Distributed Passivity-Based Control of DC Microgrids

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Abstract—In this paper, we propose a new distributed passivity-based control strategy for Direct Current (DC) microgrids. The considered DC microgrid includes Distributed Generation Units (DGUs) sharing power through resistive-inductive distribution lines. Each DGU is composed of a generic DC energy source that supplies an unknown load through a DC-DC buck converter. The proposed control scheme exploits a communication network, the topology of which can differ from the topology of the physical electrical network, in order to achieve proportional (fair) current sharing using a consensus-like algorithm. Moreover, the proposed distributed control scheme regulates the average value of the network voltages towards the corresponding desired reference, independently of the initial condition of the controlled microgrid. Convergence to a desired steady state is proven and satisfactorily assessed in simulations.

I. INTRODUCTION

The Distributed Generation (DG) and the possibility of storing energy are changing the paradigm of power generation, transmission and distribution [1]. Differently from the past, nowadays many agents of the electrical distribution network are indeed prosumers, playing an active role in the network by producing, as well as consuming, energy. Moreover, the DG has been proposed as a conceptual solution to

1. Facilitate the integration of Renewable Energy Sources (RES) in order to reduce the carbon emissions,
2. Increase the energy efficiency by reducing the transmission power losses,
3. Improve the service quality by supplying high-priority loads when a portion of the distribution network is isolated from the main grid and
4. Contain the costs for electrifying remote areas or re-powering the existing power networks due to the ever increasing energy demand.

A low-voltage electrical distribution network composed of multiple Distributed Generation Units (DGUs), loads and energy storage devices interconnected through power lines is identified in the literature as a microgrid [2].

In the last decades, since most of the existing power networks are Alternate Current (AC)-based, the literature on power networks mainly considered AC grids (see for instance [3]–[6] and the references therein). However, the recent widespread use of RES as DGUs is motivating the design and operation of Direct Current (DC) microgrids. Several devices (e.g., photovoltaic panels, batteries, electronic appliances, electric vehicles) can indeed be directly connected to a DC network avoiding lossy DC-AC conversion stages and the issues related to the frequency and reactive power control [7]. Besides the development of industrial, commercial and residential DC distribution networks, some examples of existing or promising DC microgrid applications are ships, mobile military bases, trains, aircrafts and charging facilities for electric vehicles. For all these reasons, control of DC microgrids is recently gaining growing interest.

One of the main control objectives in DC microgrids is the regulation of the network voltage towards the nominal value that guarantees a proper functioning of the connected loads [8]–[10]. Additionally, in order to perform an efficient demand and supply matching and avoid the over stressing of a source, it is generally desired that the total demand of the microgrid is shared among all the DGUs proportionally to the generation capacity of their corresponding energy sources [11]. However, achieving current or power sharing prescribes the value of the required differences in voltages among the nodes of the network. As a consequence, it is generally not possible to control the voltage at each node towards the corresponding desired value. Then, in [11], [12] the authors propose to control the average voltage across the whole microgrid (not a specific node) towards a global voltage set point (e.g., the average of the voltage references).

In the literature, the aforementioned objectives are conventionally achieved by designing hierarchical and distributed control schemes requiring that each node of the physical network shares information through a communication network (cyber system). For the sake of feasibility, it is usually desired that i) the control scheme is independent of the knowledge of the whole microgrid and ii) each node of the microgrid communicates only with its neighbouring nodes. This motivated a growing interest in the development of distributed controllers, particularly aiming at current (load) sharing [11]–[16].

A. Main contributions

In this paper, we design a distributed passivity-based control (PBC) scheme that provably guarantees to achieve at the steady state proportional (fair) current sharing and average voltage regulation for DC microgrids that include buck converters, unknown “ZIP” (constant impedance, constant current, constant power) loads and dynamic resistive-inductive lines. Our main contributions are outlined below, where we also provide a brief comparison with existing theoretical results considering both the aforementioned control objectives:

1) The considered microgrid model takes into account a possible meshed microgrid topology, incorporating dynamic resistive-inductive lines, which are neglected in e.g. [12]
and [13], where purely resistive lines are adopted. Moreover, we include ZIP loads, which are not considered in e.g. [12], [15] and [16], where only constant current loads are analyzed.

