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Plasmon-assisted two-photon Rabi oscillations in a semiconductor quantum dot – metal nanoparticle heterodimer

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Two-photon Rabi oscillations hold potential for quantum computing and quantum information processing because during a Rabi cycle a pair of entangled photons may be created. We theoretically investigate the onset of this phenomenon in a heterodimer comprising a semiconductor quantum dot strongly coupled to a metal nanoparticle. Two-photon Rabi oscillations in this system occur due to a coherent two-photon process involving the ground-to-biexciton transition in the quantum dot. The presence of a metal nanoparticle near the quantum dot results in a self-action of the quantum dot via the metal nanoparticle because the polarization state of the latter depends on the quantum state of the former. The interparticle interaction gives rise to two principal effects: (i) enhancement of the external field amplitude and (ii) renormalization of the quantum dot's resonance frequencies and relaxation rates of the off-diagonal density matrix elements, both depending on the populations of the quantum dot's levels. Here, we focus on the first effect, which results in interesting features, in particular, an increased number of Rabi cycles per pulse compared to an isolated quantum dot and subsequent growth of the number of entangled photon pairs per pulse. We also discuss the destructive role of radiative decay of the excitonic states on two-photon Rabi oscillations for both an isolated quantum dot and a heterodimer.

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I. INTRODUCTION

Nanohybrids comprising a quantum emitter (QE) coupled to a metal nanoparticle (MNP) have been shown to exhibit a variety of novel optical properties which not only are intriguing in their own right but also offer great prospects for applications. In spite of considerable recent interest in hybrid QE-MNP systems, a number of questions regarding their optical properties have not been elucidated so far. One of those concerns the nonlinear optical interactions occurring in a QE-MNP nanohybrid, namely, the onset of coherent two-photon processes, in particular, coherent two-photon absorption (TPA) and two-photon Rabi oscillations (TPRO). Although two-photon processes generally are weak, they may serve efficiently for various applications. The characteristics of two-photon processes make them superior to other room-temperature schemes based on all-optical nonlinear processes [1]. The best-known examples of practical applications of TPA are microfabrication via three-dimensional photopolymerization [2,3], imaging [4], and optical data storage [5–7]. The principle of using TPA processes is based on the fact that many materials, while not being transparent for radiation in the visible, are transparent in the infrared. This allows one to reach the bulk materials with infrared light, where TPA processes may be used for optical applications such as the ones mentioned above.

The most interesting application of TPRO envisioned at the moment is the realization of a single-emitter source of pairs of polarization-entangled photons, which is a challenge for quantum computing and quantum information processing [8,9], as well as for quantum cryptography [10]. A single

semiconductor quantum dot (SQD) is considered an excellent candidate for efficient TPRO, as one may exploit the multiexciton states, in particular, biexciton states that naturally occur in these systems, to achieve this phenomenon.

During a cascade emission from the biexciton state of a SQD, a pair of polarization-entangled photons is created with its polarization determined by the spin of the intermediate exciton state [11–16]. However, the entanglement is not complete because of the hyperfine splitting of one-exciton states forming the biexciton. This is the major obstacle for high-quality polarization entanglement when using the cascade process. Additional manipulations are needed to reduce the splitting and improve entanglement [11]. This problem is avoided by placing a SQD into a microcavity [17,18] tuned exactly to the coherent two-photon resonance. Due to the biexciton shift, single-photon transitions are detuned and thus are effectively suppressed, while the coherent two-photon emission is Purcell enhanced [19]. An additional enhancement of the two-photon rate comes from the fact that the intermediate-state denominator, determining the rate, is equal to half of the biexciton binding energy, which is usually on the order of several meV, i.e., relatively small for the second-order processes.

The TPRO represents a coherent process, involving the ground-to-biexciton transition, in which the intermediate one-exciton states play the role of virtual states, which are not populated, so that two photons created during one Rabi cycle are perfectly entangled by default. Importantly, this can be realized in a cavity-free configuration [20,21]. Coherent control of the biexciton state of an isolated SQD has been achieved

FIG. 1. (a) Schematics of a SQUID-MNP heterodimer subject to a pulsed applied field $\mathcal{E}_0(t) = E_0(t) \cos(\omega_0 t)$. The field is linearly polarized along the system axis (shown by the red arrow). Here, d is the SQUID-MNP center-to-center distance, r is the radius of the MNP, ε_s and $\varepsilon_m(\omega)$ are the dielectric constants of the SQUID and the MNP, respectively. The system is embedded in an isotropic and nonabsorbing medium with permittivity ε_b . (b) Energy diagrams of the MNP (left) and a ladder-type three-level SQUID (right). The excited state of the MNP represents a broad line centered at the frequency of the LSP's resonance ω_{LSP} , shown by the dashed yellow line. For the SQUID, $|1\rangle$, $|2\rangle$, and $|3\rangle$ are the ground, one-exciton, and biexciton states, respectively. The energies of these states are $\varepsilon_1 = 0$, $\varepsilon_2 = \hbar\omega_2$, and $\varepsilon_3 = 2\hbar(\omega_2 - \Delta_B/2)$, where $\hbar\Delta_B$ is the biexciton binding energy. Allowed transitions with the corresponding transition dipole moments μ_{21} and μ_{32} are indicated by solid double-headed arrows. Wiggly arrows denote the spontaneous decay with rates γ_{32} and γ_{21} . The black dashed line shows the location of the coherent two-photon resonance $\omega_3/2 = \omega_2 - \Delta_B/2$ (with simultaneous absorption of two photons).

within two-pulse [13,22] and single-pulse [23] schemes of excitation followed by the cascade emission of a pair of entangled photons. The first observation of the cavity-free TPRO of a single InGaAs SQUID was reported by Stufli *et al.* [20] together with a simplified theoretical approach explaining the peculiarities of the effect. A more comprehensive theory was presented in Ref. [24].

