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Measurement of $D^+$ and $\Lambda_c^+$ production in deep inelastic scattering at HERA

ZEUS collaboration

Abstract: Charm production in deep inelastic scattering has been measured with the ZEUS detector at HERA using an integrated luminosity of 120 pb$^{-1}$. The hadronic decay channels $D^+ \rightarrow K_S^0 \pi^+$, $\Lambda_c^+ \rightarrow pK_S^0$ and $\Lambda_c^+ \rightarrow \Lambda \pi^+$, and their charge conjugates, were reconstructed. The presence of a neutral strange hadron in the final state reduces the combinatorial background and extends the measured sensitivity into the low transverse momentum region. The kinematic range is $0 < p_T(D^+, \Lambda_c^+) < 10$ GeV, $|\eta(D^+, \Lambda_c^+)| < 1.6$, $1.5 < Q^2 < 1000$ GeV$^2$ and $0.02 < y < 0.7$. Inclusive and differential cross sections for the production of $D^+$ mesons are compared to next-to-leading-order QCD predictions. The fraction of $c$ quarks hadronising into $\Lambda_c^+$ baryons is extracted.

Keywords: Lepton-Nucleon Scattering

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1 Introduction

Heavy-quark production in ep interactions in deep inelastic scattering (DIS) is dominated by the Boson Gluon Fusion (BGF) process. Heavy-quark production provides a two-fold test of perturbative quantum chromodynamics (pQCD); a study of the BGF process and the higher-order corrections to it, and an independent check of the validity of the gluon density in the proton extracted from the inclusive DIS data. Of the two heavy quarks whose production is accessible at HERA, c and b, the latter is strongly suppressed due to its smaller electric charge and larger mass.

The production of charm via the identification of D and D* mesons in DIS has been extensively studied at HERA in the kinematic range $1 < Q^2 < 1000 \text{GeV}^2$, $p_T(D, D^*) >$
1.5 GeV [1–8], where $Q^2$ is the negative squared four-momentum exchange at the electron vertex and $p_T$ is the transverse momentum. The results are consistent with the calculations of pQCD. The fragmentation fraction $f(c \rightarrow \Lambda^+_c)$ has been measured by the ZEUS collaboration in the photoproduction regime [9]. The obtained fragmentation fraction is larger than but consistent within uncertainties with the average from $e^+e^-$ collisions [10].

In this paper, a charm quark in the final state was identified by the presence of a charmed hadron. The production of $D^+$ mesons and $\Lambda_c^+$ baryons was studied using the decays\(^1\) $D^+ \rightarrow K_S^0 \pi^+$, $\Lambda_c^+ \rightarrow pK_S^0$ and $\Lambda_c^+ \rightarrow \Lambda \pi^+$. These decay channels were chosen since the presence of a neutral strange hadron in the final state significantly reduces the combinatorial background. Measurements of $D^+$ and $\Lambda_c^+$ cross sections provide information about both $c$-quark production and its fragmentation.

With respect to previous studies, in this analysis the kinematic region of the measurement is extended to very low transverse momenta of the produced charmed hadrons. No explicit cut on the transverse momenta of the reconstructed charmed hadrons was applied. This is particularly relevant at low $Q^2$, where charm quarks are predominantly produced with low transverse momentum. In addition, $\Lambda_c^+$ production was studied for the first time at HERA in DIS. From a comparison of the $D^+$ and $\Lambda_c^+$ cross sections, the fragmentation fraction $f(c \rightarrow \Lambda_c^+)$ is extracted.

2 Experimental set-up

The analysis was performed with data taken from 1996 to 2000 corresponding to a luminosity of 120.4 ± 2.4 pb\(^{-1}\). The sample consists of 38.6 pb\(^{-1}\) of $e^+p$ data collected at a centre-of-mass energy of 300 GeV and of 65.1 pb\(^{-1}\) collected at 318 GeV, plus 16.7 pb\(^{-1}\) of $e^-p$ data collected at 318 GeV.\(^2\)

A detailed description of the ZEUS detector can be found elsewhere [11]. A brief outline of the components most relevant for this analysis is given below.

Charged particles were tracked in the central tracking detector (CTD) [12–14], which operated in a magnetic field of 1.43 T provided by a thin superconducting coil. The CTD consisted of 72 cylindrical drift chamber layers, organised in 9 superlayers covering the polar-angle\(^3\) region $15^\circ < \theta < 164^\circ$. The transverse-momentum resolution for full-length tracks was $\sigma(p_T)/p_T = 0.0058p_T + 0.0065 + 0.0014/p_T$, with $p_T$ in GeV.

To estimate the ionisation energy loss per unit length, $dE/dx$, of particles in the CTD [15–18], the truncated mean of the anode-wire pulse heights was calculated, which removes the 10% lowest and at least the 30% highest pulses depending on the number of saturated hits. The measured $dE/dx$ values were corrected by normalising to the measured

\(^1\)The charge conjugated modes are implied throughout this paper.

\(^2\)Hereafter, both electrons and positrons are referred to as electrons, unless explicitly stated otherwise.

\(^3\)The ZEUS coordinate system is a right-handed Cartesian system, with the $Z$ axis pointing in the proton beam direction, referred to as the “forward direction”, and the $X$ axis pointing towards the centre of HERA. The coordinate origin is at the nominal interaction point. The pseudorapidity is defined as $\eta = -\ln(\tan(\theta/2))$, where the polar angle, $\theta$, is measured with respect to the proton beam direction. The azimuthal angle in the $X$-$Y$ plane is called $\phi$. 
average $dE/dx$ for tracks around the region of minimum ionisation for pions with momentum $p$ satisfying $0.3 < p < 0.4$ GeV. Henceforth, $dE/dx$ is quoted in units of minimum ionising particles (mips).

