Linear relation between $\text{H}\, \text{I}$ circular velocity and stellar velocity dispersion in early-type galaxies, and slope of the density profiles

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Accepted 2016 April 26. Received 2016 April 26; in original form 2016 March 6

ABSTRACT

We report a tight linear relation between the $\text{H}\, \text{I}$ circular velocity measured at $6\, R_e$ and the stellar velocity dispersion measured within $1\, R_e$ for a sample of 16 early-type galaxies with stellar mass between $10^{10}$ and $10^{11}\, M_\odot$. The key difference from previous studies is that we only use spatially resolved $v_{\text{circ}}(\text{H}\, \text{I})$ measurements obtained at large radius for a sizeable sample of objects. We can therefore link a kinematical tracer of the gravitational potential in the dark-matter dominated outer regions of galaxies with one in the inner regions, where baryons control the distribution of mass. We find that $v_{\text{circ}}(\text{H}\, \text{I}) = 1.33\, \sigma_\text{c}$ with an observed scatter of just 12 per cent. This indicates a strong coupling between luminous and dark matter from the inner- to the outer regions of early-type galaxies, analogous to the situation in spirals and dwarf irregulars. The $v_{\text{circ}}(\text{H}\, \text{I}) – \sigma_\text{c}$ relation is shallower than those based on $v_{\text{circ}}$ measurements obtained from stellar kinematics and modelling at smaller radius, implying that $v_{\text{circ}}$ declines with radius – as in bulge-dominated spirals. Indeed, the value of $v_{\text{circ}}(\text{H}\, \text{I})$ is typically 25 per cent lower than the maximum $v_{\text{circ}}$ derived at $\sim 0.2\, R_e$ from dynamical models. Under the assumption of power-law total density profiles $\rho \propto r^{-\gamma}$, our data imply an average logarithmic slope $\langle \gamma \rangle = 2.18 \pm 0.03$ across the sample, with a scatter of 0.11 around this value. The average slope and scatter agree with recent results obtained from stellar kinematics alone for a different sample of early-type galaxies.

Key words: galaxies: elliptical and lenticular, cD – galaxies: kinematics and dynamics – galaxies: structure.

1 INTRODUCTION

The distribution of mass in galaxies continues to be the subject of intense debate. The situation is clear at large radius: stellar kinematics, gas kinematics and gravitational lensing show that a dark matter of unknown nature dominates the gravitational potential of most galaxies (assuming Newtonian dynamics). In these regions the rotation curves are approximately flat and the total density profiles close to isothermal (Bosma 1978, 1981; van Albada et al. 1985; Gavazzi et al. 2007; Cappellari et al. 2015, hereafter C15). Well inside galaxies’ stellar body the situation is much more diverse but, in these regions, baryons and dynamics are closely connected (Sancisi 2004; Swaters et al. 2012; Lelli, Fraternali & Verheijen 2013): in low-surface-brightness galaxies, rotation curves rise slowly and dark matter dominates the potential (de Blok, McGaugh & Rubin 2001); in high-surface-brightness galaxies, rotation curves rise fast to approximately (or slightly above) their flat part, and baryons constitute most of the mass (van Albada et al. 1985; Kent 1987; Sackett 1997; Palunas & Williams 2000; Cappellari et al. 2006, 2013a, hereafter C13; Noordermeer et al. 2007).

This situation is reflected in the observed correlation between galaxies’ circular velocity $v_{\text{circ}}$ measured at the largest possible radius and the stellar velocity dispersion $\sigma$ measured in the central
regions of the stellar body (Whitmore, Schechter & Kirshner 1979; Gerhard et al. 2001; Ferrarese 2002; Baes et al. 2003; Pizzella et al. 2005, hereafter P05; Courteau et al. 2007, hereafter C07; Ho 2007, C13). In particular, the slope of this correlation depends on galaxy surface brightness in a way that, to first order, can be linked to the shape of the rotation curve (C07; Kormendy & Bender 2011). In simple terms, σ traces the inner gravitational potential and can be related to the circular velocity measured well within the stellar body. If the rotation curve has already reached its flat part in the regions where σ is measured (as in high-surface-brightness disc galaxies) then \( v_{\text{circ}} \sim 1.4 \sigma \), close to the theoretical expectation for an isothermal density profile. However, if the rotation curve is still rising (as in low-surface-brightness galaxies) σ is lower and the \( v_{\text{circ}}-\sigma \) relation is steeper, while if the rotation curve declines at large radius (as in early-type spirals) the relation should be shallower.

Rotation curves and the correlation between \( v_{\text{circ}} \) and σ are powerful tools to investigate the relative distribution of baryons and dark matter in galaxies of different type, provided that \( v_{\text{circ}} \) is measured all the way to the dark-matter dominated outer regions. This is relatively straightforward for late-type galaxies, where the abundant and dynamically cold H I traces the potential well outside the stellar body. Indeed, for such objects, resolved H I observations have been used in this field for decades (e.g. Bosma 1978; Begeman, Broeils & Sanders 1991; Verheijen 2001; Martinsson et al. 2016).

