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## Dimensionality assesment with factor analysis methods

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# Dimensionality Assessment with Factor Analysis Methods

by Maria Theodora Barendse

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# Dimensionality assessment with factor analysis methods

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# Contents

<b>1</b>	<b>Introduction</b>	<b>1</b>
<b>2</b>	<b>Exploratory Factor Analysis of Discrete Responses</b>	<b>7</b>
2.1	Introduction . . . . .	8
2.2	Method . . . . .	10
2.2.1	Data Generation: Continuous Responses . . . . .	10
2.2.2	Data Generation: Discrete Responses . . . . .	14
2.2.3	Data Analysis . . . . .	14
2.3	Results . . . . .	17
2.3.1	Continuous Responses . . . . .	17
2.3.2	Discrete Responses . . . . .	21
2.4	Discussion . . . . .	32
	Appendices . . . . .	35
<b>3</b>	<b>Multilevel Exploratory Factor Analysis</b>	<b>67</b>
3.1	Introduction . . . . .	68
3.2	Methods . . . . .	69
3.2.1	Model . . . . .	69
3.2.2	Measurement Invariance . . . . .	70
3.2.3	Identification . . . . .	71
3.2.4	Estimation . . . . .	72
3.2.5	Evaluation of Fit . . . . .	72
3.2.6	Dimensionality Assessment . . . . .	73
3.2.7	Rotation . . . . .	74
3.3	Illustration . . . . .	74
3.3.1	Preliminary Analysis . . . . .	75
3.3.2	Procedure 1: Within-Level Results . . . . .	75
3.3.3	Procedure 1: Between-Level Results . . . . .	75
3.3.4	Procedure 2: Measurement Invariance Results . . . . .	78
3.3.5	Rotation Results . . . . .	78
3.4	Discussion . . . . .	80

<b>4</b>	<b>Model Fit After Pairwise Maximum Likelihood</b>	<b>83</b>
4.1	Introduction . . . . .	84
4.1.1	Weighted Least Squares Method . . . . .	84
4.1.2	Multivariate ML Estimation Method . . . . .	85
4.1.3	Bivariate ML Estimation Method . . . . .	86
4.2	Model Fit Statistics . . . . .	88
4.3	Method . . . . .	90
4.3.1	Data Generation . . . . .	91
4.3.2	Analysis . . . . .	92
4.4	Results . . . . .	92
4.4.1	The $C_F$ Fit Statistic . . . . .	93
4.4.2	The $C_M$ Fit Statistic . . . . .	94
4.4.3	The $C_P$ Fit Statistic . . . . .	94
4.4.4	The $C_W$ Fit Statistic . . . . .	98
4.5	Discussion . . . . .	98
<b>5</b>	<b>Measurement Bias Detection Through Factor Analysis</b>	<b>103</b>
5.1	Introduction . . . . .	104
5.2	Methods . . . . .	106
5.2.1	Data Generation . . . . .	106
5.2.2	Measurement Bias Detection . . . . .	107
5.2.3	Analysis . . . . .	111
5.3	Results . . . . .	112
5.3.1	Measurement Bias Detection . . . . .	112
5.3.2	Estimation Bias . . . . .	117
5.4	Discussion . . . . .	121
	Appendices . . . . .	125
	A Example Script for Fitting the RFA/LMS Model . . . . .	125
	B Example Script for Fitting the RFA/RSP Model . . . . .	126
<b>6</b>	<b>Bayesian Measurement Bias Detection</b>	<b>127</b>
6.1	Introduction . . . . .	128
6.2	Method . . . . .	130
6.2.1	Data Generation . . . . .	131
6.2.2	Bayesian SEM and Bias Detection . . . . .	132
6.2.3	Bayesian Model Selection . . . . .	133
6.2.4	Measurement Bias Detection . . . . .	134
6.2.5	Analysis . . . . .	136
6.3	Results . . . . .	138
6.3.1	Parameter Estimates . . . . .	139
6.3.2	Bias Detection . . . . .	141

6.3.3	Sensitivity Analyses . . . . .	145
6.4	Discussion . . . . .	146
Appendices	. . . . .	149
A	Computation of $\sigma^2$ in Table 6.1 . . . . .	149
B	Specification of Prior Information . . . . .	151
C	Model Specification in Bugs . . . . .	152
<b>7</b>	<b>Summary and Discussion</b>	<b>155</b>
	<b>Bibliography</b>	<b>161</b>
	<b>Summary in Dutch</b>	<b>173</b>
	<b>Curriculum Vitae</b>	<b>179</b>
	<b>List of Publications</b>	<b>180</b>
	<b>Acknowledgements</b>	<b>181</b>