The high-resolution uranium-scintillator calorimeter (CAL) [19–22] consisted of three parts: the forward (FCAL), the barrel (BCAL) and the rear (RCAL) calorimeters. Each part was sub-divided transversely into towers and longitudinally into one electromagnetic section (EMC) and either one (in RCAL) or two (in BCAL and FCAL) hadronic sections (HAC). The smallest subdivision of the calorimeter is called a cell. The CAL energy resolutions, as measured under test-beam conditions, are $\sigma(E)/E = 0.18/\sqrt{E}$ for electrons and $\sigma(E)/E = 0.35/\sqrt{E}$ for hadrons, with $E$ in GeV.

The position of the scattered electron at the CAL was determined by combining information from the CAL and, where available, the small-angle rear tracking detector (SRTD) [23] and the hadron-electron separator (HES) [24].

The luminosity was measured from the rate of the bremsstrahlung process $ep \rightarrow e\gamma p$, where the photon was measured in a lead-scintillator calorimeter [25–27] placed in the HERA tunnel at $Z = -107$ m.

3 Theoretical predictions

The next-to-leading-order (NLO) QCD predictions for the $c\bar{c}$ production cross sections were obtained using the HVQDIS program [28] based on the fixed-flavour-number scheme (FFNS). In this scheme, only light quarks ($u$, $d$ and $s$) and gluons are included in the proton parton density functions (PDFs) which obey the DGLAP equations [29–32], and the $c\bar{c}$ pair is produced via the BGF mechanism [33, 34] with NLO corrections [35, 36]. The presence of different large scales, $Q$, $p_T$ and the mass of the $c$ quark, $m_c$, can spoil the convergence of the perturbative series because the neglected terms of orders higher than $\alpha_s^2$ (where $\alpha_s$ is the strong coupling constant) contain $\log(Q^2/m_c^2)$ factors which can become large. The FFNS variant of the ZEUS-S NLO QCD fit [37] to structure function data was used as the parametrisation of the proton PDFs. In this fit, $\alpha_s(M_Z)$ was set to 0.118 and the mass of the charm quark was set to 1.5 GeV; the same mass was used in the HVQDIS calculation.

The renormalisation and factorisation scales were set to $\mu_R = \mu_F = \sqrt{Q^2 + 4m_c^2}$. The charm fragmentation to the $D^+$ meson was modelled using the Peterson function [38] with the Peterson parameter, $\epsilon$, set to 0.079 [39]. For the hadronisation fraction, $f(c \rightarrow D^+)$, the value $0.216^{+0.021}_{-0.029}$ was used [7].

The HVQDIS predictions for the production of $D^+$ mesons are affected by the theoretical uncertainties listed below. The uncertainty on the total cross section is given in parentheses:

- the ZEUS PDF uncertainties were propagated from the experimental uncertainties of the fitted data ($^{+5.3\%}_{-5.2\%}$);

- the charm quark mass was changed consistently in the PDF fit and in HVQDIS by $\pm 0.15$ GeV ($^{+15.2\%}_{-13.5\%}$).
• the renormalisation scale was varied by a factor 2 \((+19.7\%,-12.6\%)\);

• the factorisation scale was changed by a factor 2 independently of the renormalisation scale \((+13.1\%,-21.7\%)\);

• the \(\epsilon\) parameter of the Peterson fragmentation function was changed to 0.01 and 0.1 \([39, 40]\). This modification affects the shapes of the \(p_T\), \(Q^2\) and \(x\) distributions \((+0.1\%,-0.4\%)\).

4 Monte Carlo models

The detector acceptance was modelled using the RAPGAP 3.00 [41] Monte Carlo (MC) program, interfaced with HERACLES 4.6.1 [42] in order to incorporate first-order electroweak corrections. The generated events were passed through a full simulation of the detector, using GEANT 3.13 [43], and finally processed and selected in the same way as the data.

The MC was used to simulate events containing charm quarks produced in the BGF process. The RAPGAP generator used leading-order matrix elements with leading-logarithmic parton showers. The CTEQ5L [44] PDFs were used for the proton. The charm-quark mass was set to 1.5 GeV. Charm fragmentation was simulated using the Lund string model [45]. The \(D^+\) and \(\Lambda_c^+\) hadrons originating from beauty decays were accounted for by including a RAPGAP \(b\)-quark sample where the \(b\)-quark mass was set to 4.75 GeV. An additional sample where charm was produced by the process \(cg \to cg\) was generated and was used to study the model dependence of the simulation. For this process, the charm quark was treated as a part of the structure of the photon. The processes \(gg \to c\bar{c}\) and \(q\bar{q} \to c\bar{c}\) were not included because their contribution estimated using the RAPGAP MC was found to be less than 1% in the studied kinematic range.

In general, the MC gives a reasonable description of the data for DIS and \(D^+\)-meson variables when compared at detector level. To improve the description further, RAPGAP was reweighted to reproduce the \(p_T(D^+)\) distribution observed in the data. The same weights used for \(D^+\) mesons were also applied to \(D_s^+\) and \(\Lambda_c^+\) hadrons.

