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## Symmetries in string theory

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Rijksuniversiteit Groningen

# Symmetries in String Theory

Proefschrift

ter verkrijging van het doctoraat in de  
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op gezag van de  
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door

Harm Jan Hugo Boonstra  
geboren op 21 mei 1969  
te Groningen

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