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## Statistical Auditing and the AOQL-method

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*Document Version*

Publisher's PDF, also known as Version of record

*Publication date:*

2005

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*Citation for published version (APA):*

Talens, E. (2005). *Statistical Auditing and the AOQL-method*. s.n.

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
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# Statistical Auditing and the AOQL-Method

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Publisher: Labyrint Publications  
P.O. Box 334  
2984 AX Ridderkerk  
The Netherlands  
Tel: 0180-463962

Printed by:  Offsetdrukkerij Ridderprint B.V., Ridderkerk

ISBN 90-5335-0497

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Rijksuniversiteit Groningen

STATISTICAL AUDITING AND THE AOQL-METHOD

Proefschrift

ter verkrijging van het doctoraat in de  
Economische Wetenschappen  
aan de Rijksuniversiteit Groningen  
op gezag van de  
Rector Magnificus, dr. F. Zwarts,  
in het openbaar te verdedigen op  
donderdag 28 april 2005  
om 14.45 uur

door

Erik Talens  
geboren op 12 september 1970  
te Aduard

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