In this paper, we examine theoretically the TPRO in a SQUID strongly coupled to a MNP, where the SQUID, as in Ref. [20], is modeled as a ladderlike three-level system (ground, one-exciton, and biexciton states). It is well established that the presence of a MNP near a SQUID has a vital influence on the optical response of the SQUID as a consequence of the polarizability of the MNP. Notable phenomena that have been studied in detail are the bistable optical response [25–29], linear and nonlinear Fano resonances [30–32], gain without inversion [33], and several other effects [34–36]. Our goal is to uncover the plasmonic effect on the TPRO of a single SQUID.

This paper is organized as follows. In the next section, we present the model system and the mathematical formalism for its description. In Sec. III, we report the results of numerical calculations of the TPRO for a set of parameters that is achievable in practice and discuss them. In Sec. IV, we analyze under what conditions additional nonlinear effects, resulting from the self-action-induced renormalization of the effective exciton energies and relaxation rates, may occur. Section V summarizes the paper.

II. MODEL AND FORMALISM

We theoretically investigate coherent light-matter interaction in a nanohybrid composed of a SQUID coupled to a closely spaced spherical MNP. The nanoparticles are embedded in an isotropic and lossless background with permittivity ε_b and are separated by a (center-to-center) distance d . The SQUID is characterized by its (bulk) dispersionless dielectric constant ε_s , while the MNP is described by the dielectric function $\varepsilon_m(\omega)$. The system is driven by a pulsed external field

$\mathcal{E}_0(t) = E_0(t) \cos(\omega_0 t)$, with a carrier frequency ω_0 and an amplitude $E_0(t)$ which varies slowly on the scale of the optical period $2\pi/\omega_0$. The field is linearly polarized along the system's axis [see Fig. 1(a)]. The SQUID and MNP radii as well as their center-to-center distance d are assumed to be small compared to the optical wavelength, allowing us to apply the quasistatic approximation [37,38] and to neglect the retardation in the SQUID-MNP interaction.

Figure 1(b) shows the schematics of the electronic states and corresponding energy levels of the nanohybrid. The oscillating external field gives rise to oscillations of conducting electrons in the MNP, conventionally called a localized surface plasmon (LSP). For the MNP's radii $r > 5$ nm we consider, quantum-size effects are negligible [39], so that for LSPs, the classical treatment can be safely applied [38]. Within this approach, the MNP's optical response can be described by its complex-valued frequency-dependent polarizability $\alpha(\omega)$, given by [37,38]

$$\alpha(\omega) = 4\pi r^3 \frac{\varepsilon_m(\omega) - \varepsilon_b}{\varepsilon_m(\omega) + 2\varepsilon_b}. \quad (1)$$

The LSP's resonance frequency ω_{LSP} is determined as the frequency at which the real part of $\alpha(\omega)$ is minimal (Fröhlich condition) [37]. Thus, the electronic states of the LSP represent a ground state and a broad continuum of excited states, as depicted in Fig. 1(b) (left panel).

The optical excitations in the SQUID are excitons. In addition to the one-exciton states of the SQUID, we also incorporate a biexciton state, corresponding to two excitations coupled by the Coulomb interaction. In such a system, the degeneracy of the two one-exciton states is lifted due to the anisotropic electron-hole exchange, leading to two split linearly polarized one-exciton states with a negligible energy splitting (on the order of a few tens of μeV), one of which is dark, while the other is bright (see, e.g., Refs. [20,40,41]). In this case, the ground state is coupled to the biexciton state via the linearly polarized one-exciton bright state. Thus, the system effectively acquires a three-level structure with a ground state

$|1\rangle$, one-exciton state $|2\rangle$, and biexciton state $|3\rangle$ with corresponding energies 0 , $\hbar\omega_2$, and $\hbar\omega_3 = 2\hbar(\omega_2 - \Delta_B/2)$, where $\hbar\Delta_B$ is the biexciton binding energy. Within this model, the allowed transitions, induced by the external field, are $|1\rangle \leftrightarrow |2\rangle$ and $|2\rangle \leftrightarrow |3\rangle$, which are characterized by the transition dipole moments $\mu_{21}(=\mu_{12})$ and $\mu_{32}(=\mu_{23})$, respectively (for the sake of simplicity, we assume that they are real). States $|3\rangle$ and $|2\rangle$ spontaneously decay with rates γ_{32} and γ_{21} [see Fig. 1(b)] [42]. Note that the biexciton state $|3\rangle$, having no allowed transition dipole moment from the ground state $|1\rangle$, can be reached either via consecutive $|1\rangle \rightarrow |2\rangle \rightarrow |3\rangle$ transitions or via the simultaneous absorption of two photons of frequency $\omega_3/2 = \omega_2 - \Delta_B/2$. At resonant excitation, each of these transitions can be addressed separately. This remains valid also for a pulsed excitation if the pulses are spectrally narrower than the biexciton binding energy $\hbar\Delta_B$. We will predominantly focus our study on the resonant excitation of the coherent two-photon transition.