In contrast, in early-type galaxies (ellipticals and lenticulars; hereafter ETGs) H I is detected less frequently and usually other methods must be used to measure \( v_{\text{circ}} \). Complex modelling of the stellar kinematics is generally required but this is typically limited to relatively small radius, comparable to the half-light radius \( R_e \) (Kronawitter et al. 2000; Gerhard et al. 2001; Wegner et al. 2012, C13). The resulting rotation curves and \( v_{\text{circ}}-\sigma \) relations apply therefore only to the baryon-dominated regions of these galaxies and do not cover the transition to the dark-matter dominated outskirts. As such, they provide limited information about the relation between baryons and dark matter in ETGs. Apart for a few individual objects (e.g. Napolitano et al. 2009, 2014; Weijmans et al. 2009; Murphy, Gebhardt & Adams 2011), the only notable exception is the study of C15, whose dynamical models of 14 ETGs reach a median radius of 4 \( R_e \).

Among the above studies, only Ho (2007) provides measurements of \( v_{\text{circ}} \) for a large number of ETGs based on H I data, potentially probing the dark-matter dominated regime. However, these values are derived from unresolved H I spectra obtained with single dish telescopes, and the uncertainty on the dynamical state and geometry of the detected gas results in no significant correlation between \( v_{\text{circ}}(\text{H I}) \) and σ. More reliable, resolved \( v_{\text{circ}}(\text{H I}) \) measurements at large radius are available for a handful of ETGs included in the samples of P05 and C07. However, both samples are dominated by galaxies whose \( v_{\text{circ}} \) is estimated from stellar kinematics and dynamical modelling at small radius. Neither P05 nor C07 derive a \( v_{\text{circ}}-\sigma \) relation for ETGs based on resolved H I data alone. We discuss these studies in more detail in Section 3.

Here we take a step forward by using new, interferometric \( v_{\text{circ}}(\text{H I}) \) estimates obtained at a median radius of 6 \( R_e \) by den Heijer et al. (2015, hereafter dH15) for a sample of 16 ETGs. Thanks to the size of this sample we are able to establish a tight linear \( v_{\text{circ}}-\sigma \) relation for ETGs using solely \( v_{\text{circ}} \) values derived within the dark-matter dominated regime from resolved H I data. We further combine our \( v_{\text{circ}}(\text{H I}) \) estimates with models by C13 to study the typical shape of the rotation curve in these objects, and measure the average slope of their density profiles out to large radius.

# 2 Sample and Data

We analyse a sample of 16 nearby ETGs drawn from the ATLAS3D sample (Cappellari et al. 2011). All galaxies and quantities used for this work are listed in Table 1. Galaxies are selected for hosting a regular H I disc or ring, which allows the determination of \( v_{\text{circ}}(\text{H I}) \) at large radius. The selection is based on a large set of interferometric H I observations and data products presented by Serra et al. (2012, 2014) for ~150 galaxies. This data set was largely assembled as part of the ATLAS3D project but includes earlier data taken by Morganti et al. (2006), Weijmans et al. (2008), Józsa et al. (2009) and Oosterloo et al. (2010). The H I kinematics was modelled by

<table>
<thead>
<tr>
<th>Name</th>
<th>( R_e ) (arcsec)</th>
<th>( \sigma_e ) (km s(^{-1}))</th>
<th>( R_{\text{max}} ) (arcsec)</th>
<th>( v_{\text{circ}}(\text{JAM}) ) (km s(^{-1}))</th>
<th>( R_{\text{H I}} ) (arcsec)</th>
<th>( v_{\text{circ}}(\text{H I}) ) (km s(^{-1}))</th>
<th>( \gamma )</th>
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<tr>
<td>NGC 2685</td>
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<td>277</td>
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<td>115</td>
<td>215 ± 41</td>
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<td>226</td>
<td>7.9</td>
<td>369</td>
<td>130</td>
<td>310 ± 10</td>
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<td>187</td>
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<td>0.9</td>
<td>209</td>
<td>60</td>
<td>144 ± 14</td>
<td>2.18 ± 0.05</td>
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</tbody>
</table>

Column 1: galaxy name; Column 2: circularized projected half-light radius from C13; Column 3: stellar velocity dispersion measured from integral-field spectroscopy within the half-light ellipse (uncertainty ~5 per cent; C13); Column 4: radius of the peak circular velocity of the JAM models (C13); Column 5: peak circular velocity of the JAM models (uncertainty ~5 per cent; C13); Column 6: radius where dH15 measure the H I circular velocity; Column 7: H I circular velocity (dH15); Column 8: average logarithmic slope γ of the density profile \( \rho \propto r^{-\gamma} \) calculated using equation (4).
where the value 150 km s\(^{-1}\) was adopted to minimize the covariance between the fit parameters (C13). The observed r.m.s. scatter around this relation is 0.049 dex (12 per cent). The intrinsic scatter is 0.036 ± 0.016 dex (9 ± 4 per cent).

The value of the power-law exponent in equation (1) is consistent with unity. Indeed, Fig. 1 shows that, within the \(\sigma_e\) range of our sample, the best-fitting power law is fully compatible with the linear relation:

\[
v_{\text{circ}}(H) = 1.33 \, \sigma_e, \tag{2}
\]

where the uncertainty on the slope is 3 per cent. The scatter around this relation is 12 per cent, identical to the scatter around the best-fitting power law. This is the first time that such a tight, linear relation is found using \(v_{\text{circ}}\) measurements obtained at such a large radius (\(~6 R_e\)) from the resolved H\textsc{i} kinematics of a sizeable sample of ETGs. In Section 3.2 we support this claim by performing a detailed comparison between this result and previous work.