2) The proposed control scheme requires only local measurements of the generated current. Differently from [12], [13] and [16], average voltage regulation is achieved without voltage measurements, while current sharing is achieved by exploiting a communication network where each DGU shares the corresponding value of the generated current with its neighbours. Notably, the design of the communication network is independent from the topology of the microgrid, in contrast to the results provided in [12], where an assumption is introduced on the product between the Laplacian matrices associated to the microgrid and communication networks [12, Assumption 4].

3) The stability analysis provides conditions on the controller gains making the control synthesis simpler than e.g. the one proposed in [12], where a Linear Matrix Inequality (LMI) problem is solved for each local primary voltage controller.

4) Convergence to a desired steady state is guaranteed, independently from the initial condition of the states of the physical microgrid and the controller. This is in contrast to e.g. [13], where a suitable initialization of the voltages is assumed, or [12] and [16] where a suitable initialization of the controller state is required to perform average voltage regulation.

B. Outline

The remainder of this paper is organized as follows. The microgrid model is presented in Section II, while the control problem is formulated in Section III. In Section IV, the proposed PBC control scheme is introduced and the stability of the controlled microgrid is studied. In Section V, the simulation results are illustrated and discussed, and finally, conclusions are gathered in Section VI.

II. DC MICROGRID MODEL

In this paper, we study a typical DC microgrid composed of \( n \) Distributed Generation Units (DGUs) connected to each other through \( m \) resistive-inductive (RL) power lines. A schematic electrical diagram of the considered DC network including a DGU and a distribution line is illustrated in Fig. 1 (see also Table I for the description of the used symbols). Each DGU includes a DC-DC buck converter equipped with an output low-pass filter \( L_i C_i \) supplying an unknown “ZI” (constant impedance, constant current) load\(^*\). The DC load is connected to the so-called Point of Common Coupling (PCC). By using the Kirchhoff’s current (KCL) and voltage (KVL) laws, the equations describing the dynamic behaviour of the DGU \( i \) are given by

\[
\begin{align*}
L_i \dot{I}_i &= -V_i + u_i \\
C_i \dot{V}_i &= I_{ti} - \frac{V_i}{Z_{li}} - I_i - \sum_{k \in E_i} I_k,
\end{align*}
\]

where \( E_i \) is the set of distribution lines incident to the DGU \( i \), while the control input \( u_i \) represents the buck converter output voltage\(^1\). The current shared among DGU \( i \) and DGU \( j \) is denoted by \( I_k \), and its dynamic is given by

\[
L_k \dot{I}_k = (V_i - V_j) - R_k I_k.
\]

The symbols used in (1) and (2) are described in Table I.

The overall DC microgrid is represented by a connected and undirected graph \( \mathcal{G} = (\mathcal{V}, \mathcal{E}) \), where the nodes, \( \mathcal{V} = \{1, \ldots, n\} \), represent the DGUs and the edges, \( \mathcal{E} = \{1, \ldots, m\} \), represent the distribution lines interconnecting the DGUs. The microgrid topology is described by its corresponding incidence matrix \( \mathcal{B} \in \mathbb{R}^{n \times m} \). The ends of edge \( k \) are arbitrarily labeled with a + and a −, and the entries of \( \mathcal{B} \) are given by

\[
\mathcal{B}_{ik} = \begin{cases} +1 & \text{if } i \text{ is the positive end of } k \\ -1 & \text{if } i \text{ is the negative end of } k \\ 0 & \text{otherwise.} \end{cases}
\]

Consequently, the overall dynamical system describing the microgrid behaviour can be written compactly for all DGUs

\(^*\)Because of the page limitation, we restrict the analysis to ZI loads.

\(^1\)Note that, without loss of generality, in (1) we use \( u_i \) instead of \( \delta_i V_{DCi} \), where \( \delta_i \) is the duty cycle of the converter \( i \) and \( V_{DCi} \) is the constant DC voltage provided by a generic (voltage) energy source at node \( i \).
\( i \in V \) as

\[
L_i \dot{I}_i = -V + u \\
\dot{L}I = -RI - B^\top V \\
C_i \dot{V} = I_t + BI - Z_i^{-1}V - I_t,
\]

(4)

where \( I_t, I_v, V, u \in \mathbb{R}^n \), and \( I \in \mathbb{R}^m \). Moreover, \( C_t, L_t, Z_t \in \mathbb{R}^{n \times n} \) and \( R, L \in \mathbb{R}^{m \times m} \) are positive definite diagonal matrices, e.g., \( C_t = \text{diag}(C_{t1}, \ldots, C_{tn}) \).

