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Seven-branes and instantons in type IIB supergravity

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Seven-branes and Instantons in Type IIB Supergravity

JELLE HARTONG

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