Excitons and plasmons, excited in the nanohybrid, interact with each other via the dipole-dipole interaction, which gives rise to a renormalization of the field experienced by both the SQD and MNP. The effects of the coupling can be inferred from the amplitude of the total field acting on the SQD, which equals the sum of the external field $E_0(t)$ and the field produced by the MNP [25–29]. Accounting for the contribution of higher multipoles, which is important if the MNP's radius r is on the order of the SQD-MNP spacing d (our case; see below), $E_{\text{SQD}}(t)$ reads [36,43]

$$E_{\text{SQD}}(t) = \frac{1}{\varepsilon'_s} \left[1 + \frac{\alpha(\omega_0)}{2\pi d^3} \right] E_0(t) + \frac{1}{4\pi^2 \varepsilon_0 \varepsilon_b \varepsilon'_s} \times \sum_{n=1}^{\infty} \frac{(n+1)^2 \alpha_n(\omega_0)}{d^{2n+4}} P_{\text{SQD}}(t). \quad (2)$$

Here, $\varepsilon'_s = (\varepsilon_s + 2\varepsilon_b)/(3\varepsilon_b)$ is the effective dielectric constant of the SQD; $P_{\text{SQD}}(t)$ is the amplitude of the dipole moment generated in the SQD [see below, Eq. (5)]. Furthermore, the higher multipole polarizabilities $\alpha_n(\omega_0)$ are given by

$$\alpha_n(\omega_0) = 4\pi r^{2n+1} \frac{\varepsilon_m(\omega_0) - \varepsilon_b}{\varepsilon_m(\omega_0) + \frac{n+1}{n} \varepsilon_b}. \quad (3)$$

The first term in Eq. (2) shows that the external field amplitude $E_0(t)$ experiences renormalization due to the presence of the nearby MNP (second term in the square brackets). The last term in Eq. (2) reveals the electromagnetic self-action of the SQD via the MNP: the field acting upon the SQD depends on the amplitude of its own dipole moment $P_{\text{SQD}}(t)$. As will be shown below, this may considerably affect the hybrid's TPRO compared to those of an isolated SQD.

It is worth noting that all polarizabilities in Eq. (2) are taken at the carrier frequency of the external field ω_0 . Throughout this paper, we assume that the spectral width of the envelope $E_0(t)$ is narrow enough to neglect variations of the polarizabilities over this interval. For the parameters chosen in our calculations, this condition is fulfilled easily.

We describe the optical process in the SQD by making use of the Lindblad quantum master equation for the density operator $\rho(t)$, which in the rotating frame (with frequency ω_0

of the external field) reads [44,45]

$$\dot{\rho} = -\frac{i}{\hbar} [\mathcal{H}^{\text{RWA}}(t), \rho] + \mathcal{L}(\rho), \quad (4a)$$

$$\mathcal{H}^{\text{RWA}}(t) = \hbar(\Delta_{21}|2\rangle\langle 2| + \Delta_{31}|3\rangle\langle 3|) - \hbar[\Omega_{21}(t)|2\rangle\langle 1| + \Omega_{32}(t)|3\rangle\langle 2| + \text{H.c.}], \quad (4b)$$

$$\mathcal{L}(\rho) = \frac{\gamma_{21}}{2} ([|1\rangle\langle 2|\rho, |2\rangle\langle 1|] + [|1\rangle\langle 2|, \rho |2\rangle\langle 1|]) + \frac{\gamma_{32}}{2} ([|2\rangle\langle 3|\rho, |3\rangle\langle 2|] + [|2\rangle\langle 3|, \rho |3\rangle\langle 2|]). \quad (4c)$$

Here, $[A, B]$ denotes the commutator, $\mathcal{H}^{\text{RWA}}(t)$ is the SQD Hamiltonian in the rotating-wave approximation (RWA), and $\mathcal{L}(t)$ is the Lindblad operator describing the radiative relaxation in the system. In Eq. (4b), $\hbar\Delta_{21} = \hbar(\omega_2 - \omega_0)$ and $\hbar\Delta_{31} = \hbar(\omega_3 - 2\omega_0)$ are the energies of states $|2\rangle$ and $|3\rangle$ in the rotating frame, respectively. Alternatively, the former may be interpreted as the detuning away from the one-photon resonance, and the latter may be interpreted as the detuning from the coherent two-photon resonance. $\Omega_{21}(t) = \mu_{21} \cdot E_{\text{SQD}}(t)/(2\hbar)$ and $\Omega_{32}(t) = \mu_{32} \cdot E_{\text{SQD}}(t)/(2\hbar)$ are the slowly varying Rabi amplitudes of $E_{\text{SQD}}(t)$ for the corresponding transitions, where $E_{\text{SQD}}(t)$ is the amplitude of the total field acting on the SQD. The latter is the sum of the applied field $E_0(t)$ and the field produced by the plasmon oscillations in the MNP given by Eq. (2) [25–29]. H.c. stands for the Hermitian conjugate.