**Remark 1:** (Kron reduction). Note that in (1), the loads are located at the Point of Common Coupling (PCC) of each DGU (see also Figure 1). This configuration can generally be obtained by a Kron reduction of the original network (with arbitrary interconnections of generation and load nodes), yielding an equivalent representation of the network [17].

### III. Problem Formulation: Current Sharing and Voltage Regulation

In this section, we formulate two common control objectives in DC microgrids. First, we notice that for given constant input \( \pi \), a steady state solution \((I_t, I, V)\) to system (4) satisfies

\[
\bar{V} = \pi \quad \text{(5a)} \\
\bar{I} = -R^{-1}B^\top \bar{V} \quad \text{(5b)} \\
\bar{I}_t = -B^\top l + Z_i^{-1} \bar{V} + I_l \quad \text{(5c)}
\]

Equation (5c) implies that at the steady state the total generated current \( \mathbb{1}^\top I_t \) is equal to the total current \( \mathbb{1}^\top (Z_i^{-1} l + I_l) \) demanded by \( \mathbb{1}V \). In order to achieve an efficient demand and supply matching, so avoiding the over stressing of a source, it is generally desired that the total demand of the microgrid is shared among all the DGUs proportionally to the generation capacity of their corresponding energy sources (fair current sharing). This desire is equivalent to achieve \( w_i I_{t,i} = w_j I_{t,j} \) for all \( i, j \in V \), where a relatively large value of \( w_i \) corresponds to a relatively small generation capacity of DGU \( i \). Consequently, we formulate the first control objective concerning with the steady state value of the generated currents \( I_t \):

**Objective 1:** (Current sharing).

\[
\lim_{t \to \infty} I_{t,i} = \bar{I}_t = W^{-1} l_i^\ast,
\]

(6)

with \( W = \text{diag}(w_1, \ldots, w_n) \), \( w_i > 0 \), for all \( i \in V \) and \( l_i^\ast \) any scalar.

Note that the steady state requirement \( \mathbb{1}^\top I_t = \mathbb{1}^\top (Z_i^{-1} l + I_l) \) implies that \( l_i^\ast = \mathbb{1}^\top (Z_i^{-1} l + I_l) / (\mathbb{1}^\top W^{-1} l) \). Before formulating the second control objective concerning with the steady state value of the PCC voltages \( V \), we assume that for every DGU \( i \), there exists a nominal reference voltage \( V_i^\ast \):

**Assumption 1:** (Nominal voltages). There exists a reference voltage \( V_i^\ast \in \mathbb{R}_{>0} \) at the PCC, for all \( i \in V \).

Achieving Objective 1 prescribes the value of the required differences in voltages among the nodes of the network. As a consequence, it is generally not possible to control the voltage at each node towards the corresponding desired value. Followig [11], [12], we aim at achieving (weighted) average voltage regulation, where the sources with the largest generation capacity determine the grid voltage. Then, we select a weight of \( 1/w_i \) for all \( i \in V \), leading to the second objective:

**Objective 2:** (Average voltage regulation).

\[
\lim_{t \to \infty} \mathbb{1}^\top W^{-1} V(t) = \mathbb{1}^\top W^{-1} \bar{V} = \mathbb{1}^\top W^{-1} V_i^\ast.
\]

(7)

### IV. The Proposed Solution: A Passivity-Based Approach

In this section, we introduce the key aspects of the proposed solution to simultaneously achieve Objective 1 and Objective 2, consisting of a passivity-based distributed control algorithm. To permit the controller design, the following assumption is introduced on the available information of system (4):

**Assumption 2:** (Available informations). The current \( I_{t,i} \) is measurable at DGU \( i \in V \).

Before proposing a distributed controller achieving the objectives discussed in the previous section, we study the passivity property of system (4), proposing a Krasovskii-type storage function (see [18]–[21] for more details), which depends on the first time derivative of the states of system (4). For this reason, we consider the following extended dynamics\(^5\) of system (4)

\[
L_t \dot{I}_t = -V + u \\
L \dot{I} = -RI - B^\top V \\
C_t \dot{V} = I_t + BI - Z_i^{-1}V - I_t \\
L_i \dot{I}_t = -\dot{V} + v \\
L \dot{I} = -RI - B^\top \dot{V} \\
C_t \dot{V} = I_t + BI - Z_i^{-1} \dot{V} \\
\dot{u} = v.
\]

Then, the following result can be proved.