The existence of a correlation between \(v_{\text{circ}}(H)\) and \(\sigma_e\) for ETGs is expected given that \(\sigma_e\) correlates with \(L_K\) (Faber & Jackson 1976) and \(L_K\) correlates with \(v_{\text{circ}}(H)\) (dH15). However, the actual linearity, slope and scatter of the relation, which we establish here, are not trivial. In particular, its linearity implies that the \(L_K\)–\(\sigma_e\) power-law relations have identical exponents, in agreement with general predictions of the Modified Newtonian Dynamics (Milgrom 1984).

Importantly, the \(v_{\text{circ}}(H)\)–\(\sigma_e\) relation is relatively free of systematics as both quantities involved are independent of distance and stellar mass-to-light ratio (unlike in other galaxy scaling relations), and have small errors. The main source of uncertainty on \(v_{\text{circ}}(H)\) is the inclination of the gas disc, which results in a typical error below 10 per cent (dH15; Table 1). The uncertainty on \(\sigma_e\) is ~5 per cent (C13).

The small intrinsic scatter of the \(v_{\text{circ}}(H)\)–\(\sigma_e\) relation is particularly interesting. In Sections 3.2 and 3.3 we discuss evidence that \(v_{\text{circ}}\) declines with radius in ETGs, and this raises the question of whether some of this scatter is related to the relatively large range of \(R_{\text{HI}}\) values covered by our sample. We investigate this aspect in Fig. 2. The figure shows no clear trend between the deviation from the relation and \(R_{\text{HI}}/R_e\); galaxies where \(v_{\text{circ}}(H)\) is measured at larger (lower) radius are not systematically below (above) the relation. This suggests that other factors drive the observed scatter. An important contribution might come from the scatter in the shape of the ETG rotation curves. This can be linked to the scatter in the mass–concentration relation of dark matter haloes predicted by dark-matter-only simulations (Dutton & Macciò 2014). In the future it will be interesting to test whether the intrinsic scatter of the \(v_{\text{circ}}(H)\)–\(\sigma_e\) relation is consistent with these simulations (see Dutton 2012; Lelli, McGaugh & Schombert 2016 for a similar test based on the intrinsic scatter of the baryonic Tully–Fisher relation).

The relation between \(v_{\text{circ}}(H)\) and \(\sigma_e\) is remarkable as the two quantities are measured in completely independent ways and, unlike in previous work, trace the gravitational potential in two extremely different regimes of the distribution of matter: \(\sigma_e\) is measured in a region where the luminous matter constitutes on average 85 per cent of the mass (C13); while \(v_{\text{circ}}(H)\) is measured in a region where dark matter accounts for basically all of the mass (the total dynamical mass within \(R_{\text{HI}}\) is on average \(~3\) times the total stellar mass estimated by C13). This tight correlation suggests that galaxies in our sample all have roughly the same overall distribution of mass – another manifestation of the poorly understood coupling between

3 RESULTS

3.1 Linear relation between \(v_{\text{circ}}(H)\) and \(\sigma_e\)

We plot \(v_{\text{circ}}(H)\) against \(\sigma_e\) in Fig. 1. The figure shows a strong correlation between these two quantities. A power-law fit to our data performed as a linear fit in logarithmic space with the LTS_LINEFIT software (C13) results in:

\[
\log \frac{v_{\text{circ}}(H)}{\text{km s}^{-1}} = (2.299 \pm 0.013) + (0.96 \pm 0.11) \times \log \frac{\sigma_e}{150 \text{ km s}^{-1}},
\]

Figure 1. Relation between \(v_{\text{circ}}(H)\) and \(\sigma_e\). Dashed and solid lines show the best-fitting power-law and linear relation, respectively, obtained for our sample of 16 ETGs (see Section 3.1 and legend). The dotted line is a linear fit (with zero intercept) to the P05 data, noting that for consistency with our work we correct their \(\sigma_e\) measurements to an aperture of radius 1 \(R_e\) (see Section 3.2 for details). We do not correct the \(\sigma_e\) values of Ho (2007) because that sample shows no correlation between \(v_{\text{circ}}(H)\) and \(\sigma_e\) in the first place (Section 3.2), and the correction is irrelevant for the purpose of our comparison.

dH15 for all but two galaxies for which literature values were used: NGC 2685 (Józsa et al. 2009) and NGC 2974 (Weijmans et al. 2008). Here we make use of the \(v_{\text{circ}}(H)\) values measured at the largest possible radius \(R_{\text{HI}}\) and listed by dH15. The \(R_{\text{HI}}\) values fall in the range 4–16 \(R_e\), and their median is \(~6 R_e\).