5 Kinematic reconstruction and event selection

A three-level trigger system was used to select events online [11, 46]. At the third level, an electron with an energy greater than 4 GeV and a position outside a box of 24 \(\times\) 12 cm\(^2\) centred around the beampipe on the face of the rear calorimeter was required by a fully inclusive DIS trigger which had a high acceptance for \(Q^2 \gtrsim 1\) GeV\(^2\). However, this trigger was heavily prescaled and the equivalent luminosity is 17 pb\(^{-1}\).

Additionally, events above \(Q^2 \approx 20\) GeV\(^2\) were selected by a medium-\(Q^2\) trigger. The only difference to the inclusive DIS trigger is that the position of the scattered electron on the RCAL face had to lie outside a circle centred around the beampipe of radius between 25 and 35 cm, depending on the running period.

The fraction of the electron energy transferred to the proton in its rest frame, \(y\), as well as the kinematic variables \(Q^2\) and Bjorken \(x\), were reconstructed offline using the electron
method [47] (denoted by the subscript e), which uses the energy and angle of the scattered electron. The inelasticity $y$ was also obtained using the Jacquet-Blondel (JB) method [48]. The double angle (DA) method [47], which relies on the angles of the scattered electron and the hadronic-energy flow, was used as a systematic check.

The following requirements were imposed offline:

- $38 < \delta < 65$ GeV, where $\delta = \sum E_i(1 - \cos \theta_i)$ and $E_i$ and $\theta_i$ are the energy and the polar angle of the $i^{th}$ energy-flow object (EFO) [49] reconstructed from charged tracks, as measured in the CTD, and energy clusters measured in the CAL. The sum $i$ runs over all EFOs [50];
- $E'_e > 10$ GeV, where $E'_e$ is the energy of the scattered electron identified using a neural-network algorithm [51, 52];
- $E_{\text{cone}} < 5$ GeV, where $E_{\text{cone}}$ is the calorimeter energy measured in a cone around the electron position that was not assigned to the electron cluster. The cone was defined by $R_{\text{cone}} < 0.8$ with $R_{\text{cone}} = \sqrt{(\Delta \phi)^2 + (\Delta \eta)^2}$;
- a match between the tracking and the calorimeter information for electrons well within the CTD acceptance, $17^\circ < \theta_e < 149^\circ$. For $\theta_e$ outside this region, the cut $\delta > 44$ GeV was imposed;
- for events with the scattered electron reconstructed within the SRTD acceptance, the impact position of the electron on the face of the RCAL had to be outside the region $26 \times 14 \text{ cm}^2$ centred on $X = Y = 0$. If the electron position was reconstructed without using SRTD information, a box cut of $26 \times 20 \text{ cm}^2$ was imposed;
- $1.5 < Q_e^2 < 1000$ GeV$^2$;
- $y_{\text{JB}} > 0.02$ and $y_e < 0.7$;
- a primary vertex position in the range $|Z_{\text{vertex}}| < 50$ cm.

This analysis used charged tracks measured in the CTD that were assigned either to the primary or to a secondary vertex. The tracks were required to have transverse momenta $p_T > 0.15$ GeV and pseudorapidity in the laboratory frame $|\eta| < 1.75$, restricting the study to a region where the CTD track acceptance and resolution were high. Candidates for long-lived neutral strange hadrons decaying to two charged particles were identified by selecting pairs of oppositely charged tracks, fitted to a displaced secondary vertex. The events were required to have at least one such candidate.

6 Strange-particle reconstruction

The $K^0_S$ mesons were identified by their charged decay mode, $K^0_S \rightarrow \pi^+\pi^-$. Both tracks were assigned the mass of the charged pion and the invariant mass, $M(\pi^+\pi^-)$, of each track pair was calculated. Additional requirements to select $K^0_S$ were imposed:
• $M(e^+e^-) > 50\,\text{MeV}$, where the electron mass was assigned to each track, to eliminate tracks from photon conversions;

• $M(p\pi) > 1121\,\text{MeV}$, where the proton mass was assigned to the track with higher momentum, to eliminate $\Lambda$ contamination in the $K_S^0$ signal;

• $\cos \theta_{XY} > 0.98$, where $\theta_{XY}$ is defined as the angle between the momentum vector of the $K_S^0$ candidate and the vector defined by the primary interaction vertex and the $K_S^0$ decay vertex in the $X-Y$ plane;

• $483 < M(\pi^+\pi^-) < 513\,\text{MeV}$;

• $|\eta(K_S^0)| < 1.6$.

The $\Lambda$ candidates were reconstructed by their charged decay mode to $p\pi^-$. The track with the larger momentum was assigned the mass of the proton, while the other was assigned the mass of the charged pion, as the decay proton always has a larger momentum than the pion, provided the $\Lambda$ momentum is greater than $0.3\,\text{GeV}$. Additional requirements to select $\Lambda$ were imposed:

• $M(e^+e^-) > 50\,\text{MeV}$;

• $M(\pi^+\pi^-) < 483\,\text{MeV}$, where the charged pion mass was assigned to both tracks, to remove $K_S^0$ contamination in the $\Lambda$ signal;

• $\cos \theta_{XY} > 0.98$;

• $1112 < M(p\pi) < 1121\,\text{MeV}$;

• $|\eta(\Lambda)| < 1.6$.

Figure 1 shows the invariant-mass spectra of $K_S^0$, $\Lambda$ and $\bar{\Lambda}$ candidates. Distributions of the reconstructed proper lifetime for these particles based on the same data sample as analysed in this paper were found to be satisfactory [53].

