Open-Loop Magnetic Actuation of Helical Robots using Position-Constrained Rotating Dipole Field

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Abstract—Control of tetherless magnetically actuated helical robots using rotating dipole fields has a wide variety of medical applications. The most promising technique in manipulation of these robots involves a rotating permanent magnet controlled by a robotic manipulator. In this work, we study the open-loop response of helical robots (in viscous fluids characterized by low Reynolds numbers) in the presence of position constraints on the actuating rotating permanent magnet. We first derive a mapping between the space of the manipulator’s joints, the produced magnetic fields in three-dimensional space, and the translational and rotational velocities of the helical robot. Then, we constrain the 3D position of the rotating dipole field and predict the response of the helical robot by controlling its angular velocity using the constrained mapping. We demonstrate open-loop control and gravity compensation of the robot using the angular velocities of the actuating permanent magnet while enforcing constraints on the end-effector position.

I. INTRODUCTION

Over the past decade, robots at the nano- and micro-scales have shown potential to revolutionize medicine by reaching regions inaccessible to catheterization [1]–[4]. The locomotion of these tetherless devices capitalizes on the conversion of several forms of energies into mechanical energy or movement. Magnetic [5], [6], acoustic [7], chemical [8], electric [9], thermal [10], and light [11] energy have been utilized to actuate structures fabricated specifically to work upon sensing one, or a combination [12], of these external stimuli. Once the relation between the external energy and the behavior of the stimuli-responsive material in the fabricated structures is understood, a locomotion strategy is designed to work based on the environment and the potential application. For example, rolling or tumbling on a solid boundary [13], [14], swimming using the drag-based thrust [15], and pulling with a force [16] have been proven to be efficient locomotion strategies. The form of energy and the locomotion strategy must be selected specifically based on the physical surroundings, intended application, and the localization strategy. In practice, magnetic actuation using the drag-based thrust of helical microrobots is efficient under a wide range of Reynolds numbers (Re). In this case, it is reasonable to power these microrobots using actuating time-varying magnetic field produced by rotating permanent magnets fixed to the end-effector of a manipulator [17], as shown in Fig. 1. Scalability and adaptability are two direct consequences of the fact that the displacement of the actuating permanent magnet can be fully controlled in three-dimensional (3-D) space. First, the size of the workspace is no longer limited by the projection distance of the magnetic field, but rather depends on the relatively large workspace of the manipulator. Second, the configuration of this permanent magnet-based robotic system can be adapted to incorporate important functionalities like non-invasive imaging systems [18].

It has been shown that when a magnetic dipole, is rotated around a fixed axis such that the dipole is perpendicular to
the axis of rotation, the magnetic field vector at every point in space also rotates around a fixed axis [17]. Mahoney et al. have reformulated this phenomenon using linear algebraic techniques, which enables finding the necessary dipole rotation axis that is required to make the magnetic field at any desired point in space rotate about any desired axis [17]. Such method has been tested using a rotating permanent magnet fixed in space by a robotic manipulator to control the displacement of the magnet, and actuation of capsule endoscopes, helical swimmers, and spherical agents have been demonstrated inside fluid-filled confined environments. They have also demonstrated closed-loop control of three degree-of-freedom (3-DOF) and 2-DOF open-loop directional control of a magnetic capsule endoscope based on position feedback only [19]. These control results are implemented in the absence of constraints on the displacement of the actuating dipole field or the robotic manipulator. In this paper, we control the motion of helical robots inside a viscous fluid in 3-D space using a rotating magnetic field produced by an actuating permanent magnet fixed to a robotic manipulator. We demonstrate the ability of the system to control the motion of the helical robot in the presence of a position constraint on the end-effector. We focus on changing the actuation axis of the rotating dipole field while keeping the magnet position fixed over time to follow a prescribed path whilst compensating for gravity in an open-loop way.

II. MODELING OF HELICAL PROPULSION AND MAGNETIC ACTUATION

In low-Re, the response of the robot to an externally applied magnetic field is governed by balance between magnetic, viscous drag, and gravitational forces and torques.

A. Helical Propulsion in Low-Re

Suppose we consider a helical body with length \( L \) and magnetic moment \( \mathbf{m} \) perpendicular to its helix axis, immersed in a viscous fluid, with density \( \rho_i \), characterized by low-Re and actuated using non-uniform magnetic field, \( \mathbf{B} \), as shown in Fig. 2. In low-Re, inertial forces are negligible and the motion of helical robot is governed by

\[
\begin{align*}
\mathbf{f}_{\text{visc}} + \mathbf{f}_{\text{mag}} + \mathbf{f}_{g} &= 0 \quad (1) \\
\mathbf{T}_{\text{visc}} + \mathbf{T}_{\text{mag}} + \mathbf{T}_{g} &= 0, \quad (2)
\end{align*}
\]