The SQD's dipole moment amplitude $P_{\text{SQD}}(t)$ in Eq. (2) is given by

$$P_{\text{SQD}}(t) = \mu_{21}\rho_{21}(t) + \mu_{32}\rho_{32}(t). \quad (5)$$

Thus, the Rabi amplitudes $\Omega_{21}(t)$ and $\Omega_{32}(t)$ may be expressed as follows:

$$\Omega_{21}(t) = \tilde{\Omega}_{21}^0(t) + G_1\rho_{21}(t) + G_3\rho_{32}(t), \quad (6a)$$

$$\Omega_{32}(t) = \tilde{\Omega}_{32}^0(t) + G_3\rho_{21}(t) + G_2\rho_{32}(t), \quad (6b)$$

where we introduced the quantities

$$\tilde{\Omega}_{21}^0(t) = \frac{1}{\varepsilon'_s} \left[1 + \frac{\alpha(\omega_0)}{2\pi d^3} \right] \Omega_{21}^0(t), \quad (7a)$$

$$\tilde{\Omega}_{32}^0(t) = \frac{1}{\varepsilon'_s} \left[1 + \frac{\alpha(\omega_0)}{2\pi d^3} \right] \Omega_{32}^0(t), \quad (7b)$$

and

$$G_1 = \frac{\mu_{21} \cdot \mu_{21}}{16\pi^2 \hbar \varepsilon_0 \varepsilon_b \varepsilon'_s} \sum_n \frac{(n+1)^2 \alpha_n(\omega_0)}{d^{2n+4}}, \quad (8a)$$

$$G_2 = \frac{\mu_{32} \cdot \mu_{32}}{16\pi^2 \hbar \varepsilon_0 \varepsilon_b \varepsilon'_s} \sum_n \frac{(n+1)^2 \alpha_n(\omega_0)}{d^{2n+4}}, \quad (8b)$$

$$G_3 = \frac{\mu_{21} \cdot \mu_{32}}{16\pi^2 \hbar \varepsilon_0 \varepsilon_b \varepsilon'_s} \sum_n \frac{(n+1)^2 \alpha_n(\omega_0)}{d^{2n+4}}. \quad (8c)$$

Here, $\Omega_{21}^0(t) = \mu_{21} \cdot E_0(t)/(2\hbar)$ and $\Omega_{32}^0(t) = \mu_{32} \cdot E_0(t)/(2\hbar)$ are the Rabi amplitudes of the external field for the corresponding transitions. As can be seen, the

external field experiences a renormalization due to the presence of a nearby MNP, which is reflected in the factor $1 + \alpha(\omega_0)/(2\pi d^3)$. The complex-valued quantities $G_1 = G_1^R + iG_1^I$, $G_2 = G_2^R + iG_2^I$, and $G_3 = G_3^R + iG_3^I$ represent the so-called feedback parameters, describing the self-interaction of the SQD via the MNP [25–29]. They contain all details of the SQD-MNP coupling, such as the contribution of higher multipoles, material properties, and geometry of the system.

Using the above, the set of equations for the density matrix elements ρ_{ij} ($i, j = 1, 2, 3$) governing the optical dynamics of the SQD in the presence of the nearby MNP reads [36]

$$\dot{\rho}_{11} = \gamma_{21}\rho_{22} + i(\Omega_{21}^*\rho_{21} - \Omega_{21}\rho_{21}^*), \quad (9a)$$

$$\dot{\rho}_{22} = -\gamma_{21}\rho_{22} + \gamma_{32}\rho_{33} + i(\Omega_{21}\rho_{21}^* - \Omega_{21}^*\rho_{21} + \Omega_{32}^*\rho_{32} - \Omega_{32}\rho_{32}^*), \quad (9b)$$

$$\dot{\rho}_{33} = -\gamma_{32}\rho_{33} + i(\Omega_{32}\rho_{32}^* - \Omega_{32}^*\rho_{32}), \quad (9c)$$

$$\dot{\rho}_{21} = -[i\Delta_{21} + \frac{1}{2}\gamma_{21}]\rho_{21} + i(\Omega_{32}^*\rho_{31} - \Omega_{21}Z_{21}), \quad (9d)$$

$$\dot{\rho}_{32} = -[i\Delta_{32} + \frac{1}{2}(\gamma_{32} + \gamma_{21})]\rho_{32} - i(\Omega_{21}^*\rho_{31} + \Omega_{32}Z_{32}), \quad (9e)$$

$$\dot{\rho}_{31} = -[i\Delta_{31} + \frac{1}{2}\gamma_{32}]\rho_{31} + i(\Omega_{32}\rho_{21} - \Omega_{21}\rho_{32}), \quad (9f)$$

where $\Delta_{32} = \omega_3 - \omega_2 - \omega_0$ is the detuning away from the $|3\rangle \leftrightarrow |2\rangle$ transition and $Z_{ji} = \rho_{jj} - \rho_{ii}$ denotes the population difference between states $|j\rangle$ and $|i\rangle$. Here, we suppressed the time dependence of all dynamic variables.

III. RESULTS AND DISCUSSION

A. Isolated SQD

First, we consider the TPRO of an isolated SQD. This will serve as a reference case for the hybrid analyzed in Sec. III B. Yet another aspect added in this section compared to what has been done in previous studies of the isolated SQD [20,24] is an analysis of the destructive effect of the exciton's spontaneous decay on the TPRO. For the SQD, we use the set of parameters of a CdSe/ZnSe quantum dot with a radius of 3 nm [13]: the energies of the bare one-exciton and biexciton transitions are $\hbar\omega_2 = 2.36$ eV and $\hbar\omega_3 = \hbar(2\omega_2 - \Delta_B)$, with $\hbar\Delta_B = 20$ meV ($\Delta_B \approx 30$ ps⁻¹) and the population radiative decay rates $\gamma_{21} = 1/220$ ps⁻¹ and $\gamma_{32} = 1/120$ ps⁻¹. From these data, the transition dipole moments are evaluated as $\mu_{21} = 0.6$ e nm and $\mu_{32} = 0.8$ e nm. For the SQD's dielectric constant ϵ_s , the typical value $\epsilon_s = 6$ is taken. In the following, we denote $\Omega_0(t) \equiv \Omega_{21}^0(t)$ and $\Omega(t) \equiv \Omega_{21}(t)$. Accordingly, $\Omega_{32}^0(t) = (\mu_{32}/\mu_{21})\Omega_0(t)$, and $\Omega_{32}(t) = (\mu_{32}/\mu_{21})\Omega(t)$.