7 Reconstruction of charmed hadrons

The production of $D^+$ and $\Lambda_c^+$ hadrons was measured in the range of transverse momentum $0 < p_T(D^+, \Lambda_c^+) < 10\,\text{GeV}$ and pseudorapidity $|\eta(D^+, \Lambda_c^+)| < 1.6$. Strange-hadron candidates were combined with a further track measured in the CTD which was assigned to the primary interaction vertex. The combinatorial background was significantly reduced by requiring $p_T(D^+)/E_T^{\theta > 10^\circ} > 0.1$ and $p_T(\Lambda_c^+)/E_T^{\theta > 10^\circ} > 0.12$, where the transverse energy $E_T^{\theta > 10^\circ}$ was evaluated as $E_T^{\theta > 10^\circ} = \sum_{i, \theta_i > 10^\circ}(E_i \sin \theta_i)$. The sum runs over all energy deposits in the CAL with a polar angle $\theta$ above $10^\circ$. The details of the reconstruction of the three different decay channels are given in the next subsections.
Figure 1. Mass distributions of the secondary vertex candidates in the (a) $K_S^0$, (b) $\Lambda$ and (c) $\bar{\Lambda}$ samples. The statistical uncertainties are in general smaller than the point size. For illustration the data have been fitted using the sum of a “modified” Gaussian function [9] and a linear background.

7.1 Reconstruction of the decay $D^+ \rightarrow K_S^0 \pi^+$

The $D^+$ mesons were reconstructed from the decay channel $D^+ \rightarrow K_S^0 \pi^+$. In each event, $D^+$ candidates were formed from combinations of $K_S^0$ candidates reconstructed as described
in section 6 with further tracks assumed to be pions. The pion candidates were required to have $p_T(\pi^+)/E_T^{\text{jet}} > 0.04$. Only pion candidates with $dE/dx < 1.5$ mips were considered. Further reduction of the combinatorial background was achieved by cutting on the angle between the pion in the $D^+$ rest frame and the $D^+$ flight direction, $\theta^*(\pi^+)$. Different cuts depending on $p_T(D^+)$ were used to ensure optimal background suppression:

- $\cos \theta^*(\pi^+) < 0.9$ for $0 < p_T(D^+) < 1.5$ GeV;
- $\cos \theta^*(\pi^+) < 0.8$ for $1.5 < p_T(D^+) < 3.0$ GeV;
- $\cos \theta^*(\pi^+) < 0.6$ for $3.0 < p_T(D^+) < 10.0$ GeV.

The $K_S^0\pi^+$ invariant-mass distribution was fitted with the sum of contributions from the signal, the non-resonant background and a reflection caused by $D_s^+ \rightarrow K_S^0 K^+$ decays. The signal was described by a Gaussian function defined as:

$$g(\sigma, M_0; m) = \frac{1}{\sqrt{2\pi}\sigma} \exp\left(-\frac{(m - M_0)^2}{2\sigma^2}\right),$$

where $M_0$ and $\sigma$ are the resonance mass and width, respectively. For the background a sum of Chebyshev polynomials up to the second order was used:

$$b(A, B, C; y(m)) = A \cdot (1 + B \cdot y + C \cdot (2y^2 - 1)),\quad (7.2)$$

where $y(m) = (2m - m_{\text{max}} - m_{\text{min}}) / (m_{\text{max}} - m_{\text{min}})$ and $m_{\text{max}}(m_{\text{min}}) = 2.1(1.6)$ GeV is the upper (lower) limit of the fitted range.

The mass distribution of the reflection $r(m)$ caused by the decay $D_s^+ \rightarrow K_S^0 K^+ \rightarrow \pi^+\pi^- K^+$ was obtained from $D_s^+$ combinations in the Monte Carlo at detector level matched to the same decay at generator level. The normalisation of the reflection with respect to the Gaussian signal assumed for $D^+ \rightarrow K_S^0 \pi^+$ decays is based on previously measured fragmentation fractions $f$ [7] and branching ratios $B$ [54] (see also table 1) and the detector acceptances for both decay channels. For this purpose, the invariant mass distribution of the reflection was normalised to unity and then multiplied by the expected ratio of $D_s^+$ to $D^+$ mesons:

$$R = \frac{f(c \rightarrow D_s^+) \cdot B(D_s^+ \rightarrow K_S^0 K^+ \rightarrow \pi^+\pi^- K^+) \cdot A(D_s^+)}{f(c \rightarrow D^+) \cdot B(D^+ \rightarrow K_S^0 \pi^+ \rightarrow \pi^+\pi^- \pi^+) \cdot A(D^+)} = 0.44 \pm 0.10,$\quad (7.3)$$

where $A(D_s^+)$ and $A(D^+)$ are the reconstruction acceptances for $D_s^+$ and $D^+$ mesons, respectively, as obtained from the Monte Carlo. The resulting fitting function is given by:

$$F(A, B, C, D, \sigma, M_0; m) = b(A, B, C; y(m)) + D \cdot [r(m) + g(\sigma, M_0; m)],\quad (7.4)$$

<table>
<thead>
<tr>
<th>Decay mode</th>
<th>Branching ratio [%]</th>
</tr>
</thead>
<tbody>
<tr>
<td>$D^+ \rightarrow K_S^0\pi^+ \rightarrow \pi^+\pi^-\pi^+$</td>
<td>1.00 ± 0.03</td>
</tr>
<tr>
<td>$D_s^+ \rightarrow K^+ K_S^0 \rightarrow K^+\pi^+\pi^-$</td>
<td>1.03 ± 0.06</td>
</tr>
<tr>
<td>$\Lambda_c^+ \rightarrow pK_S^0 \rightarrow p\pi^+\pi^-$</td>
<td>0.80 ± 0.21</td>
</tr>
<tr>
<td>$\Lambda_c^+ \rightarrow \Lambda\pi^+ \rightarrow p\pi^-\pi^+$</td>
<td>0.68 ± 0.18</td>
</tr>
</tbody>
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Table 1. Branching ratios of the charmed hadron decays [54].
where the parameters $A$, $B$, $C$, $D$, $\sigma$ and $M_0$ were determined by the fit.

