Water delivery in the inner solar nebula
Monte Carlo simulations of forsterite hydration

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ABSTRACT

Context. Endogenous or exogenous, dry or wet, various scenarios have been depicted for the origin of water on the rocky bodies in our solar system. Hydrated silicates found in meteorites and in interplanetary dust particles, together with observations of abundant water reservoirs in the habitable zone of protoplanetary disks, are evidence that support aqueous alteration of silicate dust grains by water vapor condensation in a nebular setting.

Aims. We investigate the thermodynamics (temperature and pressure dependencies) and kinetics (adsorption rates and energies, surface diffusion and cluster formation) of water adsorption on surfaces of forsterite grains, constraining the location in the solar nebula where aqueous alteration of silicates by water vapor adsorption can occur efficiently and leads to the formation of phyllosilicates. We analyze the astrophysical conditions favorable for such hydration mechanism and the implications for water on solid bodies.

Methods. The protoplanetary disk model (ProDiMo) code is tuned to simulate the thermochemical disk structure of the early solar nebula at three evolutionary stages. Pressure, temperature, and water vapor abundance within 1 au of the protosun were extracted and used as input for a Monte Carlo code to model water associative adsorption using adsorption energies that resemble the forsterite [100] crystal lattice.

Results. Hydration of forsterite surfaces by water vapor adsorption could have occurred within the nebula lifetime already at a density of 10^3 cm^-2, with increasing surface coverage for higher water vapor densities. Full surface coverage is attained for temperatures lower than 300 K, while for hotter grain surfaces water cluster formation plays a crucial role. Between 0.5 and 10 Earth oceans can arise from the agglomeration of hydrated 0.1 μm grains into an Earth-sized planet. However, if grain growth occurs dry and water vapor processes the grains afterward, this value can decrease by two orders of magnitude.

Conclusions. This work shows that water cluster formation enhances the water surface coverage and enables a stable water layer to form at high temperature and low water vapor density conditions. Finally, surface diffusion of physisorbed water molecules shortens the timescale for reaching steady state, enabling phyllosilicate formation within the solar nebula timescale.

Key words. astrochemistry – protoplanetary disks – molecular processes – Sun: evolution – planets and satellites: oceans – planet-star interactions

1. Introduction

After almost 40 years of study, the origin of Earth’s water is still strongly debated (Drake 2005). One hypothesis is that Earth accreted from a mixture of dry and wet primary building blocks in which water was in the form of hydrous silicates (the wet-endogenous scenario); another view supports dry accretion, with water delivered at a later stage during impact of hydrous asteroidal or cometary bodies (the exogenous scenario).

Direct evidence of aqueous alteration processes in the solar nebula is contained in carbonaceous chondrites (CCs). These “undifferentiated” meteorites are considered primitive solar system objects along with interplanetary dust particles (IDPs) and cometary grains because they show solar composition (Barrat et al. 2012). Depending on the chemical and mineralogical composition and size of the parent body, several classes of CCs are defined (Weisberg et al. 2006). Among them, CI (Ivuna-like) group, CM (Mighei-like) group, and CR (Renazzo-like) carbonaceous chondrites are the most hydrous varieties, with 3%–14% by weight (wt%) of water content in CM and CR, and up to 15 wt% in CI (Alexander et al. 2010). Most of the water in these chondrites is structurally bound in phyllosilicates1 that formed during aqueous alteration of anhydrous minerals (e.g., olivine and pyroxene) very likely on the parent bodies of meteorites (Brearley 2006). Recent mid-IR spectroscopy measurements revealed that the most aqueous altered samples are (−OH)-rich and almost depleted in olivine, the “dry” precursor mineral (Beck et al. 2014).

The high variability in the abundance and in the nature of these hydro-silicates in CCs indicates many levels of aqueous

1 Layered silicate platelets with swelling properties (Schuttlefield et al. 2007).
alteration and suggests different possible origins and evolutions. Most of the models that have been developed over the last 30 years are based on the fluid flow and liquid water-rock interaction on their parent bodies: previously accreted water ice melts, the fluid flows through various mineral matrices of different permeability and reacts with the anhydrous precursor mineral finally forming the hydrated products (see review by Brearley 2006). The chemical composition of phyllosilicates forming by the flow of fluids may be controlled by the composition of the anhydrous precursor mineral and/or the composition of the aqueous solutions (Howard et al. 2011; Velbel et al. 2012).

On the other hand, hydrated silicates could have formed by direct condensation of water vapor within the terrestrial planets forming region. Early models indicated that silicate hydration would be kinetically inhibited in a nebular setting (Fegley & Prinn 1989). Using a simple collision theory (SCT) model and the activation energy of 8420 K (70 kJ mol⁻¹) as the amount of energy required to convert MgO into Mg(OH)₂ (brucite) at 1 atmosphere, they estimated the formation rates of serpentinite and brucite and concluded that formation of hydrous silicates takes too long to occur by nebular condensation (10⁵ times the nebular life time of 10¹³ s). However, Ganguly & Bose (1995) used the same SCT approach and estimated a shorter timescale for the hydration of olivine if a lower activation energy (about 3909 K, i.e., 32.5 kJ mol⁻¹) is assumed in the calculation.

In an attempt to explain the presence of phyllosilicates fine-grained rims (FGRs) in the Murray CM chondrite, Ciesla et al. (2003) draw a scenario where, holding the 8420 K of hydration energy, shock waves pass through an icy region of the nebula and the water vapor partial pressure is locally enhanced, thus increasing the collision rates of water molecules with the bare grains. Therefore, hydrated silicates can form much more quickly than the solar nebula lifetime, allowing a nebular origin of the chondrules and the phyllosilicates components as well. Woitke et al. (2018) consider phyllosilicates in thermo-chemical equilibrium, and found that below 345 K and at one bar, the dominant phyllosilicate is Mg₃Si₂O₅H₂ (lizardite), which replaces Mg₃SiO₅ in chemical + phase equilibrium.

Phyllosilicates can retain water when heated up to a few hundred degrees centigrade (Beck et al. 2014; Davies 1996), being able to preserve structural water also in the inner and warmer regions of a protoplanetary disk. Once agglomerated into planetesimals, phyllosilicates could be a potential source of water for terrestrial planets, in line with the wet-endogenous scenario.