All galaxies in the sample were observed with optical integral-field spectroscopy as part of the SAURON project (4 galaxies; de Zeeuw et al. 2002) or ATLAS1D (12 galaxies; Cappellari et al. 2011). Here we make use of the stellar velocity dispersion measurements \(\sigma_e\) within a 1 \(R_e\) aperture given in C13. The same paper describes Jeans anisotropic modelling of the stellar kinematics of these galaxies (JAM; Cappellari 2008). Here use the maximum circular velocity \(v_{\text{circ}}^{\text{max}}\) (JAM) values predicted by the JAM models at the radius \(R_{\text{max}}\). For this work we use JAM models (A), which assume that mass follows light and are appropriate for the central regions of galaxies. The values of \(R_{\text{max}}\) fall in the range 0.1–0.4 \(R_e\) (median \(~0.2 R_e\)).

This sample does not have any strong bias on the mass-size plane of ETGs, and the 16 galaxies cover a representative range of bulge-to-disc ratio (as traced by \(\sigma_e\)) in the stellar mass range \(10^{10}–10^{11} M_{\odot}\) (dH15). Bearing in mind the small sample size, the conclusions of this work should hold for the general early-type population within this mass range and with \(\sigma_e\) between 100 and 250 km s\(^{-1}\).
the distribution of luminous matter and total mass in galaxies (van Albada & Sancisi 1986; Sancisi 2004; Swaters et al. 2012; Lelli et al. 2013). We will return to this point in Section 3.4.

3.2 Comparison with previous $v_{\text{circ}}$–$\sigma_e$ relations

3.2.1 $v_{\text{circ}}$ from $H_\text{i}$ kinematics

The only previous study of the $v_{\text{circ}}$–$\sigma_e$ relation of ETGs entirely based on $H_\text{i}$ data is that of Ho (2007), whose sample includes $\sim$100 ellipticals and lenticulars. However, that work makes use of single-dish unresolved $H_\text{i}$ data, which give no information about the dynamical state and geometry of the gas. In order to derive $v_{\text{circ}}$ from unresolved spectra one must assume that (i) the $H_\text{i}$ is on a rotating disc and (ii) the disc has the same inclination of the stellar body. These two assumptions are in error for more than half of all $H_\text{i}$-rich ETGs (Serra et al. 2012, 2014), resulting in inaccurate single-dish $v_{\text{circ}}(H_\text{i})$ values for this type of galaxies. It is likely for this reason that $v_{\text{circ}}(H_\text{i})$ and $\sigma_e$ do not correlate significantly for the ETG sample of Ho (2007), as shown in Fig. 1. We have independently obtained a Spearman correlation coefficient of 0.41 (with $p$-value 0.17) for that sample, confirming the visual impression given by the figure.

Ho (2007) finds that $v_{\text{circ}}(H_\text{i})$ and $\sigma_e$ do correlate if they limit their analysis to a subsample of ETGs selected to follow the $v_{\text{circ}}(H_\text{i})$–$L_K$ (Tully–Fisher) relation of spirals. However, we argue that for such a subsample the $v_{\text{circ}}(H_\text{i})$–$\sigma_e$ relation is a selection effect. A Tully–Fisher selection will always result in a $v_{\text{circ}}(H_\text{i})$–$\sigma_e$ relation – even if none existed and regardless of the quality of the $v_{\text{circ}}(H_\text{i})$ estimates – because of the tight $\sigma$–$L_K$ (Faber–Jackson) relation of ETGs. Furthermore, the shape and scatter of the resulting $v_{\text{circ}}(H_\text{i})$–$\sigma_e$ relation will be entirely determined by the details of the Tully–Fisher selection rather than by the properties of the galaxies being studied. Our galaxies, too, follow the Tully–Fisher relation (dH15), but they are not selected to do so. Therefore, the existence, shape and scatter of our $v_{\text{circ}}(H_\text{i})$–$\sigma_e$ relation fully reflect the properties of the ETGs in our sample rather than the way they are selected.

The only previous studies of the $v_{\text{circ}}$–$\sigma_e$ relation to overcome the limitations of single-dish data and include resolved $v_{\text{circ}}(H_\text{i})$ measurements for ETGs are those by P05 and, using the same $H_\text{i}$ data, C07. The main difference from our analysis is that the number of $H_\text{i}$ measurements used is very small – just 5. Apart from these five objects, those ETG samples are dominated by $v_{\text{circ}}$ values obtained at a radius comparable with $R_e$ from stellar kinematics and dynamical modelling (discussed in Section 3.2.2), and these authors do not derive an ETG $v_{\text{circ}}$–$\sigma_e$ relation based on $H_\text{i}$ data alone. Nevertheless, in this Section we discuss whether the tight linear relation $v_{\text{circ}}(H_\text{i}) = 1.33 \sigma_e$ obtained in Section 3.1 from our data could have been derived from the five ETGs with $H_\text{i}$ data included in the P05 and C07 samples.

Fig. 1 shows those five ETGs on the $v_{\text{circ}}(H_\text{i})$–$\sigma_e$ plane. An important detail is that P05 and C07 use $\sigma$ measurements obtained within (or corrected to) an $R_e$/8 aperture. For consistency with our work we correct those values to a 1 $R_e$ aperture multiplying them by a factor 0.872 derived from equation (1) of Cappellari et al. (2006). The accuracy of (and need for) this correction can be easily verified considering the two ETGs in common with our sample, NGC 2974 and NGC 4278.