The system is subjected to a resonant pulsed external field with Gaussian Rabi amplitude,

$$\Omega_0(t) = \frac{A}{\sqrt{\pi}t_0} \exp\left[-\left(\frac{t-t_d}{t_0}\right)^2\right], \quad (10)$$

tuned into the two-photon transition ($\omega_0 = \omega_3/2$, $\Delta_{21} = \Delta_B/2$). In Eq. (10), $A = \int_{-\infty}^{\infty} \Omega_0(t)dt$ is the pulse area, t_d is the delay time until the pulse maximum, and t_0 is the parameter determining the pulse duration t_p , which we define as the pulse full width at half maximum, $t_p = 2\sqrt{\ln 2} t_0$. We

are primarily interested in the behavior of the biexciton state population ρ_{33} .

1. Adiabatic limit

Here, we recall the principal results of the adiabatic theory of the TPRO of an isolated SQD developed in Refs. [20,24]. Adiabaticity means that the coherently driven evolution of the system is slow enough that at each instant in time, the system follows the adiabatic instantaneous eigenstate of the Hamiltonian (4b) (see, e.g., Ref. [46]). This limit involves certain relationships between the system's parameters $\Omega_0(t)$, t_0 , Δ_B , and γ_{32}^{-1} . First, adiabaticity requires the inequality $\Delta_B t_0 \gg 1$, which means that the spectral width of the incident pulse, $\approx 1/(2t_0)$, is much smaller than the detuning away from the one-exciton resonance $\Delta_B/2$, so that the transition to the latter is almost forbidden. This criterion is obeyed better the longer the pulse is. On the other hand, the pulse duration must be much shorter than the biexciton decay time, $t_0 \ll \gamma_{32}^{-1}$. Otherwise, the one-exciton state will be incoherently populated via the biexciton state during the pulse action, thus destroying the coherent TPRO.

We restrict ourselves to a simplified version of the adiabatic theory of the TPRO, assuming that the Rabi amplitude $A/(\sqrt{\pi}t_0)$ is much smaller than half the biexciton binding frequency $\Delta_B/2$. In this limit, the perturbation theory can be applied. A more comprehensive treatment (free of this assumption) can be found in Refs. [20,24].

The two-photon Rabi amplitude $\Omega_2(t)$, calculated using second-order perturbation theory, reads

$$\Omega_2(t) = \frac{2\Omega_{21}(t)\Omega_{32}(t)}{\Delta_B\epsilon_s'^2} = \frac{2}{\Delta_B} \frac{\mu_{32}}{\mu_{21}} \left[\frac{\Omega_0(t)}{\epsilon_s'} \right]^2. \quad (11)$$

Accordingly, the area of the two-photon pulse can be written as

$$A_2 = \int_{-\infty}^{\infty} \Omega_2(t)dt = \sqrt{\frac{2}{\pi}} \frac{\mu_{32}}{\mu_{21}} \left(\frac{A}{\epsilon_s'} \right)^2 \frac{1}{\Delta_B t_0}. \quad (12)$$

The A_2 dependence of the biexciton population is given by [20,24]

$$\rho_{33} = \sin^2 \frac{A_2}{2}. \quad (13)$$

Thus, the biexciton population acquires its first maximum, $\rho_{33} = 1$ (full population), at $A_2 = \pi$, similar to that of the one-photon counterpart, except that the area of the two-photon pulse A_2 depends quadratically on the area of the incident pulse A [see Eq. (12)].

Equating $A_2 = \pi$, one can evaluate the incident pulse area A at which the biexciton state is fully populated:

$$A_{A_2=\pi} = \epsilon_s' \left(\pi \sqrt{\frac{\pi}{2}} \frac{\mu_{21}}{\mu_{32}} \Delta_B t_0 \right)^{1/2}. \quad (14)$$

From this estimate it follows that on increasing the incident pulse duration t_0 , a larger area of the incident pulse is needed to invert the system. Moreover, it increases proportionally to $t_0^{1/2}$, which is consistent with our numerical calculations (see Sec. III A 2). Note that the corresponding Rabi amplitude of the incident pulse $\Omega_0(t)$ decreases inversely proportionally to $t_0^{1/2}$. The latter, together with narrowing of the pulse spectrum

FIG. 2. Contour plots of the TPRO of an isolated SQD. Top: population of the biexciton state ρ_{33} . The white dashed curve shows the t_0 dependence of the incident pulse area A , at which ρ_{33} acquires its first maximum, plotted according to Eq. (14) with a correction coefficient of 0.62. Bottom: population of the one-exciton state ρ_{22} .

for increasing t_0 , points to the fact that the contribution of the intermediate one-exciton state to the TPRO will be less important for pulses of a larger duration, which is also in agreement with numerical data (see Sec. III A 2).

2. Numerical results

In Fig. 2, we present the contour plots of the populations of the bi- and one-exciton states obtained by numerically integrating Eqs. (9a)–(9f). Figure 2 clearly exhibits TPRO when following the behavior of ρ_{33} as a function of pulse area at constant pulse duration. In the ρ_{33} plot, the white dashed curve displays the theoretical fit of the ρ_{33} maxima. The fitting procedure was as follows. We approximated the long-pulse numerical data ($\Delta_B t_0 \gg 1$) with the help of the adiabatic result, Eq. (14), allowing for a constant prefactor on the right-hand side of this equation. It turns out that an excellent fit was achieved when a prefactor of 0.62 was used. This fit, however, breaks down for $\Delta_B t_0$ on the order of unity, as expected.