More recent computer simulations have studied water adsorption energy, binding sites, and mechanisms (associative and/or dissociative) on forsterite surfaces and have demonstrated that many Earth oceans could efficiently form in situ under accretion disk conditions (Stimpfl et al. 2006; Muralidharan et al. 2008; King et al. 2010; Asaduzzaman et al. 2013, 2015; Prigibbe et al. 2013). However, these modeling attempts possess some major uncertainties, namely a detailed temperature-pressure structure of the young solar nebula. In the exploratory rate-based warm surface chemistry model of Thi et al. (2018), water from the gas-phase can chemisorb on dust grain surfaces and subsequently diffuse into the silicate bulk. The phyllosilicate formation model was applied to a zero-dimensional chemical model and to a 2D protoplanetary disk model (ProDiMo) to investigate the formation of phyllosilicates in protoplanetary disks.

In this work we tested the possibility of water vapor condensation on bare forsterite grains in the region of the terrestrial planets prior to their accretion into planetesimals. In the endogenous scenario, we wanted to quantify how much water could have been delivered to planetesimal precursors of Venus, Earth, and Mars 4.5 Gyr ago. We used the astrophysical model for protoplanetary disks, ProDiMo (Woitke et al. 2009), and the Monte Carlo (MC) simulation optimized for studying accretion of ice mantles on grains (Cazaux et al. 2010, 2015), both described in Sects. 2.1 and 3.1. Using T Tauri disks observed in the Orion Nebula as templates, with ProDiMo we carefully built up our early solar nebula model at three time steps in the Sun’s evolution. Temperature and pressure radial profiles and water vapor abundances were then extracted specifically for the midplane region close to the protosun. We used the MC simulations to calculate water adsorption rates. Surface coverage data at different physical conditions were then estimated and used to quantify possible scenarios on the origin of water on terrestrial planets and meteorites.

2. Simulating the early solar nebula with ProDiMo

Over the last decades the thermo-chemical evolution of our solar nebula has been modeled with different approaches and assumptions. In some of them the temperature and pressure gradients at different nebula stages were extrapolated from the condensation curves for actual solar system bodies (Cameron 1995; Fegley 1999; Lewis 1974), and in others the temperature and pressure gradients are a result of simulations of protoplanetary disks with typical solar nebula parameters (Willacy et al. 1998; Makalkin & Dorofeeva 2009).

To this latter approach belongs the (1+1D) model developed by Davis (2005a,b) to study the dependency of the surface density radial distribution from the disk accretion rate. Min et al. (2011) modeled the solar nebula conditions using 3D radiative transfer to investigate how the snow line changes with evolving mass accretion rate. Horsant et al. (2001) used the (1+1D) disk structure turbulent model of Huré & Galliano (2001) applied to the solar nebula to extract the density and temperature profiles favorable for the D/H enrichment in LL3 meteorites and comets. Albertsson et al. (2014) combined an extended gas-grain chemical model, which accounts for high temperature reactions and surface reactions with multiply deuterated species, with a (1 + 1D) steady-state α-viscosity nebular model to obtain molecular abundances and D/H ratios for a 1 Myr old solar nebula. However, in all these models, the input parameters are not necessarily informed by typical protoplanetary disks as they are now observed in tremendous detail.

The early solar nebula disk structure presented in this work uses the protoplanetary disk modeling code ProDiMo (Woitke et al. 2009; Aresu et al. 2012). The code was developed to consistently calculate the physical, thermal, and chemical structure of protoplanetary disks. It uses 2D dust continuum radiative transfer, gas phase and photo-chemistry, and a detailed thermal energy balance for the gas. ProDiMo models have been successfully applied to simultaneously explain multiwavelength observations of dust and gas (including resolved images) in disks around young stars (see Thi et al. 2010; Woitke et al. 2011; Tilling et al. 2012; Garufi et al. 2014). The code uses now the more realistic disk dust opacities from Min et al. (2016), which can simultaneously reproduce thermal, scattering, and polarization data from disks. Recently, Woitke et al. (2016) proposed a parametrized setup for disk models that can capture enough complexity to match observations without introducing too many free parameters.

In the following, we use this parametrized setup of ProDiMo to simulate a young solar nebula under steady-state condition around a Sun-like star at three evolutionary stages.
Table 1. Stellar and disk parameters.

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<thead>
<tr>
<th>Parameters</th>
<th>Symbol</th>
<th>Value</th>
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<td>1 $M_\odot$</td>
</tr>
<tr>
<td>Stellar Luminosity</td>
<td>$L_\star$</td>
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</tr>
<tr>
<td>Effective temperature</td>
<td>$T_{\text{eff}}$</td>
<td>4147, 4282, 4290 K</td>
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<td>UV luminosity</td>
<td>$L_{\text{UV}}$</td>
<td>0.01 $L_\odot$</td>
</tr>
<tr>
<td>X-ray luminosity</td>
<td>$L_X$</td>
<td>$10^{30}$ erg s$^{-1}$</td>
</tr>
<tr>
<td>Cosmic ray ionization rate</td>
<td>CRI</td>
<td>$1.7 \times 10^{-17}$ s$^{-1}$</td>
</tr>
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</table>

Disk mass $M_d$, Disk inner radius $r_{\text{in}}$, Disk outer radius $r_{\text{out}}$, Tapering-off radius $R_{\text{tap}}$, Reference scale height $H_0$, Reference radius $R_{\text{ref}}$.

Dust settling turbulence $\alpha$, Column density index $\epsilon$, Dust-to-gas ratio $\rho_d/\rho_g$, Min. size dust grain $a_{\text{min}}$, Max. size dust grain $a_{\text{max}}$, Dust size distr. index $\rho$, Dust composition $\sigma$.

Mg$_2$O, FeO, SiO$_3$ 60%, amorph. carbon 15%, porosity 25%.

Dust material density $\rho_g$ 2.076 g cm$^{-3}$.

Notes. ProDiMo input parameters used to model six early solar nebula, for two disk mass values (0.003 $M_\odot$ and 0.03 $M_\odot$) at three nebular ages (0.2 Myr, 1 Myr, and 10 Myr), to which the following stellar parameters ($L_\star$ and $T_{\text{eff}}$) correspond respectively (11.02 $L_\odot$, 4147 K), (2.17 $L_\odot$, 4282 K), and (0.46 $L_\odot$, 4290 K). Standard values from Helling et al. (2014) and Woitke et al. (2009).

2.1. Physical input parameters

The study of the oxygen isotope fractionation found in meteoritic mineral inclusions revealed that the protosun probably formed in a high mass, star forming region at a distance of ~1 parsec from an O or B star (Young et al. 2011). However, some uncertainty remains as to the cluster size (Adams 2010). Therefore, protoplanetary disks observed in the Orion Nebula (also called proplyds) are used here as templates to build our astrophysical model of the early solar nebula. The stellar and disk input parameters chosen for this work are listed in Table 1.