**Lemma 1:** (Passivity property of (8)). Let Assumptions 1 and 2 hold. System (8) is passive with respect to the supply rate \( v^\top \dot{I}_t \) and the storage function

\[
S_1(\dot{I}_t, \dot{V}) = \frac{1}{2} \dot{I}_t^\top L_t \dot{I}_t + \frac{1}{2} \dot{V}^\top C_t \dot{V}.
\]

(9)

**Proof:** A straightforward calculation shows that the storage function \( S_1 \) in (9) satisfies

\[
\dot{S}_1 = -\dot{I}^\top R \dot{I} - \dot{V}^\top Z_i^{-1} \dot{V} + v^\top \dot{I}_t \leq u^\top \dot{I}_t,
\]

(10)

along the solutions to (8), which concludes the proof. \( \blacksquare \)

To permit the design of a distributed controller achieving Objective 1, we exploit a communication network where each\(^6\)

\[^{5}\text{The state variables and the input of the extended system are } \dot{I}_t, I, V, \dot{I}_t, I, V, u \text{ and } v, \text{ respectively.}\]

\[^{6}\text{The incidence matrix } B \text{ satisfies } 1^\top B = 0, \text{ where } 1 \in \mathbb{R}^n \text{ is the vector consisting of all ones.}\]

\[^{1}\text{Often the values for } V_i^\ast \text{ are chosen identical for all } i \in V. \text{ However, the control scheme that we propose in Section IV permits to select also non-identical values for } V_i^\ast.\]
DGU shares the information with its neighbouring DGUs. We make the following assumption on the communication network:

**Assumption 3: (Communication network).** The graph $G^c = (V, E^c)$ corresponding to the topology of the communication network is undirected and connected, where $E^c = \{1, ..., m_c\}$ represents the set of the communication links between the DGUs.

Then, the communication network topology is described by its corresponding incidence matrix $B^c \in \mathbb{R}^{n \times m_c}$, which is defined similarly to $B$ in (3). Let $L_c = B^c \Gamma(B^c)^\top$ be the (weighted) Laplacian matrix associated to the communication network, where $\Gamma \in \mathbb{R}^{m_c \times m_c}$ is a positive definite diagonal matrix describing the weights on the edges.

**Remark 2: (Suggested consensus protocol).** Since the output port-variable $I_t$ is integrable, then Lemma 1 suggests as a candidate storage function $S = S_1 + \sigma(I_t)$, where $S_1$ is given by (9) and the function $\sigma: \mathbb{R}^n \to \mathbb{R}_{>0}$ is chosen such that $S$ has a minimum satisfying Objective 1. Then, $\sigma(I_t) = \frac{1}{2}(L^cW_lI_t)^\top(L^cW_lI_t)$ has a minimum at $L^cW_lI_t = 0$, which implies $W_lI_t \in \text{im}(I)$ (see Objective 1).

Consequently, Remark 2 suggests to augment system (4) with additional state variables (distributed integrators) $\theta_i, i \in V$, with dynamics given by

$$\dot{\theta}_i = \sum_{j \in N_i^c} \gamma_{ij}(w_i I_{ti} - w_j I_{tij}),$$  

where $N_i^c$ is the set of the DGUs that communicate with the DGU $i$, and $\gamma_{ij} = \gamma_{ji} \in \mathbb{R}_{>0}$ are the entries of $\Gamma$, i.e., the edge weights. Then, the dynamics in (11) can be expressed compactly for all nodes $i \in V$ as

$$\dot{\theta} = L^cW_lI_t,$$

that indeed has the form of a consensus protocol, permitting a steady state where $W_lI_t \in \text{im}(I)$ (see Objective 1 and Remark 2).

Following the procedure suggested in [15], we now interconnect the dynamical physical system (4) with the dynamical cyber system (12) by choosing

$$u = -W L^c \theta + u_c,$$

yielding the following dynamical cyber-physical system

$$L_c I_t = -V - W L^c \theta + u_c$$
$$L \dot{I} = -RI - B^\top V$$
$$C_l \dot{V} = I + BI - Z_l^{-1} V - I_t$$
$$\dot{\theta} = L^cW_lI_t,$$

where $u_c$ is the control input to be designed. Before designing $u_c$, we study the passivity property of system (14), proposing again a Krasovskii-type storage function. Consider first the extended dynamics** of system (14).

