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Bayesian model determination in complex systems

Mohammadi, Abdolreza

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Summary

In this thesis, we address several problems related to modeling complex systems. The difficulty of modeling complex systems lies partly in their topology and how they form rather complex networks. From this perspective, our interest in networks (graphs) is part of a broader current of research on complex systems.

Graphical models provide powerful tools to model and make statistical inference regarding complex relationships among variables. In this context, Gaussian graphical models are commonly used, since inference in such models is often tractable. In Chapter 2, we introduce a novel Bayesian framework for Gaussian graphical model determination. We carry out the posterior inference by using an efficient sampling scheme which is a trans-dimensional MCMC approach based on birth-death process. In particular, we construct an efficient search algorithm which explores the graph space to detect the underlying graph with high accuracy. We cover the theory and computational details of the proposed method. We then apply the method to large-scale real applications from mammary gene expression studies to show its empirical usefulness.

The method that we propose in chapter 2 is limited only to the data that follows the Gaussianity assumption. In Chapter 3, we propose a Bayesian approach for graphical model determination based on a Gaussian copula approach that can deal with continuous, discrete, or mixed data. We embed a graph selection procedure inside a semi-parametric Gaussian copula. We implement our approach to discovering potential risk factors related to Dupuytren disease.

In chapter 4, we introduce an R package `BDgraph` which efficiently performs the Bayesian approaches that proposed in chapters 2 and 3. The core of the `BDgraph` package efficiently implemented in C++ to maximize computational speed.

The most promising statistical model that can be used for network modelling is the class of Exponential Random Graph Models (ERGMs). However, they are restricted to the models that regarded the network as given. In chapter 5, we develop a novel Bayesian statistical framework which combines the class of ERGMs with graphical models capable of modelling non-observed networks. Our proposed method greatly extends the scope of

the ERGMs to more applied research areas.

In chapter 6, we introduce a Bayesian framework in an $M/G/1$ queuing system with an optional second service. We estimate system parameters, predictive densities and some performance measures related to this queuing system such as stationary system size and waiting time.

Samenvatting

In dit proefschrift bekijken we een aantal problemen met betrekking tot het modelleren van complexe systemen. De moeilijkheid in het modelleren van complexe systemen ligt deels in hun topologie en deels in hoe ze tamelijk complexe netwerken vormen. Onze interesse in netwerken (grafan) is onderdeel van een bredere beweging in de richting van onderzoek naar complexe systemen.

Na de introductie, in hoofdstuk 2, introduceren we een nieuw Bayesiaans kader voor Gaussische grafische modelbepaling, namelijk een trans-dimensionale Markov Chain Monte Carlo (MCMC) aanpak op basis van een continue-tijd geboorte-dood-proces. We behandelen de theorie en computationele details van de voorgestelde methode. Vervolgens passen we de methode toe op borstklier genexpressie studies om zijn empirische nut tonen.

De werkwijze die we in hoofdstuk 2 voorstellen is beperkt tot de gegevens die de Gaussiaanse aanname volgt. In hoofdstuk 3 introduceren we een Bayesiaanse aanpak gebaseerd op de Gaussiaanse copula benadering die tegelijkertijd met binaire, gewone of continue variabelen kan werken. We verwerken een grafische selectieprocedure binnen een semi-parametrische Gaussische copula. Wij passen een posterieure inferentie toe door gebruik te maken van een efficiënt bemonsteringsschema: een trans-dimensionale MCMC aanpak op basis van een geboorte-dood-proces. Wij implementeren onze aanpak met als doel het ontdekken van potentiële risicofactoren bij de ziekte van Dupuytren.

In hoofdstuk 4, introduceren we een op R gebaseerd softwarepakket, BDgraph, dat efficiënt de Bayesiaanse benaderingen die in de hoofdstukken 2 en 3 zijn geïntroduceerd uitvoert. De kern van het BDgraph pakket is efficiënt geïmplementeerd in C++ om de rekensnelheid te bevorderen.

De meest veelbelovende statistische modellen die kunnen worden gebruikt voor netwerkmodellering zijn de exponentiële Random Graph Models (ERGMs). Ze zijn echter beperkt tot de modellen die het netwerk als gegeven beschouwen. In hoofdstuk 5 ontwikkelen we een nieuw Bayesiaans statistisch kader, welke de klasse van ERGMs combineert met grafische modellen die in staat zijn niet-waargenomen netwerken te modelleren. Onze voorgestelde methode vergroot het bereik van de ERGMs met meer toegepaste onderzoeks-

gebieden.

In hoofdstuk 6, stellen we een Bayesiaans kader voor in een $M/G/1$ wachtrijsysteem met een optionele tweede dienstverlening (service). Wij schatten parameters van het systeem, voorspellen dichtheden en een aantal prestatie-indicatoren met betrekking tot dit wachtrijsysteem zoals stationaire systeemgrootte en de wachttijd.

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Abdolreza Mohammadi

Groningen

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