Ultraviolet (UV) and X-ray luminosities are fixed to standard values in circumstellar disks (Woitke et al. 2016). We neglect here the presence of the external UV radiation field by the possible nearby O and B stars; its impact on the disk midplane temperatures is small (~1 au) – the region relevant for our study of dust hydration – is negligible (Wals et al. 2013). However, as shown by Walsh et al. (2013), Antonellini et al. (2015), and Rab et al. (2018), among others, such enhanced external UV and X-ray radiation fields can have profound consequences for disk surface layers and the outer disk midplane which are readily observable through mid-IR and submm line emission of water and ion molecules.

Throughout the solar nebula, dust abundance and size distribution are assumed constant, with the latter following the power law $f(a) \sim a^{-\epsilon}$, with index $\epsilon = 3.5$ (Woitke et al. 2009) and grain sizes between $a_{\text{min}} = 0.05 \mu$m and $a_{\text{max}} = 3000 \mu$m (see Table 1). The dust in our models is attributed to that part of solids that are accessible through observations of protoplanetary disks such as SEDs. These disks could already contain larger solids, but evidence for this to date is indirect, for example from dating meteorites and putting constraints on ages of their parent asteroids in our solar system (e.g., Amelin et al. 2005, 2006) or disk substructure as revealed by SPHERE and ALMA images (e.g., Pérez et al. 2014; Benisty et al. 2015), which could indicate planetary mass companions (de Juan Ovelar et al. 2016).

The comparison between the disk mass distribution of the SubMillimeter Array (SMA) survey of 55 proplyds in Orion and similarly aged disks in the low mass, star forming regions Taurus and Ophiuchus shows that the Orion disk distribution is statistically different from the other two. The number of disks per logarithmic mass bin is approximately constant for masses 0.004–0.04 $M_\odot$ in all three regions, but Orion lacks disks more massive than 0.04 $M_\odot$ (Mann & Williams 2012). Accordingly, 0.03 $M_\odot$ and 0.003 $M_\odot$ were chosen as representative values for the disk mass of our early solar nebula.

Most of the previous solar nebula models are based on the Hayashi Minimum-Mass-Solar Nebula (MMSN) representation, where the local surface density is given by the mass of each planet spread on an appropriate annular area. In that case the surface density scales as a power law with index equal to −3/2 (Weidenschilling 1977; Hayashi 1981). The surface density profile in our work is assumed to be a power law

$$\Sigma(r) = \Sigma_0 r^{-\epsilon} e^{-r/r_{\text{tap}}},$$

with index $\epsilon$ equal to 1, less steep than the MMSN but in agreement with observations of proplyds in the Orion Nebula (Mann & Williams 2010). The exponential factor causes a tapering-off for the outer edge, meaning that at $R_{\text{tap}}$ the disk surface density profile starts an exponential cutoff and most of the disk mass will be contained therein.

The disk size was extracted from the disk diameter distribution histogram made for the total sample of 149 proplyds observed in the Trapezium cluster of the Orion Nebula with the HST (Vicente & Alves 2005) and the SMA (Mann & Williams 2010). It indicates that 75%–80% of disks have diameters smaller than 150 au and 40% of these disks have radii larger than 50 au. Hence, we picked a radius of 50 au as taper radius for our solar nebula.

In ProDiMo, the vertical disk structure is fully parametrized. Given a scale height, $H_0$, at a reference radius, $R_{\text{ref}}$, the scale height of the disk is given as

$$H = H_0(r/R_{\text{ref}})^{1.1}.$$
Lesur et al. 2014) and recent ALMA studies putting strong limits on levels of turbulence, both indicating that the disks are in large part more laminar than originally thought (e.g., Flaherty et al. 2018).

2.2. Temperature and pressure disk radial profiles

The dust temperature ($T_{\text{dust}}$) and pressure radial profiles at the disk midplane ($z/r = 0.00$) were extracted from six early solar nebula models: two disk mass limits (0.003 $M_\odot$ and 0.03 $M_\odot$) at three nebular ages (0.2 Myr, 1 Myr, and 10 Myr). In the following figures, only the values for the highest disk mass are shown for simplicity.

The youngest disk at the inner radius (fixed to 0.07 au) is hotter than the other two older models (Fig. 1, left). The main difference in the three ages is the stellar luminosity, which determines the main heating source in the innermost regions close to the protosun. The inner rim of the dust disk is heated by the stellar radiation, which is stronger for the youngest protosun. The maximum temperature far exceeds the dust condensation temperature. It ranges from about 2700 K for the 0.2 Myr old disk (black curve) to 1770 K at 1 Myr (red curve) and finally to about 1210 K for the 10 Myr model (blue curve). Here the inner radius was not adapted to a unified dust condensation temperature since our primary goal is not to capture the intricate details of the inner rim of the disk. Our study focuses on the midplane region where $T_{\text{dust}}$ ranges between 300 K and 600 K (Sect. 3.1). There are no differences in the midplane temperature profiles for the two disk masses considered.

The radial pressure profile (right side of Fig. 1) follows the trend of the dust temperature. From Eqs. (1) and (2), it is clear that the column density is indeed fixed and the mass is distributed according to our prescription, so the volume density does not change with age in our models. For disks with mass 0.03 $M_\odot$, the pressure is simply one order of magnitude higher than for 0.003 $M_\odot$ disks. This is true for the very optically thick part of the midplane.

Figure 2 offers an overview of the state of the art of previous solar nebula simulations in terms of temperature and pressure values at three representative distances from the protosun. A big discrepancy between our temperature values and those given in the Lewis (1974), Cameron (1995), and Willacy et al. (1998) simulations exists throughout the disk. At 0.1 au our youngest nebula (0.2 Myr old) is two times colder than the Willacy et al. (1998) nebula and a factor of 13 colder than the Lewis (1974) model. At 1 au the gap decreases to a factor of four and at 10 au our disk becomes two times colder indicating a very different slope of $T(r)$. For the pressure there is an overall good agreement, except for the values in the Lewis (1974) model,
which are two orders of magnitude larger than ours. The Lewis (1974) and Cameron (1995) models, based on the condensation curves of the actual composition of the bodies in the solar system, predict an adiabatic temperature-pressure dependency, far from our ProDiMo disks in thermal equilibrium. The 1D vertical structure model of a viscously heated disk ($\alpha = 0.01, M = 10^{-7} M_\odot \text{ yr}^{-1}, R_{\text{disk}} = [0.1−100] \text{ au}$) described by Wilicy et al. (1998) is slightly closer to ours. However, differences in input parameters likely cause the temperature differences. Differences are also seen for the $(P−T)$ values taken from the solar nebula simulation of Hersant et al. (2001). The model was calculated using $\alpha = 0.009$ and $M_{\text{disk}} = 0.3 M_\odot$, and it results in $R_{\text{out}} = 42$ and $32 \text{ au}$ respectively for a 1 and 0.2 $\text{Myr old disk}$. A good agreement exists between our temperature values and those of Davis (2005a), who implemented a $\beta$-prescription for the viscous heating in the 2D disk model from Dullemond et al. (2002).