As a whole, the five ETGs of P05 and C07 appear systematically offset towards high $v_{\text{circ}}(H_\text{i})$ relative to our sample in Fig. 1. Furthermore, they do not follow a linear $v_{\text{circ}}(H_\text{i})$–$\sigma_e$ relation. The best-fitting power law obtained with the same LTS_linefit software used in Section 3.1 has an exponent of 0.59 ± 0.17. This is significantly non-linear, unlike our equation (1). Assuming linearity, the slope of the relation defined by those five ETGs and obtained with an orthogonal distance regression fit of a linear relation through the origin is 1.76 with a 6 per cent uncertainty (Fig. 1). This is $\sim$30 per cent larger than the 1.33 slope of our relation.

We note that, taken individually, none of the five ETGs studied by P05 and C07 is dramatically offset from our sample in Fig. 1. The average $\sim$30 per cent offset discussed above is most likely caused by the small number of objects combined with the large uncertainty on $v_{\text{circ}}(H_\text{i})$. More in detail, P05 adopt $v_{\text{circ}}(H_\text{i})$ values obtained from data with a velocity resolution of $\sim$40 km s$^{-1}$ for the two galaxies in common with our sample: NGC 2974 (Kim et al. 1988) and NGC 4278 (Lees 1994). Despite being consistent with our measurements within the large errors, the resulting $v_{\text{circ}}(H_\text{i})$ values of 355 ± 60 and 326 ± 40 km s$^{-1}$ obtained at $\sim$4 and $\sim$10 $R_e$, respectively, are 15 and 27 per cent larger than those in Table 1. We also note that Lees (1994) estimate $v_{\text{circ}}(H_\text{i})$ in NGC 4278 through complex modelling of the $H_\text{i}$ data cube assuming a triaxial gravitational potential at constant inclination, which may introduce systematic differences compared to the method used by dH15. For NGC 2865 P05 adopt the $v_{\text{circ}}(H_\text{i})$ estimate at $\sim$6 $R_e$ from Schiminovich et al. (1995), who remark that their assumption of coplanar circular orbits for the $H_\text{i}$ gas is not necessarily supported by their data. For NGC 5266 $v_{\text{circ}}(H_\text{i})$ comes from a study by Morganti et al. (1997), where again circular orbits are just assumed. These authors estimate $v_{\text{circ}}(H_\text{i})$ at $\sim$4 $R_e$ while at larger radius the gas disc appears unsettled. Finally, for IC 2006 – the main outlier in Fig. 1 – $v_{\text{circ}}(H_\text{i})$ is taken from Franx, van Gorkom & de Zeeuw (1994). Their analysis shows that the rotation curve of this galaxy is relatively flat. As we discuss below, this is not typical for ETGs.

The above considerations highlight that it would have been difficult for P05 to obtain a reliable slope of the $v_{\text{circ}}(H_\text{i})$–$\sigma_e$ relation based on such few objects and sometimes limited data quality. The inclusion of these five galaxies in their sample was important at the time, and that paper clearly shows that $v_{\text{circ}}(H_\text{i})$ grows with $\sigma_e$ in ETGs. However, that sample was just too small to establish the linearity, tightness and actual slope of the $v_{\text{circ}}(H_\text{i})$–$\sigma_e$ relation presented in Section 3.1.
3.2.2 $v_{\text{circ}}$ from stellar kinematics at small radius

Having established a precise $v_{\text{circ}}(H\text{i})$ relation for ETGs based on our data, we can investigate whether such a relation is identical to that obtained using kinematical data at smaller radius. This was one of the conclusions of P05: their five ETGs with a $v_{\text{circ}}(H\text{i})$ measurement follow the same $v_{\text{circ}}$–$\sigma_e$ relation obtained for a larger sample consisting of 40 high-surface-brightness spirals (with $v_{\text{circ}}$ from ionized gas or H$\text{i}$ data; see references in P05) and another 19 ETGs (with $v_{\text{circ}}$ measured within $\sim 2 R_e$ from the dynamical models of Kronawitter et al. 2000). Below we show that our data do not support this conclusion, and equation (2) is markedly shallower than relations obtained at smaller radius.

First, assuming that the relation between $v_{\text{circ}}$ and $\sigma_e$ is linear, P05 find $v_{\text{circ}} = (1.32 \pm 0.09) \sigma_e + 46 \pm 14$. This relation is significantly different from our equation (2) for two reasons. First, it has a non-zero intercept which cannot be ignored. At the median velocity dispersion of our sample ($\sim 130$ km s$^{-1}$), the intercept amounts to $\sim 20$ per cent of the $v_{\text{circ}}$ value predicted by the relation. Second, the $\sigma_e$ values used by P05 must be corrected to the $1 R_e$ aperture used in our work (Section 3.2.1). When this is done, we find that the best-fitting slope of a linear relation through the origin for the full P05 sample is 1.77, $\sim 30$ per cent larger than our value of 1.33.

A similar conclusion can be drawn for other samples dominated by $v_{\text{circ}}$ measurements at small radius. Focusing on ETGs, C07 adds to the P05 sample $\sim 50$ lenticulars with $v_{\text{circ}}$ measured by Bedregal, Aragón-Salamanca & Merrifield (2006, and references therein) based on stellar kinematics – but no new H$\text{i}$ data. Once their $\sigma_e$ values are corrected to an aperture of $1 R_e$ as above, these ETGs scatter about a $v_{\text{circ}}$–$\sigma_e$ relation of slope $\sim 1.7$ and are clearly inconsistent with our equation (2).

