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Theory and history of geometric models

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RIJKSUNIVERSITEIT GRONINGEN

Theory and History of Geometric Models

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Cover: illustration of the plaster model of the Clebsch diagonal surface,
by the sculptor Cayetano Ramírez López.

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