In an active disk the viscous heating of the gas by accretion of material from the disk toward the protosun increases the dust temperature in the midplane by thermal accommodation with the gas. The effect of viscous heating is not captured in our ProDiMo models of a passive disk in which the column density is fixed, the mass is distributed according to our prescription, and dust and gas are thermally coupled in the midplane. This can explain the large deviations between the accretion models discussed earlier and the set of simulations studied in this work.

### 3. Monte Carlo simulation of water adsorption on forsterite surface

In order to test the wet endogenous scenario, Stimpfl et al. (2004) quantified the number of water molecules adsorbed on grain surfaces. A grid of 10,000 sites, considered to mimic the dust surface, could interact with an infinite reservoir of water molecules, where a maximum of one monolayer is allowed for dust surface, which scales with the size of dust and gas are thermally coupled in the midplane. This can explain the large deviations between the accretion models discussed earlier and the set of simulations studied in this work.

In this work we investigate water adsorption by means of a Monte Carlo (MC) numerical code developed by Cazaux et al. (2010, 2015). With our simulations we address the following questions:

1. How many water molecules can adsorb on dust surfaces according to the $(T, n_{H_2O})$ parameters space typical from morphological (thermal and aqueous) alterations of the grains?
2. Which surface mechanisms and properties (adsorption, evaporation, binding energy, cluster formation, etc.) compete for the formation of the first water layer?
3. Where in the nebula can water vapor condensation efficiently hydrate meteoritic and asteroidal mineral components?
4. Is this a possible scenario to explain the presence of water on Earth?

#### 3.1. Input parameters

Our study focuses on the hydration of forsterite surface grains by water vapor condensation in the habitable zone. We have defined a region in the disk midplane ($z/r < 0.1$) where the gas and dust temperatures are coupled; they are referred to as the surface temperature in our MC models ($T_{\text{gas}} = T_{\text{dust}} = T$) and range from 300 K to 600 K. This “box” changes location in the nebula, moving inward or outward and/or shrinking depending on the nebula’s age, hence stellar luminosity (see Fig. 3). The $H_2O$ vapor density as a function of temperature (insets in Fig. 3), which correspond to the conditions in the “box”, was extracted from each ProDiMo model. Three values were used here as input parameters in the MC simulation within the range $[10^8−10^{13}] \text{ cm}^{-3}$ (see Table 2).

In our MC simulation the [1 0 0] forsterite crystal lattice is considered and consists of a grid composed of $20 \times 20$ sites with a total surface area of $27.04 \text{ nm}^2$. According to previous DFT calculations (Stimpfl et al. 2006), the unit cell shows four possible binding sites corresponding to Mg cations, three of which are closer to the surface and easily accessible to water molecules. The highest binding sites of about 19 240 K (160 kJ mol$^{-1}$) represent 45% of the total number of sites, while binding sites with energies around 15 640 and 8420 K (70 kJ mol$^{-1}$, respectively) represent 15% and 30% of the total number of sites. We created a step-like function to reproduce the surface energy distribution of a [1 0 0] crystal lattice by using three Gauss–Boltzmann distributions with central energies at 8420 K, 15 640 K, and 19 240 K, listed in Table 2.

Each water molecule is sent randomly onto the surface and its track is recorded from the moment of its adsorption, through surface diffusion up to its eventual desorption. In this work we focus on the formation of the first monolayer, preliminary stage for water diffusion into the bulk (Thi et al. 2018). The adsorption of water molecules from the gas phase occurs at a rate

$$R_{\text{ads}} = n_{H_2O} v_{H_2O} \sigma S \text{ cm}^{-2} \text{ s}^{-1},$$

(3)

which depends on the density of water molecules $n_{H_2O}$; their thermal velocity $v_{H_2O} \sim 0.43 \sqrt{T_{\text{gas}}/100} \text{ km s}^{-1}$; the cross section $\sigma$ of the dust surface, which scales with the size of the grid (here $7.66 \times N_\text{sites}^{-2}$); and the sticking coefficient $S$ (assumed equal to 1).
If a water molecule lands in a site surrounded by H\textsubscript{2}O, its binding energy increases linearly with the number of neighboring molecules (Cuppen & Herbst 2007) as 0\textsuperscript{b}. The binding energy increases linearly with the number of neighbors. The activation energy for diffusion is 40% of the binding energy, as in Cazaux et al. (2015), thus it depends on the binding site and number of neighboring water molecules.

Once adsorbed on the surface, water molecules can sublimate back into the gas phase. The desorption rate depends on the binding energy of the water molecules and is therefore directly dependent on the number of neighbors $n_{\text{nb}}$. The desorption rate of one water molecule with $n_{\text{nb}}$ neighbors can therefore be written as

$$R_{\text{des}} = v \exp\left(-\frac{n_{\text{nb}} E_b}{T}\right) \text{s}^{-1}.$$  

Where desorption rates increase exponentially with the surface temperature, accretion rates increase linearly with the density of water molecules. The coverage of water molecules on dust surfaces is governed by these two competing mechanisms. In the next section, we address the kinetics of forsterite hydration.

### 3.2. Results from Monte Carlo simulation

We performed several simulations with equal grid properties at the temperatures and water vapor densities indicated in Table 2. Our motivation was to study how much water can be accreted onto dust grains in the parameter space ($T, n_{\text{H}_2\text{O}}$) that defines the region between 0.07 and 0.3 au from the protosun where the raw material for terrestrial planets may have experienced morphological (thermal and aqueous) alterations.

In Fig. 4, adsorption rates of water vapor molecules onto the forsterite [1 0 0] crystal lattice are shown for various surface temperatures ($T_{\text{gas}} = T_{\text{dust}}$) and water vapor densities of $6 \times 10^3$ cm\textsuperscript{-3} (top), $6 \times 10^4$ cm\textsuperscript{-3} (middle), and $6 \times 10^5$ cm\textsuperscript{-3} (bottom). For the lowest water vapor density considered, at 300 K the [1 0 0] crystal surface is fully covered by one monolayer; at 400 K about 90% of the surface is hydrated; at a temperature between 500 K and 600 K the surface coverage drops to about 30% of the total surface area; and at 800 K no water molecules stick to the surface. Upon exposure to the intermediate water density (see Fig. 4, middle plot) the coverage at equilibrium increases for each considered temperature. At the highest water vapor density (see Fig. 4, bottom plot) at 800 K one-third of the forsterite grain can retain water on its surface. The equilibrium for the formation of one monolayer is rapidly achieved within 100 s at the lowest vapor density, within 10 s for the intermediate density value, and less than 0.1 s for the highest vapor density considered.