Likewise, our slope of 1.33 is significantly lower than the 1.52 value found by Gerhard et al. (2001). The comparison with the latter study is particularly useful to understand the cause of this difference. First, as above, we correct for the larger aperture within which we measure $\sigma_e$ ($1 R_e$ compared to $\sim 0.1 R_e$). We use again equation (1) of Cappellari et al. (2006) and find $\sigma_e = 0.859 \sigma_0.1R_e$. The other, crucial difference from this and all other previous studies of ETGs is that our $v_{\text{circ}}$ values are obtained at a much larger radius ($\sim 6 R_e$ compared to $\sim 0.3 R_e$ in the case of Gerhard et al. 2001). This difference is relevant in light of the recent findings of C15. They show that the density profiles of ETGs are somewhat steeper than isothermal, and that $v_{\text{circ}}$ decreases slowly with radius. We discuss this aspect in more detail in Sections 3.3 and 3.4, but for the moment it is sufficient to consider that on average $v_{\text{circ}} \propto r^{-0.095}$.

Therefore, our $v_{\text{circ}}$ measurements and those of Gerhard et al. (2001) are related by $v_{\text{circ}}(6R_e) = 0.752 v_{\text{circ}}(0.3R_e)$. Taken together, the two corrections transform our equation (2) from $v_{\text{circ}}(6R_e) = 1.33 \sigma_0.3R_e$ into $v_{\text{circ}}(0.3R_e) = 1.52 \sigma_0.1R_e$, which is exactly the result of Gerhard et al. (2001).

Finally, C13 derives the $v_{\text{circ}}$–$\sigma_e$ relation from dynamical models of all 260 ETGs in the volume-limited, complete ATLAS$^{3D}$ sample. They find a slope of 1.76 when using the peak $v_{\text{circ}}$ predicted by the models (typically at 0.2 $R_e$). As for the study of Gerhard et al. (2001), the larger slope compared to equation (2) can be explained by the decline of $v_{\text{circ}}$ with radius (C15 and Section 3.3).

In summary, once aperture effects on the measurement of $\sigma_e$ are taken into account, our $v_{\text{circ}}(H\text{i})$–$\sigma_e$ relation is shallower than all published relations based on $v_{\text{circ}}$ measurements at smaller radius. This suggests that $v_{\text{circ}}$ is not constant with radius and indicates the validity of the conclusions of C15 on the slow decline of $v_{\text{circ}}$. It highlights that ETG samples selected to only include objects with a flat rotation curve (as in P05) might be biased towards galaxies with a specific distribution of total mass, such that $v_{\text{circ}}$ remains high even when it is measured at relatively large radius. We explore the variation of $v_{\text{circ}}$ with radius in ETGs in the next sections.

3.3 Variation of $v_{\text{circ}}$ with radius

We compare $v_{\text{circ}}(H\text{i})$ with the circular velocity at small radius $v_{\text{circ}}^{\text{(max)}}(\text{JAM})$ derived by C13 using dynamical models (see Section 2 and Table 1). Those authors find a tight correlation between $v_{\text{circ}}^{\text{(max)}}(\text{JAM})$ and $\sigma_e$. Therefore, in light of our Fig. 1, we expect a correlation between $v_{\text{circ}}(H\text{i})$ and $v_{\text{circ}}^{\text{(max)}}(\text{JAM})$. This is shown in Fig. 3. As in Section 3.1, we fit a power law to the data points and find the best fit to be relatively close to a linear relation given the error bars (the exponent is 0.79 $\pm$ 0.15). Indeed, the 17 per cent (0.068 dex) observed scatter around the best-fitting power law is only slightly lower than the 18 per cent scatter around the linear relation:

$$v_{\text{circ}}(H\text{i}) = 0.73 v_{\text{circ}}^{\text{(max)}}(\text{JAM}).$$

The scatter of the $v_{\text{circ}}(H\text{i})$–$v_{\text{circ}}^{\text{(max)}}(\text{JAM})$ relation is considerably larger than that of the $v_{\text{circ}}(H\text{i})$–$\sigma_e$ relation. In particular, based on the 7 per cent observed scatter of the $v_{\text{circ}}^{\text{(max)}}(\text{JAM})$–$\sigma_e$ relation (C13), a conservative estimate of the uncertainty on $v_{\text{circ}}^{\text{(max)}}(\text{JAM})$ is $\sim 5$ per cent (as for $\sigma_e$). The resulting intrinsic scatter of the $v_{\text{circ}}(H\text{i})$–$v_{\text{circ}}^{\text{(max)}}(\text{JAM})$ relation is $\pm 5$ per cent (it was $\pm 4$ per cent for the $v_{\text{circ}}(H\text{i})$–$\sigma_e$ relation). This could indicate that, in the present sample, the distribution of mass is relatively homogeneous between $R_e$ and $R_{\text{HI}}$, but less so between $R_{\text{max}}$ and $R_e$. A visual inspection of the rotation curves in the Noordermeer et al. (2007) sample indicates that this is the case in early-type spirals.