**Song 3: (Average voltage regulation).** Note that, at steady state, after pre-multiplying both sides of (15a) by $I^\top W^{-1}$, one obtains $I^\top W^{-1} \dot{V} = I^\top W^{-1} \Pi_c$. As a consequence, regulating $u_c$ towards $V^*$ ensures that Objective 2 is achieved. We take this into account in the choice of the desired storage function in Theorem 1.

Before introducing the main result of this work, we assume that a steady state solution to system (15) exists:

**Lemma 3: (Existence of a unique steady state solution).** Let Assumptions 1 and 3 hold. Moreover, let $u_c = V^*$ and $v_c = 0$. There exists a unique steady state solution $(I_t, \dot{I}, \dot{V}, \theta, 0, 0, 0, 0, V^*)$ to system (15), satisfying Objective 1 and Objective 2.††

We can now show that the solutions to (15) converge to a steady state, achieving Objective 1 and Objective 2.

**Theorem 1: (Main result).** Let Assumptions 1–3 hold. Consider system (15) controlled by

$$v_c = -K_d^{-1} I_t - K_d^{-1} K_p(u_c - V^*),$$

**The state variables and the input of the extended system are $I_t, I, V, \theta, I_c, \dot{I}, \dot{V}, \dot{\theta}, u_c$ and $v_c$, respectively.

††The storage function $S_2$ in (16) depends on the states $I_t, \dot{V}, \dot{I}$ and $\dot{\theta}$. Consequently, according to [22, Remark 2], $S_2$ depends also on $I_t, V, I, \theta$ and $u_c$, i.e., the entire state of the auxiliary system (15).

††Let $G := BR^{-1} B^\top + Z_l^{-1}$. It can be proved that $G \dot{V} + I_t, (5b), \dot{V} = -W L^c Z_l^{-1} \dot{V} + V^*, \ddot{\theta} = [L]^\top [I \ddot{\theta}(0)]$ where $b := L^cW(GV^* + I_t)$ and $L := L^cWGWL^c$.
where $K_p, K_d \in \mathbb{R}^{n \times n}$ are positive definite diagonal matrices. Then, the solutions to system (15) controlled by (18) converge to the desired steady-state, satisfying Objective 1 and Objective 2.

Proof: Consider the desired storage function (see also Remark 3)

$$S = S_2 + \frac{1}{2}(u_c - V^*)^\top K_p(u_c - V^*),$$

(19)

where $S_2$ is given by (16). It is immediate to see that $S$ attains a minimum at $(\dot{T}_i, \dot{T}, \dot{V}_i, \dot{\theta}, 0, 0, 0, 0, V^*)$. Furthermore, $S$ satisfies

$$\dot{S} = -\dot{I}^\top R \dot{I} - \dot{V}^\top Z_i^{-1} \dot{V} + \dot{u}_c^\top \dot{I}_t + (u_c - V^*)^\top K_p \dot{u}_c$$

$$= -\dot{I}^\top R \dot{I} - \dot{V}^\top Z_i^{-1} \dot{V} + \dot{u}_c^\top (\dot{I}_t + K_p(u_c - V^*))$$

$$= -\dot{I}^\top R \dot{I} - \dot{V}^\top Z_i^{-1} \dot{V} - \dot{u}_c^\top K_d \dot{u}_c$$

(20)

along the solutions to (15). According to LaSalle’s invariance principle, the solutions to (15) approach the largest invariant set contained entirely in the set

$$\mathcal{Y} = \{I_t, I, V, \theta, \dot{I}_t, \dot{I}, \dot{V}, \dot{\theta}, u_c : \dot{I} = 0, \dot{V} = 0, \dot{u}_c = 0\},$$

(21)

implying that, on this set $\mathcal{Y}$, $I_t = T_i$, $V = V^*$ and $u_c = \pi_c$ are constant vectors. Furthermore, on this set $\mathcal{Y}$, it follows from (15g) that $\dot{I}_t = 0$, i.e., also $I_t = T_i$ is a constant vector. Then, from (18) it follows that, on this set $\mathcal{Y}$, $\pi_c = V^*$. Furthermore, on this set $\mathcal{Y}$, equation (15e) satisfies $W^\top \pi_c = 0$, i.e., $\pi_c = I_1 \alpha, \alpha \in \mathbb{R}$ (or equivalently $W^\top T_i = I_1 \alpha$). Consequently, $I^\top W^\top T_i = I^\top I_1 \alpha$ implies $\alpha = 0$. This further implies $L_1^\top W^\top T_i = 0$, achieving Objective 1, and $\dot{\theta} = 0$, i.e., $\theta = \overline{\theta}$ is a constant vector. Finally, pre-multiplying both sides of (15a) by $I^\top W^{-1}$, one obtains $I^\top W^{-1} \dot{V} = I^\top W^{-1} V^*$, achieving Objective 2.