The average surface coverage at equilibrium was calculated and plotted as a function of temperature (Fig. 5 left panel) and

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Table 2. Input parameters for the Monte Carlo simulation.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>This work</th>
<th>Comparison work</th>
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<tr>
<td>$n_{\text{H}_2\text{O}}$ (cm\textsuperscript{-3})</td>
<td>6(8), 6(10), 6(12)</td>
<td>1(11)\textsuperscript{a}</td>
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<tr>
<td>T (K)</td>
<td>300 – 800</td>
<td>700 – 1200\textsuperscript{b}</td>
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<td></td>
<td></td>
<td>1000 – 1500\textsuperscript{b}</td>
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<tr>
<td>$E_{\text{ads}}$ (K)</td>
<td>8420 (55%)</td>
<td>19 240.4\textsuperscript{c}, 19 240\textsuperscript{b}</td>
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<td></td>
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<td>15 640 (30%), 16 120\textsuperscript{c}, 15 132.4\textsuperscript{d}</td>
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</table>

Notes. The number in parentheses (…) indicates the power of 10.

References. \textsuperscript{(a)}Muralidharan et al. (2008); \textsuperscript{(b)}Stimpfl et al. (2006); \textsuperscript{(c)}King et al. (2010); \textsuperscript{(d)}Prigobble et al. (2013); \textsuperscript{(e)}Stimpfl et al. (2004).
The decrease in surface coverage with increasing temperatures is not linear, but reflects the step-like function used to describe the three different types of binding sites with different binding energies (see Table 2). This distribution of binding sites and the cluster effect also cause the surface coverage to decrease to zero smoothly when approaching 700 K and 800 K. For an increasing $n_{\text{H}_2\text{O}}$ the surface coverage increases, also non-linearly (see Fig. 5, right panel). This is more visible for higher temperatures and reflects the competition between desorption and adsorption of water molecules which are allowed to cluster around an occupied site.

In our MC simulations two important surface processes were implemented: surface diffusion and water cluster formation. The latter helps water molecules increase their binding energies as other adsorbed molecules, present in neighboring sites, will add energies to the binding through H-bonds. The effect can be seen in the lower panel of Fig. 5, where at equal water vapor density, molecules resist thermal desorption by forming a “cluster” around an occupied site thus increasing their adsorption energy. As claimed in de Leeuw et al. (2000) and Stimpfl et al. (2006), this cooperative behavior increases the chances for more water to adsorb and to remain on the surface, in particular at high temperatures.

3.3. Discussion of MC simulations

In case of a gas rich in water vapor, molecular adsorption onto silicate grains would be an efficient hydration mechanism over a wide temperature range within planetary accretion timescales. Our results deviate somewhat from previous works. For instance, at 700 K and $6 \times 10^{10}$ H$_2$O cm$^{-3}$, similar physical parameters used by Muralidharan et al. (2008), our simulation shows that only 30% of the [1 0 0] forsterite surface is occupied by water molecules, while Muralidharan et al. (2008) obtained full surface coverage. Our equilibrium timescales are three orders of magnitude smaller than that obtained in the Muralidharan et al. (2008) simulations (within 20 000 s at all temperatures in the range [700–1200] K), which is very short compared to the nebula lifetime of millions of years.

Finally, in our work the surface coverage decreases as a step function with the temperature, in contrast with the results of Muralidharan et al. (2008) where an exponential trend was found for the temperature range [700–1200] K. These discrepancies can be due to differences between the two models and input parameters. Adsorption and a box of gas molecules in the random-walk regime with equal mean free path and collision frequency to the [1 0 0] forsterite surface are treated in the same way in this work and in Muralidharan et al. (2008). In Muralidharan et al. (2008), the surface potential is detailed precisely using a grid subsampled in 3924 cells of area 0.062 Å$^2$ compared to the 400 sites of 6.76 Å$^2$ for our model surface. This can explain the smooth, exponential decrease in the surface coverage with temperature versus the step-like, nonlinear trend in our simulations. However, our temperature range overlaps with theirs only for two values. In addition, we allow the water molecules to scan the surface upon collision and, by lateral diffusion, to find the favorable binding site. This can explain why the time spent for the system to reach equilibrium is a factor of 1000 shorter than in Muralidharan et al. (2008), where a simple collision theory is considered.

To further understand the reason for the differences, we have investigated different surface potential energy distributions (Appendix B) that reproduce the energy potential in Stimpfl et al. (2006) and used in Muralidharan et al. (2008).
Fig. 5. Top panel: surface coverage (H$_2$O nm$^{-2}$) as a function of temperature (K) (left panel) and water vapor density (cm$^{-3}$) (right panel). Each data point is the average ±σ of the coverage values at equilibrium (see Fig. 4). Left panel: dashed lines are used here to link each point and emphasize the step-like decrease in the surface coverage with temperature. Bottom panel: simulated [1 0 0] forsterite surface grids at 6 × 10$^8$ cm$^{-3}$ and T = [300–700] K (from left to right panels). The color scale indicates the adsorption energy of the occupied sites in the range between 13 000 K (blue) and 25 000 K (yellow).

Again, at 700 K and 6 × 10$^{10}$ H$_2$O cm$^{-3}$ no full coverage was attained contrary to the results in Muralidharan et al. (2008). The cause of this discrepancy can depend on an oversampling of the surface sites which can affect the energy distribution.

4. Solar nebula implications

Several near- and mid-IR observations (Salyk et al. 2008; Carr & Najita 2008; Pontoppidan et al. 2010; Carr & Najita 2011; Riviere-Marichalar et al. 2012) have revealed the presence of warm water vapor (300–800 K) in the habitable planet forming region (within three astronomical units) in T Tauri circumstellar disks. Embedded in this environment, small micron-sized silicate dust grains have also been observed from their signatures at 10 µm and 18 µm (e.g., Kessler-Silacci et al. 2006). Shape, intensity, and exact wavelength of these spectral features are indicative of the dust morphology (crystalline or amorphous), mineralogy (i.e., forsterite, enstatite, etc.), and size properties (see, e.g., Jäger et al. 2003; Chiang 2004; Bouwman et al. 2008).