Figure 2 shows the invariant mass spectrum for the $D^+$ candidates after the reflection was subtracted using the fit, resulting in a 20% reduction in the number of $D^+$ mesons. A clear signal is visible. The fit yielded a $D^+$ mass of $1872 \pm 4$ MeV, in agreement with the PDG value \[54\]. The width of the signal was $19.0 \pm 3.1$ MeV, reflecting the detector resolution. The number of $D^+$ mesons yielded by the fit was $N(D^+) = 691 \pm 107$.

In order to extract the $D^+$-meson yields in bins of $p_T(D^+)$, $\eta(D^+)$, $Q^2$ and $x$, the signals in all analysis bins of a given quantity were fitted simultaneously, fixing the ratios of the widths in the bins to the Monte Carlo prediction. All other parameters including the masses were left free for all bins in the simultaneous fit.

The signal in the region $0 < p_T(D^+) < 1.5$ GeV that was not accessible in previous measurements is shown in figure 3.

7.2 Reconstruction of the decay $\Lambda_c^+ \rightarrow pK_S^0$

The $\Lambda_c^+$ baryons were reconstructed from the decay channel $\Lambda_c^+ \rightarrow pK_S^0$. In each event, $\Lambda_c^+$ candidates were formed from combinations of $K_S^0$ candidates reconstructed as described in section 6 with proton candidates. The proton-candidate selection used the energy-loss measurement in the CTD. Tracks fitted to the primary vertex with more than 40 hits were considered. The proton band was parametrised separately for positive and negative tracks from an examination of $dE/dx$ as a function of the momentum \[55\]. The proton selection was checked by studying proton-candidate tracks from $\Lambda$ decays. To remove the
Figure 3. The $M(K_{S}^{0}\pi^{+})$ distribution (dots) for $D^{+}$ candidates in the region $0 < p_{T}(D^{+}) < 1.5$ GeV. The reflection caused by the decay $D_{s}^{+} \rightarrow K_{S}^{0}\pi^{+}$ has been subtracted as described in the text. The solid curve represents a fit to the sum of a Gaussian signal and a background function, while the background contribution alone is given by the dashed curve.

region where the proton band completely overlaps the pion band, the proton momentum was required to be less than 1.5 GeV and a cut on $dE/dx > 1.2$ mips was applied. Due to the proton selection described above, reflections from $D^{+} \rightarrow K_{S}^{0}\pi^{+}$ and $D_{s}^{+} \rightarrow K_{S}^{0}K^{+}$ decays are suppressed.

As a result of the cut on the proton momentum, there is no acceptance for $\Lambda_{c}^{+}$ baryons at very high $p_{T}(\Lambda_{c}^{+})$. Hence the measurement of the cross section for this decay channel was restricted to the region $0 < p_{T}(\Lambda_{c}^{+}) < 6$ GeV.

Figure 4 shows the $M(pK_{S}^{0})$ distribution for the $\Lambda_{c}^{+}$ candidates. A clear signal is seen at the nominal value of the $\Lambda_{c}^{+}$ mass [54]. The mass distribution was fitted to the sum of a Gaussian function describing the signal and the function defined in eq. (7.2) to describe the non-resonant background. The number of reconstructed $\Lambda_{c}^{+}$ baryons yielded by the fit was $N(\Lambda_{c}^{+}) = 79 \pm 25$.

7.3 Reconstruction of the decay $\Lambda_{c}^{+} \rightarrow \Lambda\pi^{+}$

The $\Lambda_{c}^{+}$ baryons were also reconstructed from the decay channel $\Lambda_{c}^{+} \rightarrow \Lambda\pi^{+}$. In each event, $\Lambda_{c}^{+}$ candidates were formed from combinations of $\Lambda$ candidates as described in section 6, with further tracks assumed to be pions. The pion candidates were required to have $p_{T}(\pi^{+})/E_{T}^{\pi^{+}} > 0.05$. Only pion candidates with $dE/dx < 1.5$ mips were considered. To suppress combinatorial background further, the cut $\cos\theta^{*}(\pi^{+}) < 0.8$ was imposed, where $\theta^{*}(\pi^{+})$ is the angle between the pion in the $\Lambda_{c}^{+}$ rest frame and the $\Lambda_{c}^{+}$ flight direction.

Figure 5 shows the $M(\Lambda\pi)$ distribution for the $\Lambda_{c}^{+}$ candidates. Wrong-charge combinations in the data sample, normalised to the right-charge combinations in the region
**Figure 4.** The $M(pK_S^0)$ distribution (dots) for $\Lambda^+_c$ candidates in the region $0 < p_T(\Lambda^+_c) < 6$ GeV. The solid curve represents a fit to the sum of a Gaussian signal and a background function, while the background contribution alone is given by the dashed curve.