Our measurements show that $v_{\text{circ}}$ drops on average $\sim 25$ per cent from $R_{\text{max}}$ to $R_{\text{HI}}$ (the actual drop varying between 0 and 50 per cent depending on the galaxy). Obvious questions are where this drop occurs within galaxies and how gradual it is with radius. Some qualitative indications come from molecular gas $v_{\text{circ}}$ estimates obtained by Davis et al. (2011) at a radius intermediate between $R_{\text{max}}$ and $R_{\text{HI}}$ (for CO-detected galaxies in the ATLAS$^{3D}$ sample the molecular gas reaches a typical radius between 0.5 and $1 R_e$; see Davis et al. 2013). First, Davis et al. (2011) show that $v_{\text{circ}}(\text{CO})$ is on average $\sim 10$ per cent lower than $v_{\text{circ}}^{\text{(max)}}(\text{JAM})$ (with considerable scatter; see their fig. 4). Second, $dH_{15}$ report an offset between the CO and H$\text{i}$ K-band Tully–Fisher relations of ETGs corresponding to a $v_{\text{circ}}$ decrease by another $\sim 10$ per cent. Combining these two results we conclude that the average $\sim 25$ per cent $v_{\text{circ}}$ drop between $R_{\text{max}}$ and $R_{\text{HI}}$ is about equally distributed inside and outside $R_e$.

A more quantitative result would require a detailed study of the resolved rotation curve out to $R_{\text{HI}}$ for galaxies in this sample. However, at the typical resolution of our H$\text{i}$ data ($\sim 40$ arcsec) this is possible for just a few objects. Two such galaxies are NGC 2685 (Józsa et al. 2009) and NGC 2974 (Weijsmans et al. 2008). Their rotation curves show indeed a clear decline out to $\sim 10$ and $\sim 2 R_e$, respectively, and appear to flatten further out. This would be consistent with the situation in early-type spirals, where $v_{\text{circ}}$ peaks at small radius and then drops by 10–20 per cent to a flat level (Noordermeer et al. 2007). A similar study of the resolved H$\text{i}$ rotation curve can be performed for a few more objects in our sample and will be the subject of future work. For the time being, it remains unclear whether and at what characteristic radius the H$\text{i}$ rotation curves of ETGs become flat.

Whatever results will be obtained from studying the resolved H$\text{i}$ kinematics of more ETGs, we do know from C15 that the stellar rotation curves of most such systems decline steadily out to at
least \( \sim 4 R_e \). These authors find that the observed decline of \( v_{\text{circ}} \) is well described by power-law density profiles \( \rho \propto r^{-\gamma} \), and that the profile slopes \( \gamma \) cover a surprisingly narrow range centred around a mean value \( \langle \gamma \rangle = 2.19 \pm 0.03 \) and with an observed r.m.s. scatter \( \sigma_r \) of just 0.11. Here we can test this result using a different sample (only two galaxies are in common between our sample and that of C15) and completely different observations that reach further out into the dark-matter halo.

### 3.4 Average slope of the total density profiles

The analysis of C15 shows that the mass distribution of ETGs is well represented by power-law density profiles \( \rho \propto r^{-\gamma} \) out to large radius. We therefore assume power-law profiles for our galaxies. It follows that \( v_{\text{circ}} \propto r^{1-\gamma/2} \) (Binney & Tremaine 2008, Eq. 2.61). We can then use our measurements of \( v_{\text{circ}}\text{max} \text{(JAM)} \) and \( v_{\text{circ}}(\text{HI}) \) at \( R_{\text{max}} \) and \( R_{\text{HI}} \), respectively, to measure the average logarithmic slope of the density profile for each galaxy:

\[
\gamma = 2 - 2 \frac{\log v_{\text{circ}}(\text{HI}) - \log v_{\text{circ}}\text{max} \text{(JAM)}}{\log R_{\text{HI}} - \log R_{\text{max}}},
\]

and study the distribution of \( \gamma \) values across the sample.

Fig. 4 shows our measurements as well as model rotation curves for a range of \( \gamma \) values. We find a narrow range for \( \gamma \), with all galaxies confined in a region of the plot corresponding to \( 2 < \gamma < 2.4 \). On average, galaxies in this sample appear to have profiles somewhat steeper than isothermal. This is an important confirmation of the result presented by C15, in particular considering the different sample and type of data used here.

More quantitatively, the weighted mean and the r.m.s. scatter of the 16 \( \gamma \) values listed in Table 1 are:

\[
\langle \gamma \rangle = 2.18 \pm 0.03 \quad \text{and} \quad \sigma_\gamma = 0.11.
\]

Although here we cannot check whether the assumption of power-law profiles is correct and can only measure the average logarithmic slope, our result is in remarkable quantitative agreement with the one of C15, where the adequacy of power-law profiles is verified. Our mean slope is very close to their \( \langle \gamma \rangle = 2.19 \pm 0.03 \), and the observed scatter is identical. Our result is also in relatively good agreement with that obtained at small radius from gravitational lensing, which suggests profile shapes only marginally closer to isothermal (Auger et al. 2010; Barnabe et al. 2011).