Despite the long-standing debate on which mechanisms contributed to the water content on rocky planets in our solar system (exogenous versus endogenous), our work shows that water gas-solid interaction can lead to hydration of the pristine forsterite surface under nebula conditions within its lifetime. In the following, the surface coverage data obtained from our MC simulations are discussed in the context of the Earth mantle water and oceans, and are compared to the amount of hydrated silicates found in meteorites and observed on asteroids.

It is clear that our approach has its limitations as we neglect several processes that affect both the global and local grain size distribution in the nebula. Grain growth (and destruction), vertical settling, and radial migration are processes that act in young disks as they are evolving into planetary systems (see, e.g., Birnstiel et al. 2016 for a recent review). Pinte et al. (2016) show that ALMA images of the young T Tauri disk around HL Tau indicate the presence of large mm-sized grains that have settled efficiently to the midplane. On the other hand, Kruijer et al. (2014) find that the parent bodies of various types of iron meteorites likely accreted within 0.1–0.3 Myr after CAIs, thus providing support to the possibility that large bodies could already exist in protoplanetary disks with ages of 1–3 Myr. In that context, the assumptions made below of either a single small grain size or an observed homogeneous grain size distribution throughout the inner disk can only be limiting cases and more detailed studies are required in the future to combine the results from water adsorption with detailed dust evolutionary models of the inner disk.

4.1. Water content on Earth

The oceans are not the only water reservoir on our planet. Adding together the water contributions of the hydrosphere (1.6 × 10$^{21}$ kg), the exosphere including the crust (1.9 × 10$^{21}$ kg), and the mantle (between 0.3 and 2.5 × 10$^{21}$ kg) and normalizing by the mass of the bulk silicate Earth (BSE = mantle + crust, 4.05 × 10$^{24}$ kg), the total water budget ranges between 0.05 and 0.11 wt%. The Earth is currently 5–50 times dryer than the CV and CO, the two driest classes of C-chondrites (Mottl et al. 2007). Nevertheless, the wet bodies that collided to form our protoplanet must have possessed a larger amount of water than the actual Earth’s abundance to account for the loss of such volatile species by impact degassing.
The agglomeration of wet 0.1 \( \mu \)m sized grains upon exposure at 800 K to water molecules at densities of \( 6 \times 10^{15} \) cm\(^{-3}\) (red triangle) and \( 6 \times 10^{17} \) cm\(^{-3}\) (blue triangle), respectively.

Assuming that the \([100]\) surface constitutes about 44% of the surface area of a perfect forsterite crystal, for a water density of \( 10^{11} \) cm\(^{-3}\) Muralidharan et al. (2008) obtained between eight and four Earth oceans at respectively 700 K and 800 K, a factor of five to nine greater than our results. In a later work, Asaduzzaman et al. (2015) showed the trend of the OEW as a function of grain size for different coverage and at 900 K and 10\(^{12}\) bar of water pressure (likely Earth forming conditions).

Considering that 65% of the Earth’s mantle is olivine mineral, agglomeration of 0.1 \( \mu \)m grains would account for about five and two OEW in the Earth’s mantle, respectively, for full or partial coverage (42% of the total surface area). This occurs with most of the \((T, n_{H_2}O)\) pairs we considered in our models.

In Stimpfl et al. (2004), Monte Carlo simulations are used to evaluate the coverage of water on a substrate on a grid of 10,000 cells. They found that the adsorbed water potentially stored in the dust corresponds to about three times the Earth’s oceanic + atmospheric + crustal water (OAC) and about 1.5 times the Earth’s OAC + mantle water. According to the latest estimation of the Earth’s water reported by Genda (2016), roughly four ocean masses are needed to account for the surface and mantle water. Our results demonstrate that during the early solar nebula at a distance of 0.07–0.3 au from the protosun and with the parameter space \((T, n_{H_2}O)\) described earlier, 0.1 \( \mu \)m dust grains are subject to an intense aqueous alteration. By the same mechanisms that transport processed materials in- and outward in the disk (Gail 2004; Boss 2004; Nuth et al. 2005), these wet silicates would eventually reach the terrestrial planets feeding zone (within one astronomical unit) and there supply enough water for oceans to rise.

In our ProDiMo models, the grain size distribution holds for the entire disk with sizes ranging between 0.05 and 3000 \( \mu \)m (see Table 1). However, dust settling vertically to the mid-plane changes the second and third moments of the distribution. Accordingly, in Eqs. (4) and (5) we chose to use respectively the second and third moments of the grain size distribution (see Sect. 2.1), which are \((a'') = 1.245 \times 10^{-12} \) cm\(^{-3}\) and \((a') = 1.525 \times 10^{-13} \) cm\(^{-3}\). The number of Earth oceans thus obtained is two to three orders of magnitude smaller than in the previous case (see symbol in Fig. 6). In particular, between 3.5% to 8% of an ocean of water can accrete at 500 K and between 0.5% and 4% at 700 K. These results are close to those in Stimpfl et al. (2004), where 1% and 3% of one Earth ocean could accrete at 700 K and 500 K respectively (see Drake 2005).

Hence, the contribution to the water content on habitable planets provided by hydrated silicates varies with the size distribution of the mineral grains. At a very early stage of our solar nebula, when grains were ISM-like, Earth could potentially inherit an amount of water equal to ten oceans. At a late stage in the disk evolution, when dust grains grow, water vapor condensation can contribute to less than 1% of an Earth ocean. This is a lower limit to the amount of water that can be incorporated into the grain due to the assumptions presented in this work. Only a single layer of water molecules was allowed to form onto a defect-free crystalline silicate surface. It was ignored that hydration is enhanced when defects are present, and amorphous silicates were considered instead (Yamamoto & Tachibana 2016).

Finally, we neglected bulk diffusion into the core of the silicate grain, which has recently been shown to occur efficiently at temperatures as high as 700 K in the inner regions of a
protoplanetary disk (Thi et al. 2018). All these factors can significantly enhance the amount of phyllosilicates that can form.