where \( \mathbf{f}_{\text{visc}} \) and \( \mathbf{T}_{\text{visc}} \) are the viscous drag force and torque, respectively. Further, \( \mathbf{f}_{\text{mag}} \) and \( \mathbf{T}_{\text{mag}} \) are the magnetic force and torque, respectively. Furthermore, \( \mathbf{f}_{g} \) and \( \mathbf{T}_{g} \) are the force and torque due to gravity, respectively. One direct consequence of the negligible inertia force is that the hydrodynamics is linear. Therefore, the viscous drag force and torque are given by

\[
\begin{pmatrix} 
\mathbf{f}_{\text{visc}} \\
\mathbf{T}_{\text{visc}} 
\end{pmatrix} = 
\begin{pmatrix} 
\mathbf{A} & \mathbf{B} \\
\mathbf{B}^T & \mathbf{C} 
\end{pmatrix} 
\begin{pmatrix} 
\mathbf{U} \\
\mathbf{\omega} 
\end{pmatrix}, \quad (3)
\]

where \( \mathbf{U} \) and \( \mathbf{\omega} \) are the translational and angular velocity of the helical body due to the external force and torque, respectively. In Equation (3) the sub-matrices \( \mathbf{A}, \mathbf{B}, \) and \( \mathbf{C} \) are calculated using the Resistive-Force Theory and are only dependent on the viscosity, \( \eta_i \), of the medium and the geometry of the helical body [15]. In Equations (1)-(2), the magnetic force, \( \mathbf{f}_{\text{mag}}(\mathbf{p}) \), and torque, \( \mathbf{T}_{\text{mag}}(\mathbf{p}) \) at point, \( \mathbf{p} \), are given by

\[
\begin{align*}
\mathbf{f}_{\text{mag}}(\mathbf{p}) &= (\mathbf{m} \cdot \nabla)\mathbf{B}(\mathbf{p}) \quad (4) \\
\mathbf{T}_{\text{mag}}(\mathbf{p}) &= \mathbf{m} \times \mathbf{B}(\mathbf{p}). \quad (5)
\end{align*}
\]

Finally, in Equations (1)-(2) the force, \( \mathbf{f}_{g} \), and torque, \( \mathbf{T}_{g} \), exerted on the helical robot due to gravity are given by

\[
\begin{align*}
\mathbf{f}_{g} &= V(\rho_i - \rho_l)\mathbf{g} \quad (6) \\
\mathbf{T}_{g} &= (\mathbf{r}_{\text{cov}} - \mathbf{r}_{\text{com}}) \times \mathbf{f}_{g}, \quad (7)
\end{align*}
\]

where \( V \) is the volume the robot, \( \rho_i \) and \( \rho_l \) are its density and the density of the fluid, respectively. Furthermore, \( \mathbf{g} \) signifies gravity, \( \mathbf{r}_{\text{cov}} \) and \( \mathbf{r}_{\text{com}} \) are the position vectors of the center of volume and center of mass, respectively. These force and torque complete the relation between the external forces and torques and the resulting velocities \( \mathbf{U} \) and \( \mathbf{\omega} \) of the robot.

B. Rotating Actuating Magnetic Fields

Equations (1)-(3) show the velocities of the helical robots can be directly determined from the balance between magnetic force, force due to gravity, and viscous drag. The magnetic force and torque are directly affected by the actuating magnetic field, \( \mathbf{B}(\mathbf{p}) \), which is given by the following point-dipole approximation:

\[
\mathbf{B}(\mathbf{p}) = \frac{\mu_0}{4\pi} \left( \frac{3pp^T}{||p||^3} - \frac{I}{||p||^3} \right) \mathbf{M}(\mathbf{q}), \quad (8)
\]

where \( \mu_0 = 4\pi \times 10^{-7} \text{ N.A}^{-2} \) is the permeability of free space, \( \mathbf{M} \in SO(3) \) is the dipole moment of the actuator magnet and \( I \in \mathbb{R}^{3 \times 3} \) is the identity matrix. Equation (8) gives the magnetic field at the position of the robot, \( \mathbf{p} \), when the permanent magnet is fixed at \( \mathbf{x} \in \mathbb{R}^3 \). Note that the magnetic field at a point, \( \mathbf{p} \), is controlled by the joints of the manipulator.
Fig. 3: The magnetic field at a point, $p$, from the actuator magnet varies with the joint variables of the robotic manipulator $(q_1, \ldots, q_6)$. The coordinates $x$, $y$, and $z$ characterize the position of the actuator magnet in the manipulator frame of reference, and the angles $\alpha$, $\beta$, and $\gamma$ characterize the orientation $R$.

