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## Bayesian model determination in complex systems

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# Bayesian Model Determination in Complex Systems

**PhD thesis**

to obtain the degree of PhD at the  
University of Groningen  
on the authority of the  
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and in accordance with  
the decision by the College of Deans.

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24 April 2015 at 12.45 hours

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*To my wife and my family*



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