### 4.2. Phyllosilicates in asteroids

For a simple estimate of the fraction of phyllosilicates in asteroids under the scenario of hydration by water vapor, we assess which fraction of the precursor grains could be turned into phyllosilicates through surface reactions. The second moment of the grain size distribution \( \langle a^2 \rangle = 1.245 \times 10^{-10}\text{ cm}^2 \) provides the average surface of a grain. With a density of surface sites of \( N_{\text{sites}} = 1.5 \times 10^{15}\text{ cm}^{-2} \), we find a total of 2.35 \( \times \) \( 10^6 \) surface sites. The dust-to-gas mass ratio is

\[
\frac{M_{\text{d}}}{M_{\text{H}}} = \frac{n_{\text{d}} \cdot 4\pi \langle a^3 \rangle p_{\text{gr}}}{n_{\text{H}} \cdot \mu m_{\text{H}}} = 0.01, \tag{6}
\]

where \( M_{\text{d}} \) is the mass of dust, \( M_{\text{H}} \) the mass of the gas (hydrogen gas), \( n_{\text{d}} \) the volume density of dust, \( p_{\text{gr}} \) the mass density of dust grains (2.076 g cm\(^{-3}\)), \( \mu \) is the mean molecular weight of the gas (2.4 for H\(_2\) gas), \( m_{\text{H}} \) is the total hydrogen number density in the gas, and \( m_{\text{H}} \) the mass of hydrogen (1.67 \( \times \) \( 10^{-24}\) g). The volume density of dust grain can then be written as

\[
n_{\text{d}} = 3 \cdot 0.01 \mu m_{\text{H}} n_{\text{H}} \langle a^2 \rangle p_{\text{gr}} \tag{7}
\]

with the third moment of the grain size distribution \( \langle a^3 \rangle = 1.525 \times 10^{-13}\text{ cm}^3 \). Knowing the volume density of dust grains, we can estimate the number of sites on the surface of the grains per cm\(^3\) as

\[
n_{\text{d}} \times N_{\text{sites}} = \frac{3 \cdot 0.01 \mu m_{\text{H}} n_{\text{H}} \langle a^2 \rangle p_{\text{gr}}}{4 \pi \langle a^2 \rangle p_{\text{gr}}} \times 4 \pi \langle a^2 \rangle N_{\text{sites}} = 7.08 \times 10^{-8} n_{\text{H}}. \tag{8}
\]

We assume that no diffusion of water occurs and reactions are limited to the surface. This is a conservative lower limit to the phyllosilicate production since grains will be irregularly shaped and defects at the surface will help water to diffuse into the interior. Assuming the stoichiometry of the following reaction

\[
2\text{Mg}_3\text{SiO}_4 + 3\text{H}_2\text{O} \rightarrow \text{Mg(OH)}_2 + \text{Mg}_2\text{Si}_2\text{O}_5(\text{OH})_4,
\]

and that 60% of the surface is silicates and 30% of sites are occupied by water, the lower limit to the number density of phyllosilicates on surfaces is \( 1.274 \times 10^{-8}\text{ sites cm}^{-3}\). The fraction of water contained in dust can be written as

\[
\rho_{\text{water on grain}} = \frac{3 \cdot 0.01 \mu m_{\text{H}} n_{\text{H}} \cdot N_{\text{sites}} \cdot 4 \pi \langle a^2 \rangle \cdot 0.6 \cdot 0.3 \cdot 18 m_{\text{H}}}{4 \pi \langle a^2 \rangle p_{\text{gr}} \cdot 0.01 \mu m_{\text{H}} n_{\text{H}}}. \tag{9}
\]

This translates into a lower limit to the fraction of adsorbed water of \( \sim 10^{-3}\). If the grains had all been 0.1 \( \mu \text{m} \) in size, this number would be \( \sim 10^{-2}\), two orders of magnitude higher.

Our models show that hydration in the parent bodies of meteorites (the asteroids) could have occurred in the inner and warm solar nebula. Among different types, CM and CI carbonaceous chondrites typically contain 5–15% H\(_2\)O/OH by weight (Rivkin et al. 2002, and references therein) with the least hydrated CV type showing abundance of hydrogen typically below 0.5 wt% (Beck et al. 2014, and references therein). To account for such a large degree of aqueous alteration, subsequent hydration mechanisms need to be considered. For instance, diffusion of water molecules into the silicate bulk enables a higher formation rate of phyllosilicates (Thi et al. 2018), in particular in the relatively hot regions (\( T > 700\text{ K} \)) of the disk midplane where the cluster effect explored in our models does not retain water on the surface efficiently.

### 5. Conclusions

In this work we investigated the efficiency of water vapor adsorption onto forsterite grains surfaces as one of the mechanisms that contributed to the water on Earth and in asteroids.

The astrophysical disk model ProDiMo tailored to the solar nebula properties was combined with Monte Carlo simulations of water adsorption on a [1 0 0] forsterite crystal lattice. Water vapor abundances, temperature, and pressure radial profiles identify the region in the warm disk midplane, between 0.07 and 0.3 au from the protosun, where hydration of dust grains could have occurred. Several MC simulations were run to assess the dependency of the adsorption rate and the surface coverage on the parameter space identified by the pairs \((T, m_{\text{H}_2\text{O}})\).

Our MC models show that complete surface water coverage is reached for temperatures between 300 and 500 K. For hotter environments (600, 700, and 800 K), less than 30% of the surface is hydrated. At low water vapor density and high temperature, water cluster formation plays a crucial role in enhancing the coverage (see also Appendix C). The binding energy of adsorbed water molecules increases with the number of occupied neighboring sites, enabling a more temperature-stable water layer to form. Lateral diffusion of water molecules lowers the timescale for surface hydration by water vapor condensation by three orders of magnitude with respect to an SCT model, ruling out any doubts on the efficiency of such processes in a nebular setting.

Finally, the amount of water potentially delivered on Earth drastically varies if we rely on a grain size distribution instead of a single grain size. Grain agglomeration and dust settling to the midplane, the initial steps for planetesimal formation, should clearly lead to a wide grain size distribution as the nebula evolves. In order to improve our initial estimates, detailed dust evolution models should be combined with the water adsorption efficiencies found here.

In addition, dynamical simulations of grain growth are required to understand how agglomeration and collision processes affect the amount of water retained on the grain surfaces and how this competes with the diffusion timescale of water molecules into the bulk of the grains.

