa for both polymers. Probably at elevated pressures, the free volume available in the polymer is reduced due to compression of the polymer. Such effects are more pronounced at the low temperature due to relatively small free volume. Moreover, Figs. 8 and 9 also show that this nonlinear behavior is absent at high temperatures.

The CO2 solubilities in PPB are higher than that in PEB. The importance of the free volume available in the polymer [15] and minor changes in the groups present in a polymer [16, 17] for the CO2 solubility has already been discussed in the literature. As the structure is nearly similar for both polyesters, the accessible free volume in PEB that is smaller

<table>
<thead>
<tr>
<th>Component</th>
<th>$P^*$ (MPa)</th>
<th>$T^*$ (K)</th>
<th>$\rho^*$ (kg/m$^3$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>CO2</td>
<td>427.7</td>
<td>338.7</td>
<td>1405.5</td>
</tr>
<tr>
<td>PPB</td>
<td>439.7</td>
<td>683.2</td>
<td>1242.7</td>
</tr>
<tr>
<td>PEB</td>
<td>640.2</td>
<td>728.6</td>
<td>1271.0</td>
</tr>
</tbody>
</table>

TABLE 2. Characteristic parameters of the polymers and CO2 obtained using the S-L EOS.
due to higher chain entanglements (high molecular weight) is responsible for different solubility. The higher chain entanglements compared to PPB make CO$_2$ more difficult to access the carboxyl groups in PEB than in PPB. Albeit the swelling increases with an increase in temperature in PEB, the low CO$_2$ densities at high temperatures reduce the solubility.

The solubility results have been correlated with the S-L EOS for both PPB and PEB (see also Figs. 8 and 9) respectively. To fit the S-L EOS to the experimental solubility data, Eqs. 2–14 have been solved using the characteristic parameters determined from the PVT data (Table 2). A nonlinear regression optimization procedure (Levenberg-Marquardt, MATLAB 7) has been used for minimizing the difference between the chemical potential of CO$_2$ in the gas phase and the polymer phase, and also between the experimental and predicted solubilities using the interaction parameter, $k_{12}$. It can be seen from Figs. 8 and 9 that the S-L EOS is a good tool for predicting the CO$_2$ solubility in PPB and PEB. Though the S-L EOS has already been reported for several polymers to predict the swelling due to dissolved CO$_2$, it has not been tested together with the experimental swelling and solubility data for molten polymers. The density of a mixture can be determined using the S-L EOS, which has been used to predict the swelling of both polymers. The swelling has been poorly predicted by this EOS for PPB and PEB. The linear mixing rule for the volume of the mixture in the S-L EOS may be responsible for this poor predictability. Royer et al. [13] have introduced a correction parameter in the mixing rule used for the volume in the S-L EOS to predict the swelling of and the solubility of CO$_2$ in PDMS. Recently, over prediction of swelling using the S-L EOS has been reported for EVA polymers by Jacobs et al. [18].

**CONCLUSIONS**

The solubilities of CO$_2$ in PPB and PEB in the molten state have been measured using the MSB. It appeared to be necessary to correct the data obtained from the MSB with independent swelling data. The polymers swell considerably in the presence of CO$_2$ when they are exposed to elevated pressures. The CO$_2$ solubility in the polymers increases with an increase in pressure and decreases with an increase in temperature. The CO$_2$ solubility in PEB is lower than that in PPB, which is probably due to its smaller accessible free volume as a result of the higher molecular weight. Around 333 K, a nonlinear trend for solubility–pressure has been observed at elevated pressures for both polymers due to compression effect. The experimental solubility data have been correlated with the S-L EOS using the pure component parameters and an adjustable interaction parameter. Although the S-L EOS has often been used to predict the swelling of a polymer in the presence of CO$_2$, it is not valid for the polymers investigated here.

**ACKNOWLEDGMENTS**

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**REFERENCES**


**FIG. 8.** The CO$_2$ solubility isotherms of PPB. $k_{12}$ ((•) 333 K) = 0.065, $k_{12}$ ((■) 368 K) = 0.09, and $k_{12}$ ((▲) 420 K) = 0.108. Solid symbols and solid lines denote the experimental data and the data predicted using S-L EOS, respectively.

**FIG. 9.** The CO$_2$ solubility isotherms of PEB. $k_{12}$ ((•) 334 K) = 0.091, $k_{12}$ ((■) 373 K) = 0.083, and $k_{12}$ ((▲) 418 K) = 0.119. Solid symbols and solid lines denote the experimental data and the data predicted using S-L EOS, respectively.