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Kac-Moody Symmetries and Gauged Supergravity

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Kac-Moody symmetries and gauged supergravity

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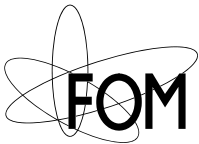
door

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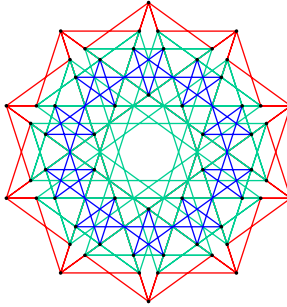
On the cover: the root system of the hyperbolic Kac-Moody algebra E_{10} up to height 124 projected onto the Coxeter plane of a regular E_8 subalgebra.

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