**Figure 5.** The $M(\Lambda\pi^+)$ distribution (dots) for $\Lambda^+_c$ candidates. The solid curve represents a fit to the sum of a Gaussian signal and a background function, while the background contribution alone is given by the dashed curve. The dotted histogram shows the distribution of wrong-charge combinations (see text).

outside the peak, are also shown. For wrong-charge combinations, the sum of the charges of the proton from the $\Lambda$ candidate and the further track is equal to zero. The data were fitted to the sum of a Gaussian function describing the signal and the background function
Figure 6. The invariant mass distribution (dots) for $\Lambda^+_c \rightarrow pK^0_S$ and $\Lambda^+_c \rightarrow \Lambda\pi^+$ candidates. The solid curve represents a fit to the sum of a Gaussian signal and a background function, while the background contribution alone is given by the dashed curve.

defined in eq. (7.2). The number of reconstructed $\Lambda^+_c$ baryons obtained from the fit was $N(\Lambda^+_c) = 84 \pm 34$.

The signal-to-background ratio for both studied $\Lambda^+_c$ decay channels is similar. Figure 6 shows the invariant-mass spectrum containing both $\Lambda^+_c \rightarrow pK^0_S$ and $\Lambda^+_c \rightarrow \Lambda\pi^+$ candidates. The fit yielded $N(\Lambda^+_c) = 146 \pm 33$ candidates. This combined peak was not used to extract any cross sections or fragmentation fractions.

8 Cross sections and acceptance corrections

For a given observable, $Y$, the differential cross section in a bin $i$ was determined using

$$\frac{d\sigma_i}{dY} = \frac{N_i(D^+)}{A_i \cdot L \cdot B \cdot \Delta Y_i},$$

where $N_i(D^+)$ is the number of reconstructed $D^+$ mesons in bin $i$ having size $\Delta Y_i$. The reconstruction acceptance, $A_i$, takes into account migrations, efficiencies and QED radiative effects for the $i^{th}$ bin, $L$ is the integrated luminosity and $B$ is the branching ratio [54] for the decay channel used in the reconstruction (see table 1). The total visible production cross sections were determined using

$$\sigma = \frac{N(D^+, \Lambda^+_c)}{A \cdot L \cdot B},$$

where $N(D^+, \Lambda^+_c)$ and $A$ were determined for the whole kinematic range of the measurement. All acceptances were obtained from the Monte Carlo.
The $b$-quark contribution, predicted by the MC simulation, was subtracted from all measured cross sections. The RAPGAP prediction for beauty production was multiplied by two, in agreement with a previous ZEUS measurement of beauty production in DIS [56]. The subtraction of the $b$-quark contribution reduced the measured cross sections by $2-3\%$ for the $D^+$ and about $1\%$ for the $\Lambda^+_c$.

There is no sizeable acceptance for charmed hadrons in the transverse-momentum range $0 < p_T(D^+, \Lambda^+_c) < 0.5\text{ GeV}$. Hence an extrapolation using the reference Monte Carlo was performed when the cross sections were extracted. For example, the extrapolation accounts for $6\%$ of the $D^+$ production in the full kinematic range of the measurement and for $11\%$ of the $D^+$ production in the restricted range $0 < p_T(D^+) < 1.5\text{ GeV}$.

9 Systematic uncertainties

The systematic uncertainties of the measured cross sections and fragmentation fractions were determined by changing the analysis procedure and repeating all calculations. In the measurement of the differential and total cross sections, the following groups of systematic uncertainty sources were considered. The effects on the total cross sections are shown in parentheses ($D^+; \Lambda^+_c \rightarrow pK^0_S; \Lambda^+_c \rightarrow \Lambda\pi^+$):

- $\{\delta_1\}$ event and DIS selection ($-4\%$, $+1\%$, $+8\%$). The following cut variations were applied to data and MC simultaneously:
  - the cut on $y_{JB}$ was changed to $y_{JB} > 0.03$;
  - the cut on the scattered electron energy $E'_e$ was changed to $E'_e > 11 \text{ GeV}$;
  - the cuts on $\delta$ were changed by $+2 \text{ GeV}$;
  - the cut on $|Z_{\text{vertex}}|$ was changed to $|Z_{\text{vertex}}| < 45 \text{ cm}$;
  - additionally, a box cut of $26 \times 14 \text{ cm}^2$ was used for all electron candidates without an SRTD requirement;
- $\{\delta_2\}$ $Q^2$ and $x$ reconstruction ($-1\%$; $-3\%$; $-6\%$). The DA method was used for the reconstruction of $Q^2$ and $x$ instead of the electron method;
- $\{\delta_3\}$ energy scale ($\pm2\%$, $+3\%$; $+2\%$). To account for the uncertainty of the absolute CAL energy scale, the energy of the scattered electron was raised and lowered by $1\%$ and $E^0_{T,\gamma} > 10^9$ was raised and lowered by $2\%$. These variations were only applied to the MC;
- $\{\delta_4\}$ model dependence of the acceptance corrections:
  - the process $cg \rightarrow cg$ was included in the RAPGAP MC sample ($+5\%$, $+3\%$, $+9\%$);
  - the MC samples were not reweighted in $p_T(D^+, D^+_s, \Lambda^+_c)$ ($-17\%$, $-6\%$, $-21\%$);
- $\{\delta_5\}$ uncertainty of the beauty subtraction ($+1\%$, $-3\%$, $+1\%$; $<1\%$). This was determined by varying the subtracted $b$-quark contributions by a factor 2;
\begin{itemize}
\item \{\delta_6\} uncertainty of the signal extraction procedure (+12\%, +14\%, +24\%):
\begin{itemize}
\item the fit was repeated changing the invariant mass window of 1.6 \text{ – } 2.1 \text{ GeV} by \pm 50 \text{ MeV} on both sides for \(D^+ \rightarrow K_S^0 \pi^+\) decays. Similarly, the considered invariant mass region of 2.0 \text{ – } 2.5 \text{ GeV} was changed by \pm 50 \text{ MeV} for \(\Lambda_c^+ \rightarrow pK_S^0\) decays and by \pm 30 \text{ MeV} for the channel \(\Lambda_c^+ \rightarrow \Lambda \pi^+\);
\item the choice of the background function was assigned an uncertainty of \pm 5\%.
\end{itemize}
\item the uncertainty in the luminosity measurement of \pm 2.0\%.
\end{itemize}