Figure 3 shows the area dependence of ρ_{33} and ρ_{22} for the region of failure of the adiabatic theory ($\Delta_B t_0 \sim 1$). As follows from the plots, this limit describes the actual behavior better for increasing t_0 , and already starting at $t_0 = 8/\Delta_B$, the adiabatic approximation can be safely applied. We relate the slight increase in the one-exciton population ρ_{22} to the direct excitation of this state due to its finite width γ_{21}^{-1} , as well as its

FIG. 3. Area dependence of the populations of the bi- and one-exciton states for the different incident pulse durations indicated above each panel. $\Delta_B = 30 \text{ ps}^{-1}$.

population via the biexciton state, both occurring during each Rabi cycle. The bottom plot in Fig. 2 presents a more detailed picture of the ρ_{22} contribution to the TPRO.

An example of the time evolution of populations for a short pulse ($t_0 = 20/\Delta_B = 2/3 \text{ ps} \ll \gamma_{21}^{-1}, \gamma_{32}^{-1}$) is presented in Fig. 4. Here, we are almost in the purely adiabatic regime. Indeed, the pulse spectrum, having a width that may be estimated as $1/(2t_0)$, is 20 times narrower than half the biexciton binding frequency $\Delta_B/2$ (detuning away from the one-exciton resonance), the condition for adiabaticity [20,24]. On the other

FIG. 4. Population dynamics calculated for the incident pulse with area $A = 9\pi$, duration $t_0 = 20/\Delta_B = 2/3 \text{ ps}$, and delay time $t_d = 2 \text{ ps}$. The red dotted curve shows the profile of the incident Gaussian pulse, $\exp\{-(t - t_0)^2/t_d^2\}$.

FIG. 5. Same as in Fig. 4, but for $A = 50\pi$, $t_0 = 900/\Delta_B = 30$ ps, and $t_d = 100$ ps.

hand, the maximal value of the Rabi amplitude of the incident pulse $A/(\sqrt{\pi}t_0)$ for the value $A = 9\pi$ used to calculate this figure is equal to $0.8\Delta_B$, i.e., even larger than $\Delta_B/2$. This explains the relatively elevated population of the one-exciton state during the pulse action. The effects of radiative decay of the bi- and one-exciton states, giving rise to the incoherent population of the one-exciton state, are negligible in the considered case because the duration of the incident pulse is much shorter than the spontaneous decay time of the biexciton state, $t_0 = 2/3$ ps $\ll \gamma_{32}^{-1} = 120$ ps.

The results presented in Figs. 2–4 were obtained for relatively short incident pulses, $t_0 \leq 50/\Delta_B = 5/3$ ps. At such pulse durations, the effects of the spontaneous decay are marginal, as was already noticed. It is interesting to look at longer pulses, when this process comes into play. Figure 5 shows the population dynamics calculated for a significantly longer incident pulse, $t_0 = 900/\Delta_B = 30$ ps. Here, the pulse spectrum width $\approx 1/(2t_0)$ is 900 times narrower than half the biexciton binding frequency, $\Delta_B/2$. From this point of view, we are deep in the adiabatic limit. The maximal value of the Rabi amplitude of the incident pulse $A/(\sqrt{\pi}t_0)$ for $A = 50\pi$ used in this case is equal to $0.1\Delta_B$, i.e., significantly smaller than $\Delta_B/2$. Thus, contrary to the previous case of a short pulse, the one-exciton state would not be expected to be noticeably excited. Nevertheless, as seen in Fig. 5, its population progressively grows during the pulse action and even onward, not disappearing after the pulse has passed, which happens in the adiabatic case. We explain this behavior by the fact that the timescale of the incident pulse, $t_0 = 30$ ps (duration ≈ 60 ps), is already comparable with the timescale of the spontaneous decay of the biexciton state, $\gamma_{32}^{-1} = 120$ ps. Thus, the latter process leads to incoherent population of the one-exciton state during the pulse action and afterward and thereby destroys the TPRO. Thus, a trade-off exists between the adiabaticity, supporting the pure TPRO, and the spontaneous decay, which breaks down the coherence of the TPRO.

B. SQD-MNP hybrid

In this section, we analyze the TPRO of a hybrid comprising a CdSe/ZnSe quantum dot and a nearby spherical gold MNP, both embedded in a host with permittivity $\varepsilon_b = 2.16$

FIG. 6. Contour plots of the TPRO of a SQD-MNP hybrid calculated for a center-to-center distance $d = 18$ nm. Top: population of the biexciton state ρ_{33} . The dashed white curve shows the t_0 dependence of the incident pulse area $\tilde{A}$, at which ρ_{33} acquires its first maximum, plotted according to Eq. (15) with a correction prefactor of 0.62. Bottom: population of the one-exciton state ρ_{22} .

(silica). For the SQD, we keep the same parameters as in Sec. III A. The gold nanosphere is chosen to have radius $a = 12$ nm. Its dielectric function ε_m is calculated by making use of an improved Drude-like model [47]. The corresponding surface plasmon resonance is found to be $\hbar\omega_{sp} = 2.34$ eV. The SQD-MNP separation d is chosen to be small enough to get a strong coupling between the nanoparticles. We perform calculations similar to those presented in Sec. III A to explicitly see the effect of the presence of a nearby MNP.