As discussed in Section 3.3, our data do not rule out that at some radius beyond \( R_e \) the rotation curves of ETGs become flat. If that is the case, we would expect our measurements of \( \gamma \) to approach the isothermal value \( \gamma = 2 \) as \( R_{\text{HI}} \) increases. Fig. 4 does not show any clear indications that this is the case. Galaxies with a \( v_{\text{circ}}(\text{HI}) \) measurement at \( \sim 10 R_e \) or above can have a value of \( \gamma \) significantly above 2, while galaxies with a \( v_{\text{circ}}(\text{HI}) \) measurement obtained below \( 5 R_e \) can have \( \gamma \) close to the isothermal value. As pointed out in the case of the \( v_{\text{circ}}(\text{HI})-\sigma_e \) relation (Section 3.1 and Fig. 2), the scatter in the shape of the ETG rotation curves might be more important than the radius at which we measure \( v_{\text{circ}}(\text{HI}) \). We stress again that only the resolved study of more \( \text{HI} \) rotation curves can clarify whether and at what radius \( v_{\text{circ}} \) becomes flat in ETGs.

The above discussion indicates that, whether or not the density profiles of all ETGs are well approximated by single power laws out to the radius probed by our \( v_{\text{circ}}(\text{HI}) \) measurements, (i) their average slopes cluster around a value of 2.2 and (ii) the small scatter of 0.11 is indicative of relatively small differences between galaxies, as also suggested by the scatter of the \( v_{\text{circ}}(\text{HI})-\sigma_e \) relation. The origin of these differences is, however, unclear. Since \( \gamma \) measures an average property of the distribution of mass one may think that its value depends on the presence of a massive bulge and, therefore, on the value of \( \sigma_e \). However, Fig. 5 shows that \( \gamma \) does not vary systematically with \( \sigma_e \), for our sample combined with the one of C15 (the correlation coefficient is below 0.4). An identical conclusion is reached from dynamical modelling of ETGs within \( 1 R_e \), considering only galaxies within the \( \sigma_e \) and stellar mass range covered by our sample (fig. 22 of Cappellari 2016). The same modelling shows that \( \gamma \) does decrease at lower \( \sigma_e \) and larger stellar masses than covered by our sample, but it is unknown whether a similar trend persists at the large, dark-matter dominated radii reached by our \( \text{HI} \) data.

We have investigated possible correlations between \( \gamma \) and additional parameters that trace the relative importance of the bulge: the bulge-to-total ratio, the effective surface brightness (both total and...
Figure 5. Average logarithmic profile slope $\gamma$ versus stellar velocity dispersion $\sigma_v$ for our sample and the sample of C15. No correlation is observed.

of the bulge) and the Sérsic index from Krajnović et al. (2013); the light concentration from C13; and the ratio $\sigma_R/\sigma_e$ from Cappellari et al. (2013b). In all cases we find correlation coefficients below 0.4 (in absolute value). Therefore, we conclude that the current sample shows no indication of a systematic variation of $\gamma$ with the optical structure of ETGs. Larger samples will be needed to establish the nature of the small scatter of the density profile shapes.

4 CONCLUSIONS

We establish a tight linear relation between the circular velocity measured in the dark-matter dominated regions ($\sim 6 R_e$) and the velocity dispersion measured inside 1 $R_e$ for a sizeable sample of 16 ETGs. The $v_{\text{circ}}$ values are obtained from resolved H$\alpha$ observations and, therefore, do not suffer from the limitations of single-dish data previously used in the literature. We find that $v_{\text{circ}}(H\alpha) = 1.33 \sigma_e$ with an observed scatter of 12 per cent. The tightness of the correlation suggests a strong coupling between luminous and dark matter from the inner regions where we measure $\sigma_e$ to the outer regions where we measure $v_{\text{circ}}(H\alpha)$. This coupling has been long known for spirals and dwarf irregulars (van Albada & Sancisi 1986; Sancisi 2004; Swaters et al. 2012; Lelli et al. 2013) but had never been established for ETGs.

Previous samples of ETGs with resolved $v_{\text{circ}}(H\alpha)$ measurements were too small to establish the tightness, linearity and actual slope of the $v_{\text{circ}}(H\alpha) - \sigma_e$ relation, and to compare it with relations obtained at smaller radius. Overall, we find that our relation is shallower than those based on $v_{\text{circ}}$ measurements obtained from stellar kinematics and dynamical modelling at a radius comparable with $R_e$. This indicates a decline in $v_{\text{circ}}$ from $R_e$ to the outer regions where we measure $v_{\text{circ}}(H\alpha)$.

Comparing our H$\alpha$ measurements of $v_{\text{circ}}$ at $\sim 6 R_e$ with those derived from dynamical modelling of the stellar kinematics at much smaller radius ($\sim 0.2 R_e$) we find that the rotation curves of ETGs drop by 0–50 per cent towards large radius for galaxies in the sample (25 per cent on average). This drop is similar to that observed in early-type spirals (Noordermeer et al. 2007). It is in excellent agreement with a recent, independent determination of the slope of the density profile of ETGs based on stellar kinematics and dynamical modelling of a different sample (C15). It appears that the average density profile of ETGs in the stellar mass and $\sigma_e$ ranges probed by our combined samples is slightly steeper than isothermal, with a logarithmic slope of 2.19 ± 0.02 and a scatter of just 0.11.

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$v_{\text{circ}}(H\alpha) - \sigma_e$ relation and density profiles in ETGs

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