The following uncertainty was considered only for the decays \(D^+ \rightarrow K_S^0 \pi^+\) and \(\Lambda_c^+ \rightarrow K_S^0 p\):
\begin{itemize}
\item \{\delta_8\} \(K_S^0\) reconstruction (+2\%; +1\%; –). Since the MC signal had a narrower width than observed in the data, the invariant-mass window for the \(K_S^0\) candidate selection was reduced to 0.486 < \(M(\pi^+\pi^-)\) < 0.510 \text{ GeV} in the MC only.
\end{itemize}

The following source of uncertainty was considered only for the decay \(D^+ \rightarrow K_S^0 \pi^+\):
\begin{itemize}
\item \{\delta_9\} uncertainty of the reflection subtraction (\pm 5\%; –; –). The normalisation of the \(D_S^+\) reflection was changed by the uncertainty of \(R\) (see eq. (7.3)) due to the uncertainties of the fragmentation fractions and branching ratios used in the calculation.
\end{itemize}

The following source of uncertainty was considered only for the decay \(\Lambda_c^+ \rightarrow K_S^0 p\):
\begin{itemize}
\item \{\delta_{10}\} proton reconstruction (–; –14\%; –). The following checks were performed:
\begin{itemize}
\item the number of hits required for the proton candidates was lowered to 32;
\item the uncertainty of the \(dE/dx\) simulation for low-momentum protons was evaluated changing the parametrisation of the proton band [55];
\item the cut on the energy loss was lowered to \(dE/dx > 1.15\) mips.
\end{itemize}
\end{itemize}

The following source of uncertainty was considered only for the decay \(\Lambda_c^+ \rightarrow \Lambda \pi^+\):
\begin{itemize}
\item \{\delta_{11}\} \(\Lambda\) reconstruction (–; –; +4\%). Since the MC signals had a narrower width than observed in the data, the invariant-mass window for the \(\Lambda\) candidate selection was reduced to 1.113 < \(M(p\pi)\) < 1.120 \text{ GeV} in the MC only.
\end{itemize}
Contributions from the different systematic uncertainties were calculated and added in quadrature separately for positive and negative variations. These estimates were made in each bin in which the differential cross sections were measured. Uncertainties due to those on the luminosity measurement and branching ratios were only included in the measured $D^+$ and $\Lambda_c^+$ total cross sections. For differential cross sections, these uncertainties are not included.

As an additional check, the $dE/dx$ efficiency for pions and protons was verified directly in the data using $K^0_S$ and $\Lambda$ decays. For the $D^+ \to K^0_S \pi^+$ decay channel, the effect of the $dE/dx$ cut on the pion candidate tracks was very small and the result changed only marginally when the cut was released.

The average cross sections obtained from the two different running periods ($\sqrt{s} = 300$ and 318 GeV) are expressed in terms of cross sections at $\sqrt{s} = 318$ GeV. This involves a typical correction of $+1\%$ determined using HVQDIS.

10 Results

Charm hadron cross sections were measured using the reconstructed $D^+$ and $\Lambda_c^+$ signals (see section 7) in the kinematic range $0 < p_T(D^+, \Lambda_c^+) < 10$ GeV, $|\eta(D^+, \Lambda_c^+)| < 1.6$, $1.5 < Q^2 < 1000$ GeV$^2$ and $0.02 < y < 0.7$.

In addition to the statistical and systematic uncertainties, a third set of uncertainties is quoted for the measured cross sections and charm fragmentation fractions, due to the propagation of the relevant branching-ratio uncertainties (table 1).

10.1 $D^+$ cross sections

The following total visible cross section for $D^+$ mesons was measured:

$$\sigma(D^+) = 25.7 \pm 4.1 \text{ (stat.)} ^{+3.8}_{-5.2} \text{ (syst.)} \pm 0.8 \text{ (br.)} \text{ nb.}$$

The corresponding prediction from HVQDIS is $\sigma(D^+) = 12.7 ^{+3.8}_{-4.1}$ nb. The measured and predicted cross sections are in agreement to better than two standard deviations.

To allow a direct comparison to a recent measurement of $D^+$ production by the ZEUS collaboration using a lifetime tag [8], the cross section was extracted for the kinematic region defined by $1.5 < p_T(D^+) < 15$ GeV, $|\eta(D^+)| < 1.6$, $5.0 < Q^2 < 1000$ GeV$^2$ and $0.02 < y < 0.7$. The measurements using different decay channels and different techniques were found to be consistent.