Remark 4: (Alternative controller). Note that controller (18) requires the information of $I_t$, which could be affected by error measurements. In order to avoid this controller (18) can be replaced by

$$u_c = \phi - K_d^{-1} I_t$$

$$K_d \phi = -K_p(u_c - V^*)$$

(22)

Then, the same results of Theorem 1 can be straightforwardly proved.

Remark 5: (Robustness and Plug-and-Play). Note that the proposed controller (18) (or (22)) does not require the information of the load, and the stability analysis in Theorem 1 does not depend on the value of $Z_l$ and $I_l$. Moreover, even if we assume a constant network topology, since the convergence result of Theorem 1 holds globally, independently of the initial conditions of the physical power network and the controller state, the proposed solution is expected to show Plug-and-Play capabilities. However, the analysis of the corresponding switched system is outside the scope of this work.

Remark 6: (ZIP loads). Similarly to [22], if constant power loads are also considered, it can be proved that Lemma 1, Lemma 2 and Theorem 1 hold locally in a neighborhood of the equilibrium, where the trajectories of the controlled system satisfy $Z_i^{-1} - V_i^{-1} P_i > 0$ for all $i \in \mathcal{V}$, $P_i$ being the constant power demand of load $i$.

V. SIMULATION RESULTS

In this section, the control strategy proposed in Section IV is assessed in simulation. We consider a microgrid composed of four DGUs interconnected as shown in Figure 2, where also the communication network is represented. The parameters of each DGU and the line parameters are reported in Tables II and III, respectively. The weights associated with the edges of the communication graph are $\gamma_{12} = \gamma_{23} = \gamma_{34} = 1 \times 10^3$. In the controller (18), we have selected $K_d = I_4$ and $K_p = 100 \times I_4$, $I_4 \in \mathbb{R}^{4 \times 4}$ being the identity matrix.

The system is initially at a steady state with load impedance $Z_l(0)$ and current $I_l(0)$. Then, consider a load current variation $\Delta I_l$ at the time instant $t = 3$ s (see Table II). The PCC voltages and the average voltage of the network are illustrated in Figure 3 (a) and (b), respectively. One can appreciate that the steady state weighted average of the PCC voltages (denoted by $V_{\text{ave}}$) is equal to the weighted average of the corresponding references (see Objective 2). Figure 3 (c) shows that the current generated by each DGU converges to the desired value, achieving proportional current sharing (see Objective 1), while Figure 3 (d) illustrates the currents shared among the DGUs through the lines of the network.
In this paper, a distributed passivity-based control scheme is proposed for achieving at the steady state proportional (fair) current sharing and regulating the average value of the voltages of a DC microgrid that includes buck converters, unknown “ZIP” (constant impedance, constant current, constant power) loads and dynamic resistive-inductive lines. The control objectives are achieved by designing a consensus-like protocol requiring that each node of the microgrid (physical system) shares information with its neighbouring nodes through a communication network (cyber system). The controlled cyber-physical system is proven to converge globally to a desired steady state, independently of the initial conditions of the system states. Interesting future research includes the analysis of different converter types, such as boost converters [8], [10].

VI. CONCLUSIONS

In this paper, a distributed passivity-based control scheme is proposed for achieving at the steady state proportional (fair) current sharing and regulating the average value of the voltages of a DC microgrid that includes buck converters, unknown “ZIP” (constant impedance, constant current, constant power) loads and dynamic resistive-inductive lines. The control objectives are achieved by designing a consensus-like protocol requiring that each node of the microgrid (physical system) shares information with its neighbouring nodes through a communication network (cyber system). The controlled cyber-physical system is proven to converge globally to a desired steady state, independently of the initial conditions of the system states. Interesting future research includes the analysis of different converter types, such as boost converters [8], [10].

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