Figure 6 shows the contour plots for the populations of the bi- and one-exciton states, calculated for the SQD-MNP center-to-center distance $d = 18$ nm. In the ρ_{33} plot, the white dashed curve displays the dependence of the incident pulse area $\tilde{A}$ at which ρ_{33} attains its first maximum, calculated within the adiabatic limit adjusted to a hybrid. Here, Eq. (14) for an isolated SQD has to be modified by replacing the Rabi amplitude $\Omega_0(t)$ of the external field by the renormalized quantity $\tilde{\Omega}_0(t) = [1 + \alpha(\omega_0)/(2\pi d^3)]\Omega_0(t)$ [see Eqs. (6a) and (6b)]. Then for $\tilde{A}_{A_2=\pi}$ one gets

$$\tilde{A}_{A_2=\pi} = \varepsilon'_s \left| 1 + \frac{\alpha(\omega_0)}{2\pi d^3} \right|^{-1} \left(\pi \sqrt{\frac{\pi}{2}} \frac{\mu_{21}}{\mu_{32}} \Delta_B t_0 \right)^{1/2}. \quad (15)$$

In deriving Eq. (15), we took into account only the enhancement effect and neglected the self-action of the SQD, which is described by the feedback constants G_i [Eqs. (8a)–(8c)].

FIG. 7. Same as in Fig. 3, but for a hybrid with center-to-center distance $d = 18$ nm.

For the system parameters used here, the self-action effect is negligible (see Sec. IV).

In order to fit the numerical data, Eq. (15) should be corrected by a prefactor of 0.62 which does not depend on the SQD-MNP spacing d . As can be seen, modified in this way, Eq. (15) works excellently for large values of $\Delta_B t_0$ but breaks down for values of $\Delta_B t_0$ on the order of unity, exactly as in the case of the isolated SQD.

We note that in the case of the hybrid, more Rabi cycles occur at the same area A of the incident pulse than for the isolated SQD (compare Figs. 6 and 2). The origin of this difference lies in the enhancement of the external field magnitude in the presence of a nearby MNP by the factor $|1 + \alpha(\omega_0)/(2\pi d^3)|$. This feature will be present in all the following figures. For the hybrid parameters used here, this factor is ≈ 2.2 , which explains the doubling of the number of Rabi cycles for the hybrid in comparison with the isolated SQD, as observed from Figs. 6 and 2.

In Fig. 7, we plot the area dependence of ρ_{33} and ρ_{22} for the region of failure of the adiabatic theory. As can be seen, the adiabatic limit approximates the actual behavior better for growing t_0 and already starting from $t_0 = 8/\Delta_B$ can be safely applied. The slight buildup of the one-exciton population ρ_{22} on increasing the pulse area has the same origin as in the case of an isolated SQD (see Sec. III A 2).

Figure 8 shows an example of the population dynamics for a short pulse ($t_0 = 20/\Delta_B = 2/3$ ps $\ll \gamma_{21}, \gamma_{32}$), when the adiabatic limit is valid (see Sec. III A 2). Obviously, the characteristics of the time dependence of the populations are similar to those for an isolated SQD (compare with Fig. 4), except the number of Rabi cycles is larger due to the field enhancement effect.

FIG. 8. Same as in Fig. 4, but for a hybrid with center-to-center distance $d = 18$ nm.

The population dynamics for a long incident pulse ($t_0 = 900/\Delta_B = 30$ ps) whose duration (≈ 60 ps) is already comparable with the spontaneous decay time of the biexciton state, $\gamma_{32}^{-1} = 120$ ps, is shown in Fig. 9. We observe that the population of the biexciton state decreases during the pulse action due to the spontaneous emission. Simultaneously, the one exciton is incoherently populated, which partly destroys the TPRO.

The results presented in Figs. 6–9 were obtained for the SQD-MNP separation $d = 18$ nm. Figure 10 shows how the TPRO depends on this separation. The contour plot was obtained numerically for an incident pulse with $t_0 = 20/\Delta_B = (2/3)$ ps. Figure 10 clearly shows that the number of Rabi cycles decreases with increasing d , which is due to the reduction of the enhancement factor $|1 + \alpha(\omega_0)/(2\pi d^3)|$ for growing d . As a result, the pulse areas A at which the Rabi oscillations attain their successive maxima grow with d .

To conclude this section, we comment on how the distance between the SQD and MNP can be controlled. This may be done, for instance, by making use of peptide- or DNA-based SQD-MNP conjugation, which is achievable by means of methods of surface chemistry (see, e.g., Ref. [48] and references therein). After preparing conjugated SQD-MNP pairs

FIG. 9. Same as in Fig. 5, but for a hybrid with center-to-center distance $d = 18$ nm.

FIG. 10. TPRO in the SQD-MNP hybrid considered in this paper as a function of the interparticle distance d and the pulse area A . Plotted is the biexciton state population ρ_{33} for a hybrid calculated numerically for an incident pulse with $t_0 = 20/\Delta_B = (2/3)$ ps.

immobilized on a substrate, single-molecule spectroscopy can be exploited to investigate their optical response.

