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Ploegh, André René

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# Particle Dynamics of Branes

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ANDRÉ RENÉ PLOEGH



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# Particle Dynamics of Branes

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# Contents

<b>1</b>	<b>Introduction</b>	<b>1</b>
<b>2</b>	<b>String Theory</b>	<b>7</b>
2.1	Classical String Theory . . . . .	7
2.2	Quantization of the Bosonic String and Curved Backgrounds . . . . .	11
2.3	Superstrings and Supergravities . . . . .	14
2.3.1	Supergravities . . . . .	15
2.3.2	T-duality . . . . .	17
2.3.3	S-duality . . . . .	17
2.4	Brane Solutions . . . . .	18
2.4.1	$p$ -branes . . . . .	18
2.4.2	D $p$ -branes . . . . .	21
2.4.3	S $p$ -branes . . . . .	23
<b>3</b>	<b>Dimensional Reduction of Branes</b>	<b>27</b>
3.1	Dimensional Reduction . . . . .	27
3.2	Torus Reduction of Gravity . . . . .	29
3.2.1	Torus Reduction over Time . . . . .	31
3.3	Maximally Symmetric Compactification . . . . .	33
3.4	Coset Geometry . . . . .	36
3.4.1	The Coset $SL(n, \mathbb{R})/SO(n)$ . . . . .	39
3.4.2	Maximally Extended Supergravities . . . . .	41
3.5	From Branes to “Particles” . . . . .	43
<b>4</b>	<b>Massless Time-Dependent Solutions</b>	<b>49</b>
4.1	S(−1)-brane Geometries . . . . .	49
4.2	A Solution-Generating Technique . . . . .	50
4.3	Spacelike Branes . . . . .	52
4.3.1	Pure Gravity . . . . .	53
4.3.2	Dilaton-Gravity . . . . .	55

4.3.3	... with Non-Trivial Flux . . . . .	55
4.4	Discussion . . . . .	59
<b>5</b>	<b>Massive Time-Dependent Solutions</b>	<b>61</b>
5.1	Cosmologies . . . . .	61
5.1.1	Multi-Field Cosmology . . . . .	63
5.1.2	Generalized Assisted Inflation . . . . .	65
5.1.3	The Critical Points . . . . .	68
5.2	First Order Formalism . . . . .	71
5.3	Multi-Field Scaling Cosmologies . . . . .	73
5.3.1	Pure Kinetic Solutions . . . . .	73
5.3.2	Potential-Kinetic Scaling Solutions . . . . .	74
5.4	Uplifts . . . . .	77
5.5	Discussion . . . . .	78
<b>6</b>	<b>Domain-Wall / Cosmology Correspondence</b>	<b>81</b>
6.1	The Domain-Wall / Cosmology Correspondence . . . . .	81
6.2	... in a Supergravity Setting . . . . .	85
6.3	Type II Actions . . . . .	86
6.3.1	The Complex Type II Action . . . . .	87
6.3.2	Back to Reality . . . . .	90
6.3.3	Examples . . . . .	93
6.3.4	Extended vs. Unextended Supersymmetry . . . . .	99
6.4	Reality of the Vielbeine . . . . .	100
6.4.1	Imaginary Vielbeine and Signature Change . . . . .	100
6.4.2	Imaginary Vielbeine without Signature Change . . . . .	102
6.5	Domain-Walls and Cosmologies . . . . .	102
6.5.1	10d Massive IIA/A* . . . . .	103
6.5.2	Maximal Gauged Supergravity in 9d . . . . .	106
6.5.3	E-branes . . . . .	109
6.6	Discussion . . . . .	110
<b>7</b>	<b>Instantons</b>	<b>113</b>
7.1	Instanton Geometries . . . . .	114
7.2	Solutions of Kaluza–Klein Theory . . . . .	116
7.2.1	The Geodesic Curves . . . . .	116
7.2.2	Normal Form of $\mathfrak{gl}(p+q)/\mathfrak{so}(p,q)$ . . . . .	117
7.2.3	Uplift to Vacuum Solutions . . . . .	121
7.3	Massive Instantons . . . . .	124
7.4	Discussion . . . . .	127

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<b>8</b>	<b>Conclusions and Future Research</b>	<b>129</b>
8.1	Summary . . . . .	129
8.2	Future Research . . . . .	130
<b>A</b>	<b>Differential Geometry: Formulae and Conventions</b>	<b>133</b>
A.1	Conventions . . . . .	133
A.2	General Relativity . . . . .	133
A.2.1	Vielbeine . . . . .	136
A.3	Forms . . . . .	137
A.4	Euler-Lagrange Variation . . . . .	138
<b>B</b>	<b>Spinors and their Reality Properties</b>	<b>141</b>
B.1	Clifford Algebras in Various Dimensions and Signatures . . . . .	141
B.2	Reality Conditions for Spinors . . . . .	143
<b>C</b>	<b>Lie Group and Lie Algebra</b>	<b>145</b>
<b>D</b>	<b>Publications</b>	<b>149</b>
	<b>Bibliography</b>	<b>151</b>
	<b>Nederlandse Samenvatting</b>	<b>159</b>
	<b>Dankwoord</b>	<b>167</b>