The differential cross sections as functions of $p_T^2(D^+)$, $\eta(D^+)$, $x$ and $Q^2$ are shown in figure 7 and given in table 2. The cross sections in $Q^2$ and $x$ fall by about three orders of magnitude, while the cross section in $p_T^2(D^+)$ falls by about two orders of magnitude in the measured region. There is no significant dependence of the cross section on $\eta(D^+)$. The HVQDIS predictions describe the shape of all measured differential cross sections reasonably well. The differential cross section in $p_T^2(D^+)$ is compared to a previous ZEUS result [7] for $p_T^2(D^+) > 9$ GeV$^2$. The two measurements are in good agreement.
10.2 $\Lambda_c^+$ cross sections and fragmentation fractions

The following $\Lambda_c^+$ cross sections were measured:

- using the decay channel $\Lambda_c^+ \rightarrow pK^0_S$ in the restricted range $0 < p_T(\Lambda_c^+) < 6$ GeV:
  \[ \sigma(\Lambda_c^+) = 14.9 \pm 4.9 \text{ (stat.)} ^{+2.2}_{-2.6} \text{ (syst.)} \pm 3.9 \text{ (br.) \ nb}; \]

- using the decay channel $\Lambda_c^+ \rightarrow \Lambda\pi^+$:
  \[ \sigma(\Lambda_c^+) = 14.0 \pm 5.8 \text{ (stat.)} ^{+3.8}_{-3.3} \text{ (syst.)} \pm 3.7 \text{ (br.) \ nb}. \]
Table 2. Measured $D^+$ cross sections as a function of $p_T^2(D^+)$, $\eta(D^+)$, $Q^2$ and $x$ for $1.5 < Q^2 < 1000$ GeV$^2$, $0.02 < y < 0.7$, $0 < p_T(D^+) < 10$ GeV and $|\eta(D^+)| < 1.6$. The statistical and systematic uncertainties are shown separately. The cross sections have further uncertainties of 3% from the $D^+ \to K_S^0 \pi^+ \to \pi^+\pi^-\pi^+$ branching ratio, and 2% from the uncertainty in the luminosity measurement.

To compare and combine both measurements, the value obtained for the decay channel $\Lambda_c^+ \to pK_S^0$ was multiplied by $1.01 \pm 0.01$ to extrapolate to the full kinematic region considered in this paper. The cross sections obtained using different decay channels are in good agreement. To extract the $\Lambda_c^+$ fragmentation fraction, the measurements were combined taking into account all systematic uncertainties and their correlations:

$$\sigma_{\text{combined}}(\Lambda_c^+) = 14.7 \pm 3.8 \, \text{(stat.)} \pm 2.1 \, \text{(syst.)} \pm 3.9 \, \text{(br.)} \, \text{nb.}$$

The uncertainty of the branching ratio was treated as partially correlated since both branching ratios, $B(\Lambda_c^+ \to pK_S^0)$ and $B(\Lambda_c^+ \to \Lambda \pi^+)$, were measured relative to the decay mode $\Lambda_c^+ \to pK^-\pi^+$ [54].

The fragmentation fraction $f(c \to \Lambda_c^+)$ can be calculated using the $D^+$ cross section:

$$f(c \to \Lambda_c^+) = \frac{\sigma(\Lambda_c^+)}{\sigma(D^+)} \cdot f(c \to D^+). \quad (10.1)$$
In a previous ZEUS publication [7], \( f(c \rightarrow D^+) \) was defined as:

\[
f(c \rightarrow D^+) = \frac{\sigma^0(D^+)}{\sigma^0(D^+) + \sigma^0(D^0) + \sigma^0(D_s^+)} \cdot \left[ 1 - 1.14 \cdot f(c \rightarrow \Lambda^+_c) \right],
\]

(10.2)

where \( \sigma^0(D^+) \), \( \sigma^0(D^0) \) and \( \sigma^0(D_s^+) \) are the cross sections for \( p_T(D) > 3 \text{ GeV} \). The factor 1.14 takes into account the production of charm-strange baryons [7]. For \( D^+ \) and \( D^0 \) mesons, the equivalent cross sections (as described elsewhere [9]) were used. Combining eqs. (10.1) and (10.2) yields:

\[
f(c \rightarrow \Lambda^+_c) = \frac{\sigma(\Lambda^+_c) \cdot \sigma^0(D^+)}{\sigma(D^+) \cdot (\sigma^0(D^+) + \sigma^0(D^0) + \sigma^0(D_s^+)) + 1.14 \sigma(\Lambda^+_c) \cdot \sigma^0(D^+)}.\]

Since the cross sections \( \sigma(D^+) \) and \( \sigma(\Lambda^+_c) \) were measured down to \( p_T(D^+, \Lambda^+_c) = 0 \text{ GeV} \), no treatment of the different transverse momentum distributions for \( D^+ \) and \( \Lambda^+_c \) was necessary. The measured value:

\[
f(c \rightarrow \Lambda^+_c) = 0.117 \pm 0.033 \text{ (stat.)}^{+0.026}_{-0.022} \text{ (syst.)} \pm 0.027 \text{ (br.)},
\]

is compared to previous measurements in table 3. The result is consistent with a previous ZEUS measurement in the photoproduction regime [9] and with the \( e^+e^- \) average value.

### 11 Conclusions

Open-charm production in \( ep \) collisions at HERA has been measured in deep inelastic scattering using three decay channels. The presence of a neutral strange hadron in the final state allowed the measurement to be extended to very low transverse momenta of the reconstructed charm hadrons. The total visible and differential cross sections for \( D^+ \) production are in reasonable agreement with NLO QCD predictions. The measured \( D^+ \) cross sections are consistent with previous ZEUS results. The fragmentation fraction \( f(c \rightarrow \Lambda^+_c) \) has been measured for the first time at HERA in deep inelastic scattering. The result obtained from a combination of two decay channels is consistent with a previous measurement performed in the photoproduction regime and with the average \( e^+e^- \) value.

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References