The configuration-to-pose kinematics of the robotics manipulator is given by [20]

$$\{x, R\} = \mathcal{F}(q), \quad (9)$$

where $\mathcal{F} : \mathbb{R}^n \to \{\mathbb{R}^3, SO(3)\}$ is the forward kinematic mapping and $q \in \mathbb{R}^n$ is the joint variables. Equations (8) and (9) provide the relation between the magnetic field at a point, $p$, and the configuration of the robotic manipulator. Fig. 3 shows the magnetic field at a point calculated using Equation (8) and the corresponding position and orientation of the end-effector for a time-varying joint variables. It is convenient to represent the composed linear and angular velocities of the end-effector by the joint velocity, we have

$$\begin{pmatrix} \dot{x} \\ \Omega \end{pmatrix} = J_m(q) \dot{q}, \quad (10)$$

where $J_m \in \mathbb{R}^{n \times n}$ is the manipulator Jacobian.

Mahoney and Abbott have shown that the velocity level kinematics (10) can also be modified to include the contribution of the magnetic moment of the actuator magnet using $M = \Omega \times M$, and we obtain [19]

$$\begin{pmatrix} \dot{x} \\ \dot{\Omega} \end{pmatrix} = \begin{pmatrix} I & 0 \\ 0 & SK(M) \end{pmatrix} J_m(q) \dot{q} = J_A(q) \dot{q}, \quad (11)$$

where $SK(\cdot) : \mathbb{R}^3 \to SO(3)$ is the skew-symmetric operator of the cross product and $J_A \in \mathbb{R}^{n \times n}$ is the actuator permanent magnet Jacobian. Equation (11) completes the relation between the joint velocities of the manipulator and the helical robot velocity, composed by the linear velocity $U$ and the angular velocity $\omega$.

C. Actuation using Pose-Constrained Dipole Field

To test the helical propulsion under a position constraint on the actuator magnet, we shall invoke $\dot{x} = 0$ into Equation (12), which yields

$$\begin{pmatrix} 0 \\ \Omega \end{pmatrix} = \begin{pmatrix} J_{11}^{12}(q) \\ SK(M) J_{12}^{12}(q) \end{pmatrix} \begin{pmatrix} J_{m1}(q) \\ SK(M) J_{m2}(q) \end{pmatrix} \dot{q}, \quad (12)$$

where $J_{11}^{12}(q)$, $J_{m1}(q)$, $J_{12}^{12}(q)$, and $J_{m2}(q)$ are the sub-matrices of the geometric Jacobian. Equations (12) maps the joint velocities into angular velocity of the actuator magnet without translation. If the translation and rotation of the actuator magnet are kept constant (Fig. 4), then the helical robot will ultimately align along the magnetic field $B(p)$. In this case, the magnetic field rotation axis, $\Omega_a$, and the actuator magnet’s rotation axis, $\Omega_a$, are given as $\Omega_a = \mathbf{H} \hat{\omega}_i$, where $\mathbf{H} = 3 p \hat{p}^T - I$. Therefore, the rotation axis of the magnetic field varies with the position of the helical robot with respect to the actuator magnet, $p$, and it is not possible to maintain the swimming direction along a straight line (along the x-axis). The angular velocity of the
actuator magnet must be controlled using Equation (12) to orient the rotation axis of the magnetic field parallel to the x-axis and enable forward swimming.

III. EXPERIMENTAL RESULTS

Open-loop motion control experiments are conducted using the permanent magnet-based robotic system shown in Fig. 1 to drive the robot along a prescribed path while enforcing a constraint on the end-effector, as shown in Fig. 5.

A. System Description

Our system consists of a 6-DOF serial manipulator (KUKA KR-1100-2, KUKA, Augsburg, Germany) to control the displacement of the rotating disc permanent magnet. The magnet (NdFeB Grade-N45) has a diameter of 35 mm, height of 20 mm, and is axially magnetized. The magnetic flux density of the actuator magnet is measured using a SENIS 3-axis digital Teslameter at varying distance, p. The magnitude of the dipole moment $|\mathbf{M}|$ is determined using a least squares solution for the point-dipole model. In this experiment, 50 samples of the flux density are measured between 40 mm and 100 mm from the center of the magnet, resulting in $|\mathbf{M}| = 18.89 \text{ A.m}^2$.

The disc magnet is actuated by a Maxon 18V brushless DC motor with Hall-effect sensors, encoder and a planetary gearbox with gear ratio of 3.7:1. The motor is controlled using an EPOS4 Compact 50/5 CAN, digital position controller.

The continuous rotation of the permanent magnet enables the robot to achieve helical propulsion. The kinematics and the Denavit-Hartenberg parameters from the base frame to the end-effector and to the actuator magnet frames of reference are provided in Appendix A.

