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Multi-level ILU preconditioners and continuation methods in fluid dynamics

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Multi-level ILU preconditioners and
continuation methods in fluid dynamics

Rijksuniversiteit Groningen

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