IV. EFFECTS OF THE SQD SELF-ACTION

In this section, we discuss the effect of the SQD-MNP self-action described by the complex-valued feedback parameters G_i ($i = 1, 2, 3$), Eqs. (8a)–(8c), on the TPRO of the hybrid. The feedback parameters are hidden in equations of motion (9a)–(9f). Their role is uncovered after substituting into Eqs. (9d) and (9f) the explicit expressions for the Rabi amplitudes Ω_{21} and Ω_{32} , Eqs. (6a) and (6b). The principal effects of the feedback are most pronounced in Eqs. (9d) and (9e):

$$\begin{aligned} \dot{\rho}_{21} = & -[i(\Delta_{21} + G_1^R Z_{21}) + \frac{1}{2}\gamma_{21} - G_1^I Z_{21}]\rho_{21} \\ & + i(\tilde{\Omega}_{32}^{0*}\rho_{31} - \tilde{\Omega}_{21}^0 Z_{21}) \\ & + i[(G_3^*\rho_{21}^* + G_2^*\rho_{32}^*)\rho_{31} - G_3\rho_{32}Z_{21}], \end{aligned} \quad (16a)$$

$$\begin{aligned} \dot{\rho}_{32} = & -[i(\Delta_{32} + G_2^R Z_{32}) + \frac{1}{2}(\gamma_{32} + \gamma_{21}) - G_2^I Z_{32}]\rho_{32} \\ & - i(\tilde{\Omega}_{21}^{0*}\rho_{31} + \tilde{\Omega}_{32}^0 Z_{32}) \\ & - i[(G_1^*\rho_{21}^* + G_3^*\rho_{32}^*)\rho_{31} + G_3\rho_{21}Z_{32}]. \end{aligned} \quad (16b)$$

Following from Eqs. (16a) and (16b), the self-action of the SQD gives rise to many additional nonlinearities compared to an isolated SQD ($G_i = 0$). Two of these should especially be mentioned, namely, (i) renormalization of the SQD frequencies, $\omega_2 \rightarrow \omega_2 + G_1^R Z_{21}$ and $\omega_3 \rightarrow \omega_3 + G_2^R Z_{32}$, and (ii) renormalization of the relaxation rates of the off-diagonal density matrix elements, $\gamma_{21}/2 \rightarrow \gamma_{21}/2 - G_1^I Z_{21}$ and $(\gamma_{21} + \gamma_{32})/2 \rightarrow (\gamma_{21} + \gamma_{32})/2 - G_2^I Z_{32}$ [compare the expressions in square brackets in Eqs. (9d) and (9e)], both depending on the corresponding population differences. Thus, during a pulsed excitation, which gives rise to time-dependent population differences, both the effective detunings away from resonance, $\Delta_{21} + G_1^R Z_{21}$ and $\Delta_{32} + G_2^R Z_{32}$, and the effective relaxation rates of the transitions, $(1/2)\gamma_{21} - G_1^I Z_{21}$ and $(1/2)(\gamma_{32} + \gamma_{21}) - G_2^I Z_{32}$, will be swept during the pulse action, which does not occur in the case of an isolated SQD ($G_i = 0$).

These two effects may, in principle, substantially modify the plasmon-assisted TPRO.

In our case of the CdSe/ZnSe-Au hybrid, the magnitudes of all feedback parameters $\hbar|G_i|$, calculated for the minimal center-to-center spacing $d = 18$ nm we used in our computations, turn out to be on the order of a few tenths of meV, i.e., a hundred times smaller than the biexciton binding energy $\hbar\Delta_B = 20$ meV. The spectral width of the longest pulse we employed ($t_0 = 900/\Delta_B = 30$ ps) is $\approx \hbar\Delta_B/1800 \approx 0.1$ meV, i.e., comparable to $|G_i|$, while for smaller t_0 it is even larger. Thus, the effects of the SQD self-action do not play any role in the range of parameters used to obtain the results presented in Sec. III B. Nevertheless, the SQD self-action effect might be important for other hybrids such as a ZnSe/ZnS (core/shell)-Ag heterodimer for which $\hbar\Delta_B = 2.5$ meV and all $|G_i|$ (taken at $d = 16$ nm) are on the order of Δ_B [36]. This situation requires additional study due to the complicated interplay of the enhancement and self-action effects.

V. SUMMARY

We conducted a theoretical study of the two-photon Rabi oscillations of a heterodimer comprising a semiconductor quantum dot and a metal nanosphere, considering the SQD as a three-level ladderlike system with ground, one-exciton, and biexciton states. The Rabi oscillations in an isolated InGaAs/GaAs quantum dot were investigated earlier in Ref. [20]. We took into account the spontaneous decay of the excitonic states, which was not done in Ref. [20], and found a trade-off between the adiabatic regime, supporting coherent TPRO, and spontaneous processes. While in the former case the TPRO can be realized, in the latter the spontaneous emission destroys the TPRO for the duration of incident pulses comparable to or longer than the spontaneous emission time. This limits the pulse width for which a coherent TPRO can be observed.

The presence of a MNP near the SQD results in an enhancement of the external field magnitude depending on the SQD-MNP center-to-center distance, which leads to increasing the number of Rabi cycles per pulse compared to an isolated SQD at the same magnitude of the external field. This effect may be advantageous for quantum technological applications that require the production of many entangled photon pairs per second.

We performed our calculations for a model system that may be realized in practice: a heterodimer composed of a closely spaced CdSe/ZnSe quantum dot and a gold nanosphere. Other candidates to observe the plasmon-assisted TPRO are ZnSe/ZnS (core/shell)-Ag hybrids and heterodimers composed of an InGaAs/GaAs quantum dot and a triangular silver nanoparticle, absorbing over a wide spectral range, from the visible to the infrared [49].

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