The robot consists of a cylindrical permanent magnet (NdFeB Grade-N52) with diameter of 1 mm and height of 1 mm, attached to a helical body such that the helix axis is perpendicular to the dipole moment. The helix has length, pitch and radius of 11.7 mm, 3 mm and 0.6 mm, respectively. The robot is immersed in silicon oil (reservoir of dimensions 100 mm $\times$ 100 mm $\times$ 50 mm) with density of $\rho_f = 970$ kg/m$^3$ and viscosity of $\eta = 1$ Pa.s. Motion of the robot is measured using two FLIR Blackfly cameras in the x-y and x-z plane. Both cameras are fitted with Fujinon lens of 6 mm fixed focal length producing sub-millimeter tracking accuracy at 60 frames per second.

The entire system is programmed and modeled through Matlab Interface (Version R2020a). To achieve real-time control of the robotic manipulator, a connection between RoboDK (RoboDK Inc., Montreal, Canada) and the robotic manipulator was established to move it automatically using RoboDK’s user interface. The connection was established through a standard Ethernet connection (TCP/IP).

For this purpose, a KUKAVARPROXY (Imts Srl, Taranto, Italy) server was installed on the KRC4 controller (KUKA,
Fig. 6: Experimental motion control result demonstrates swimming under the influence of a rotating field produced by a constrained actuating magnet. The robot swims in silicone oil ($\rho = 971$ kg/m$^3$ and $\eta = 1$ Pa.s) at an average speed of $U = 0.98$ mm/s and has Reynolds number of $Re = 10^{-3}$. Maximum swimming speed is achieved at $t = 17$ seconds when the robot swims toward the permanent magnet and the magnetic force contributes to its propulsive thrust.

Augsburg, Germany) of the robotic manipulator. This server allows the global variables from the robotic arm controller to be exchanged with the remote RoboDK’s user interface.

B. Open-Loop Control of the Helical Robot

To control the helical robot along a desired path it is critical to select the appropriate rotation axis $\tilde{\omega}_l$ of the magnetic field. When the robot swims away from the nearby solid boundary and in the absence of any interactions, its rotation axis aligns with $\tilde{\omega}_l$. Therefore, it is convenient to steer the helical robot by controlling $\tilde{\Omega}_a$. In addition, the rotation axis of the magnetic actuator can be determined using the prescribed trajectory of the desired path such that $\tilde{\omega}_l$ and the local tangent are perpendicular.

Fig. 5 shows a representative open-loop control result of the helical robot along a straight line along the x-axis. Therefore, the rotation axis of the magnetic field, $\tilde{\omega}_l$, is made parallel to the x-axis, while the constraint on the position of the actuating permanent magnet is enforced using Equations (12). In this experiment, the robot swims at a maximum swimming speed of $U = 1.43$ mm/s at actuation frequency of 5 Hz. The step-out frequency of the robot is 12 Hz. Therefore, the swimming speed of the robot can be controlled by increasing the actuation frequency of the magnetic field below the step-out frequency. In this case, the angular velocity of the rotating dipole field will depend on the linear velocity of the robot based on Equations (1)-(8).

The swimming path of the helical robot is shown in the x-y and x-z planes. This experimental result shows that associated with the translational motion of the helical robot is a continuous change in the angular velocity of the actuator magnet, as shown using the representative configurations of the robotic manipulator at $t = 0$, $t = 22$, and $t = 40$ seconds. The helical robot swims at an average velocity of 0.98 mm/s along the x-axis and 0.15 mm/s along the y-axis, as shown in Fig. 6. The average speed of the robot along the z-axis is 0.3 mm/s. For $0 < t \leq 20$ seconds, the forward swimming speed of the robots increases as the distance to the actuator magnet decreases. At $t > 20$ seconds, the swimming speed decreases at the same rate as the gap with the actuator magnet increases.

IV. CONCLUSIONS AND FUTURE WORK

Magnetic actuation of helical robots is achieved using a rotating dipole field in the presence of a constraint on its position. We derive the mapping between the robot velocity, composed by linear and angular velocity, and the joint velocities of the robotic manipulator which fix the constrained
rotating permanent magnet. The helical robot is actuated in a viscous fluid characterized by low-Re using rotating magnetic fields produced by a permanent magnet fixed in space by the robotic manipulator. Our experimental results demonstrate the capability to actuate the robot controllably and compensate for its gravity by controlling the angular velocities of the constrained actuator magnet.

As part of future work, we will implement closed-loop control of the helical robot in 3-D space in the presence of position constraint on the actuator magnet. In addition, we will modify our permanent magnet-based robotic system to actuate the helical robots using two synchronized rotating dipole fields [22]. In the current study, we have demonstrated radial actuation and gravity compensation by the pulling magnetic force of the actuator magnet. To achieve closed-loop motion control in 3-D space, we will mitigate the pulling magnetic forces along the lateral directions of the robots using two synchronized actuating magnets.

REFERENCES