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### References


Appendix A: H₂ as gas competitor

In the following, we will make some simple estimates to assess the role of dust and H₂ in our Monte Carlo simulations. The simplified approach assumes that we have a constant influx of water molecules onto a fixed surface (representing part of the surface of a single grain). However, the water molecules encounter other dust grains and H₂ molecules within a fixed volume. In a primordial disk, water is typically four orders of magnitude less abundant than H₂. This implies that water will repetitively collide with H₂ before reaching a dust grain, which could change the timescale for water molecules to reach the dust. As H₂ collides frequently with the grain surface it could hinder or block the influx of water. In this study, we consider that H₂ molecules can only be physisorbed on surfaces. Chemisorption of H₂ will make the sticking probability of H₂ molecules negligible. We therefore neglect H₂ chemisorption, and consider only the effect of the grains covered by physisorbed H₂ molecules and estimate whether this coverage could influence the sticking of water. At the typical gas temperatures considered here, H₂ cannot stick to the warm silicate surface. However, even an extremely short residence time could block that surface site from adsorbing water. The following estimates relate to one representative set of conditions in the disk with \( n_{\text{H}_2} = 10^{15} \text{ cm}^{-3} \) and \( T_g = 500 \text{ K} \). The size of an adsorption site is assumed to be \((2.6)^{2} \AA^2\) and the thermal velocity of H₂ molecules is \( v^\text{th}_{\text{H}_2} = \sqrt{\frac{2kT_g}{\pi m_{\text{H}_2}}} = 1.15 \times 10^5 \text{ cm s}^{-1}\). (A.1)

The influx of H₂ into a surface site can then be calculated to be \( F_{\text{H}_2} = n_{\text{H}_2}v^\text{th}_{\text{H}_2}(2.6 \times 10^{-8})^2 = 7.77 \times 10^4 \text{ s}^{-1}\). (A.2)

At the same time, the influx of water molecules is \(2.6 \text{ s}^{-1}\) with \( v^\text{th}_{\text{H}_2O} = 3.83 \times 10^5 \text{ cm s}^{-1}\). The residence time on the surface for H₂ molecules is given by the rate constant for adsorption

\[
\tau = \frac{1}{\nu^\text{osc} \exp(-E_{\text{ads}} / kT_g)}, \tag{A.3}
\]

with the adsorption energy \( E_{\text{ads}} / k \sim 500 \text{ K} \) for H₂ physisorption (Pirronello et al. 1997), the lattice vibrational frequency \( \nu^\text{osc} = (2n_{\text{surf}}E_{\text{ads}}/(\pi^2 m_{\text{H}_2}))^{1/2} = 2.50 \times 10^{12} \text{ s}^{-1}\), and the density of surface sites \( n_{\text{surf}} = 1.5 \times 10^{15} \text{ cm}^{-2}\). Assuming \( T_g = T_g\) as well yields \( \tau = 1.08 \times 10^{-12} \text{ s}\). If an H₂ molecule is present on the arrival site of a water molecule, then the water molecule will occupy the place of the H₂ and swap (Cuppen & Herbst 2007). In any case, it has been proven experimentally that a surface covered by H₂ molecules would be more accommodating to incoming species, and therefore that the sticking coefficient would increase. Molecular hydrogen covering a surface serves as a medium to lose kinetic energy and to become more easily thermalized on the surface and adsorb (Gavilan et al. 2012).

Appendix B: Surface potential energy distribution

### Table B.1. Parameters (central adsorption energy, sigma, and intensity) of the Maxwell–Boltzmann distributions of surface energy potential models called A, B, and C.

| E_{\text{ads}} (K) | \sigma (%| | Model A |
|-------------------|----------|----------|
| 19 240 (160)      | 80       | 15       |
| 15 640 (130)      | 80       | 30       |
| 8420 (70)         | 80       | 55       |
| Model B |
| 25 260 (210)      | 1000     | 10       |
| 8420 (70)         | 4000     | 80       |
| 0 (0)             | 4000     | 10       |
| Model C |
| 25 260 (210)      | 1000     | 8        |
| 16 840 (125)      | 500      | 22       |
| 8420 (70)         | 1000     | 60       |
| 3010 (25)         | 2000     | 10       |

**Notes.** The number in parentheses (...) are expressed in kJ mol\(^{-1}\).

Model A (red curve in the left and middle plots of Fig. B.1) is a step function composed by three distributions, where only 45% of the sites have binding energies greater than 14 430 K (120 kJ mol\(^{-1}\)), hence those most favorable for attracting the first water molecules (Stimpfl et al. 2006). Model B (green curve) is constructed by matching the surface potential energy distribution shown in Stimpfl et al. (2006). Here sites with binding energies smaller than 8420 K (70 kJ mol\(^{-1}\)) are included, contrary to model A. Finally, model C (blue curve) includes 8% of surface sites with adsorption energies higher at 25 260 K (210 kJ mol\(^{-1}\)), which were not taken into account in model A although claimed by the atomic model of Stimpfl et al. (2006).

The surface energy potential distribution of the adsorption sites of the crystal surface determines the coverage of the adsorbed water molecules. As shown in the right plot of Fig. B.1, in model C the surface coverage is 5% higher than in model A at 700 K and \( n_{\text{H}_2O} = 6 \times 10^{10} \text{ cm}^{-2}\). The surface potential energy distribution of model B allows only half the coverage than seen in model A and C, due to the higher hydrophobicity of the surface.

We can conclude that the choice of the adsorption energy of the sites does not explain the factor of three difference in surface coverage between our work and the Muralidharan et al. (2008) simulations.
Appendix C: Water cluster simulation

In our MC models the water molecules randomly “walk” on the surface until they adsorb at a favorable site. As two water molecules sit on neighboring sites, a hydrogen bond links the two species, and a dimer can be created with the total binding energy higher than the ones of single molecules. This generates the formation of water clusters for which the binding energy increases with increasing size (González et al. 2007). In two dimensions, the binding energies increase with the number of water molecules present in the cluster, while for a 3D cluster Lin et al. (2005) show that the binding energy mainly depends on the number of water molecules close to the surface.

In this work we used a simple way to calculate the binding energies, which increase linearly with the number of neighboring water molecules (Dartois et al. 2013), but we limited the number of water molecules to four. Water clusters have been implemented in previous MC simulations to study the formation of water on carbon grains in the ISM (Cazaux et al. 2010), and to investigate the porous structure of ices (Cazaux et al. 2015) and its effect on the location of the snow line in different astronomical environments (Marseille & Cazaux 2011).

Temperature programmed desorption experiments conducted by Brown & Bolina (2007) confirm that the desorption of pure H$_2$O ice on a graphite surface occurs at a higher temperature for increasing coverage. Therefore, as the coverage increases, the clusters become more important, and a higher surface temperature is needed to desorb the molecules.

The formation of clusters is therefore a competition between the evaporation of individual water molecules and the encounter of two molecules to initiate the cluster. In our models this effect can be seen in Fig. 5 of Sect. 3.2 and here in Fig C.1. At equal ($T, n_{H_2O}$) conditions, 35% of the surface sites are covered by water molecules when they form clusters with neighboring molecules (left plot, pink curve). The binding energies of the adsorbed water increase up to 25 000 K (right image) when clusters occur with four neighboring molecules. When the cluster effect is switched off, our simulations show that the surface coverage is 40% reduced (left plot, blue curve) and the adsorbed water molecules possess on average 20 000 K binding energy with the surface (middle plot).